

Jet Fragmentation at CDF

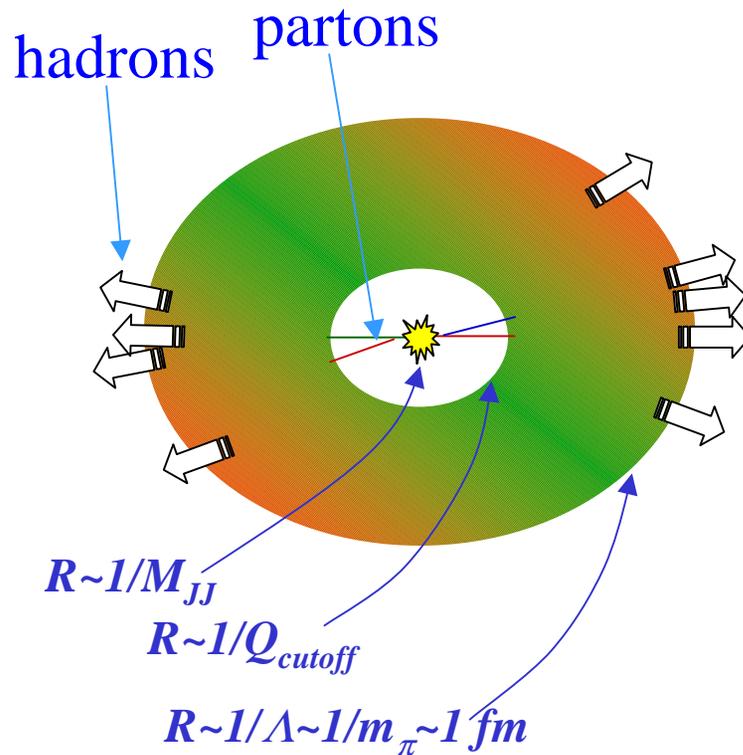
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- Theoretical Introduction.
- CDF Data and MLLA – first look.
- Consistency of results within MLLA framework.
- Comparison to model-independent measurements
- Discussion & Conclusion

Jet Fragmentation = pQCD + hadronization

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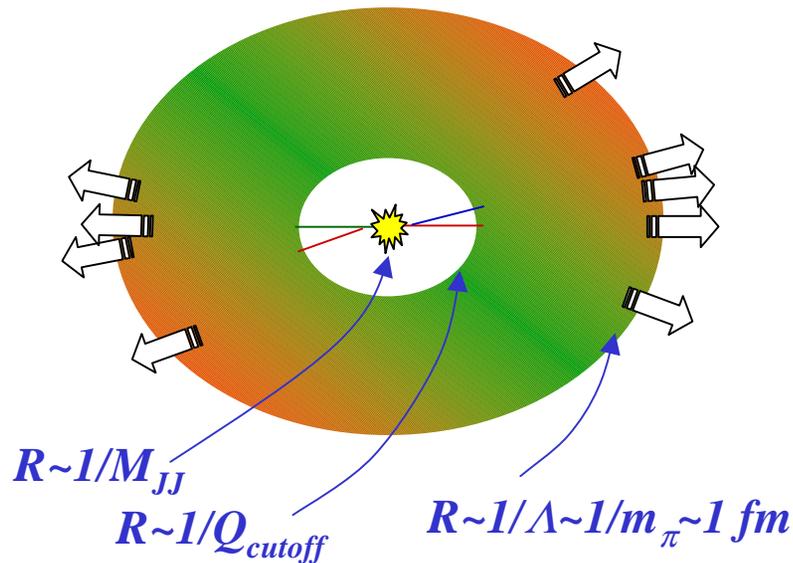
Fragmentation can be thought of as the two-stage process:

- pQCD stage that governs development of a parton shower
- Phenomenological hadronization that converts partons into hadrons

the fuzzy border between the two stages is usually associated with a k_T cut-off scale $Q_{cutoff} (\sim 1 \text{ GeV})$

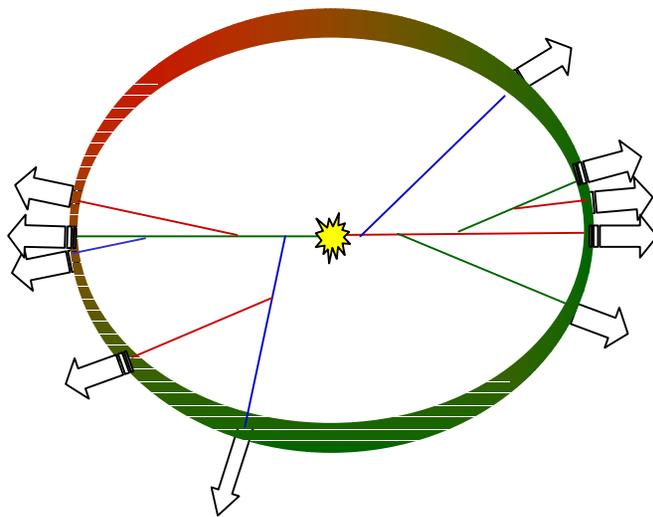
Perturbative or Non-Perturbative?

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Non-Perturbative scenario:

- Properties of final hadrons are largely determined by the stage of hadronization.
- Phenomenological methods have to be used.

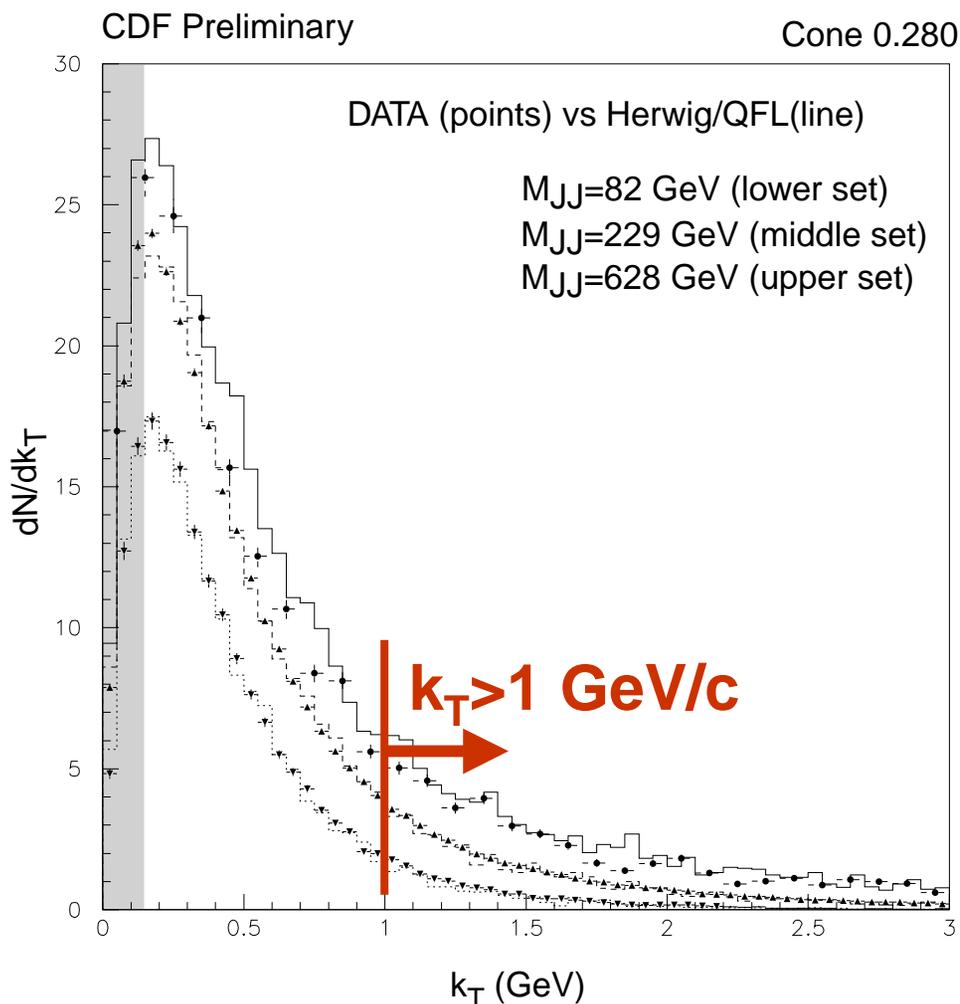


Perturbative scenario:

- Final hadrons “remember” properties of initial partons.
- Intra-jet characteristics can be analytically calculated in a consistent way (pQCD).

What If Perturbative?

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dN/dk_T distribution for tracks in cone 0.28 around the jet axis. CDF dijet events. Herwig scaled by 0.89.

- **Ordinary Perturbative QCD** ($k_T > 1$ GeV) \equiv dominance of the **phenomenological hadronization** (too few particles with such high k_T). Any predictions would rely heavily on hadronization model.
- One needs to handle particles in the region of k_T well below 1 GeV.
- **“Improved” perturbative model needed!**

Perturbative Dominance Scenario.

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MLLA + LPHD

Mueller (1983); Dokshitzer, Troyan (1984);
Malaza, Webber (1984)
(Modified Leading Log Approximation)

- Analytical results are infrared stable \Rightarrow cut-off scale parameter Q_{eff} can be pushed down to $\Lambda_{\text{QCD}} \sim 250 \text{ MeV}$.

• **Soft partons are accounted for!**

Azimov, Dokshitzer, Khoze, Troyan (1985)
(Local Parton-Hadron Duality)

- Hadronization occurs locally at the last moment \Rightarrow hadrons “remember” features of parton distributions.

$$N_{\text{hadrons}}/N_{\text{partons}} = K_{\text{LPHD}}$$

• **Hadron distributions are related to Parton ones!**

Result = Perturbative Model, which potentially may coherently describe jet fragmentation!

Two parameters only - Q_{eff} and K_{LPHD}

MLLA Parameters.

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What is the most favorable scenario?

- Q_{eff} - as low as possible (to include soft particles which constitute the majority of all). Preferably down to Λ_{QCD} .
- $K_{LPHD} \sim 1$ - "One parton becomes one hadron".
In our case (charged particles) $K_{LPHD}^{charged} \sim 1/2 - 2/3$.
- It would be nice to have something model-independent to compare the MLLA parameters to.

MLLA Predictions

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Gluon Jets:

- Multiplicity: $N_g(Y)$, $Y = \ln(E_{\text{jet}} \sin\theta / Q_{\text{eff}})$
- Momentum distribution: $dN_g(\xi, Y)/d\xi$, $\xi = \log(1/x_p)$,
 $x_p = p/E_{\text{jet}}$

Quark Jets:

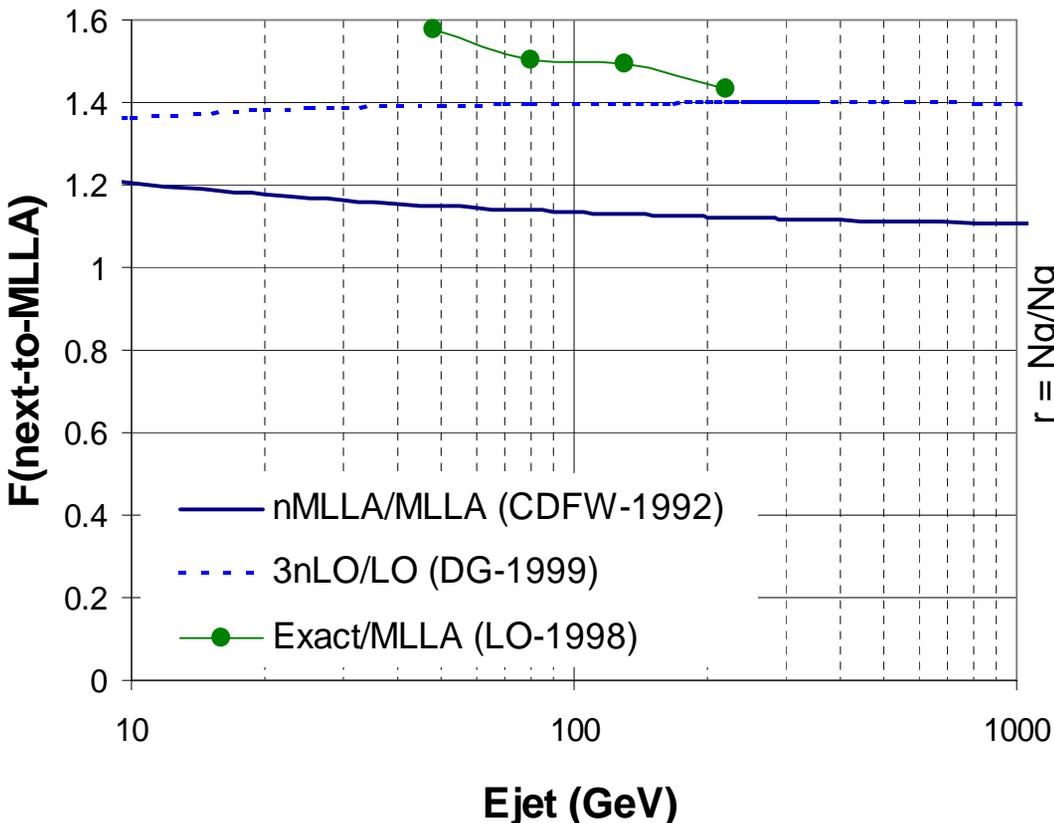
- quark jet is different by a normalization factor $1/r$, $r = C_A/C_F = 9/4$
- Multiplicity: $N_q(Y) = (1/r) \cdot N_g(Y)$
- Momentum distribution: $dN_q/d\xi = (1/r) \cdot dN_g/d\xi$

Next-to-MLLA Calculations.

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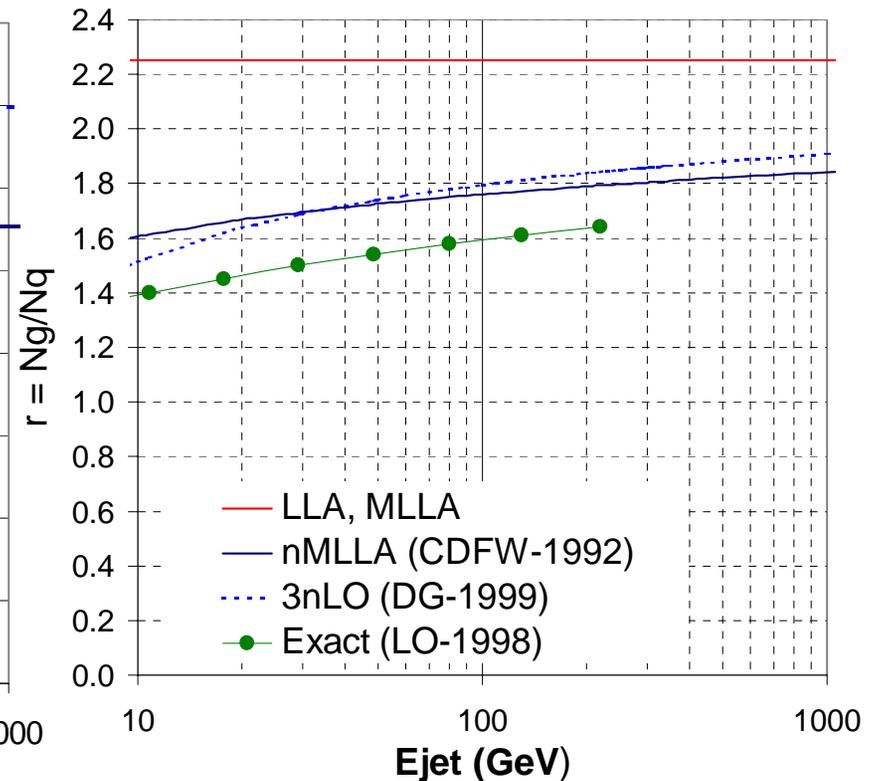
Change in gluon spectrum:

$$N_g^{next-to-MLLA}(Y, \xi) = F^{next-to-MLLA} N_g^{MLLA}(Y, \xi)$$



Change in ratio of multiplicities:

$$r = 9/4 \rightarrow 1.6 - 1.8$$



Analysis at CDF.

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- **CDF – Collider Detector at Tevatron,**
a $p\bar{p}$ - collider with $\sqrt{s} = 1800$ GeV

Explicit Advantages :

- Dijet masses available at CDF significantly expand potential area of study.
- $E_{\text{jet}} \theta / Q_{\text{eff}}$ scaling can be checked on a wide range of energies. (has never been done).
- Possibility to analyze data samples enriched either by quark or gluon jets.

Complications:

- Background environment is less trivial.
- Secondary events in the same bunch crossing.
- Underlying event debris.
- Tracker inefficiency, calorimeter response corrections and many others

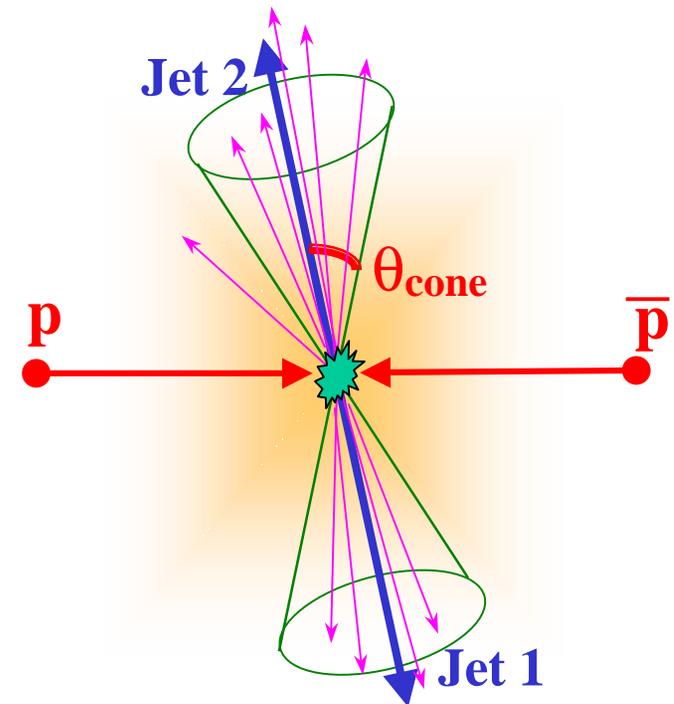
Major Detector
elements used:

- Vertex Chamber
- Central Tracker
- Calorimeters

Analysis at CDF.

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- CDF Run 1B Data.
- 100,000 Dijet Events : $M_{jj}=80 - 630 \text{ GeV}$
- Jets - Cone Algorithm
- both jets are in central region, well balanced ($E_{\text{jet}} \sim E_{T\text{jet}} \sim M_{jj}/2$)
- Particles counted in 3 cone-sizes $0.28 < \theta_{\text{cone}} < 0.47$ around the jet axis
- Mixture of quark and gluon jets



Data Analysis and Fits:

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- Hadron momentum distribution:

$$N_{hadron}(\xi) = \underbrace{K_{LPHD}^{charged} \left[\varepsilon_g(E_{jet}) + \frac{1}{r} (1 - \varepsilon_g(E_{jet})) \right]}_K F^{next-to-MLLA} N_g(\xi, Q_{eff}, E_{jet})$$

- Data was fitted with classic MLLA gluon spectrum, parameter $K \neq K_{LPHD}^{charged}$ and depends on E_{jet} :

$$K = K_{LPHD}^{charged} F^{next-to-MLLA} \left[\varepsilon_g(E_{jet}) + \frac{1}{r} (1 - \varepsilon_g(E_{jet})) \right]$$

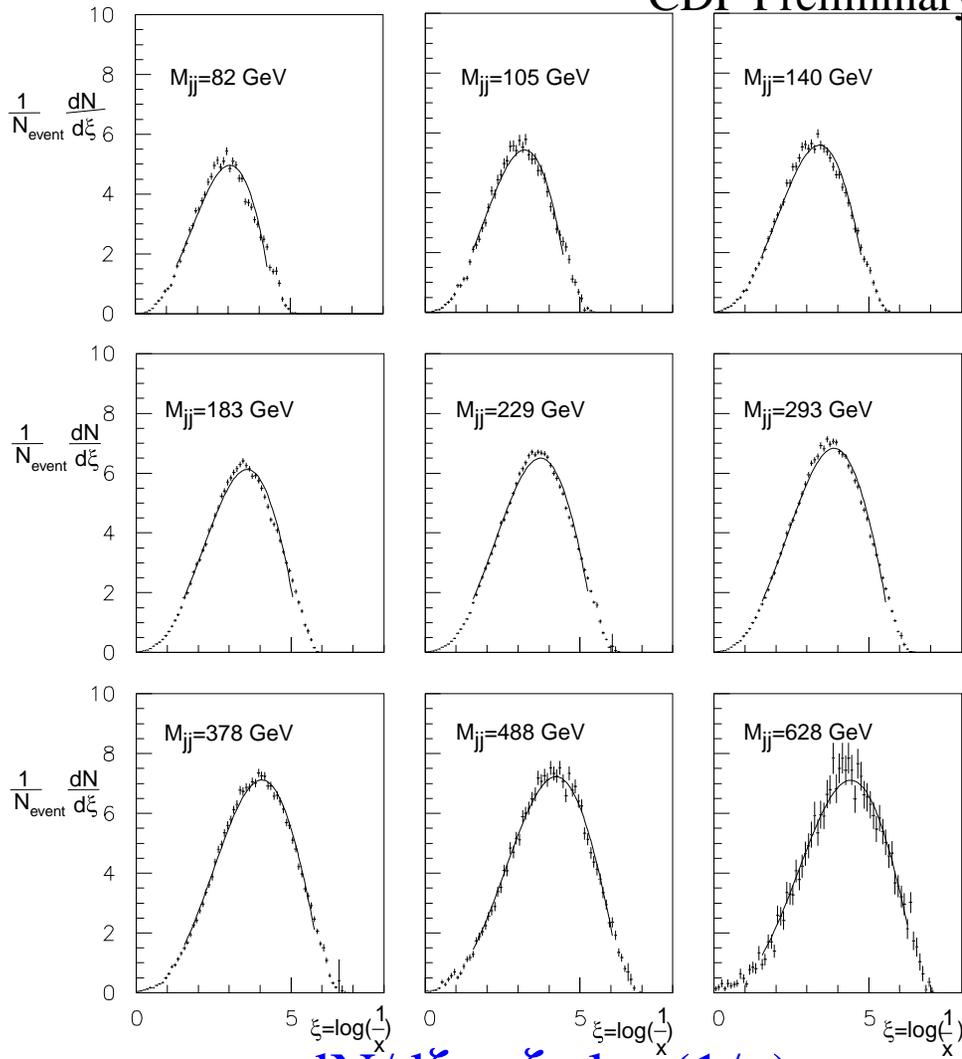
Parameters: $K_{LPHD}^{charged}$, r , Q_{eff}

Momentum Distribution of Particles

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M_{jj} -scan ($\theta_{cone}=0.47$), MLLA fit

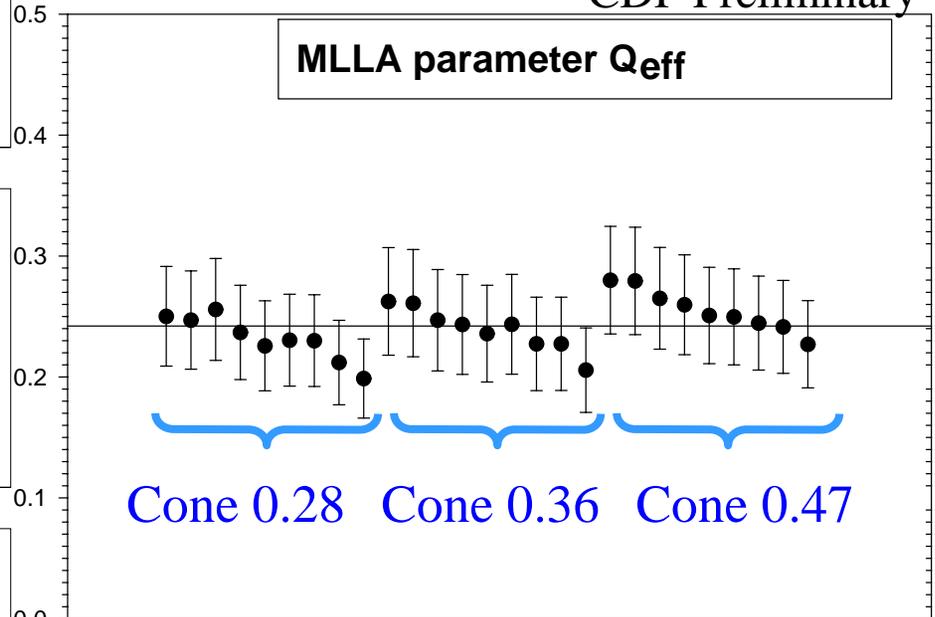
CDF Preliminary



$dN/d\xi, \xi = \log(1/x)$

Q_{eff} for all 9 M_{jj} 's and 3 opening cone-sizes

CDF Preliminary



MLLA fit $dN(\xi, Y)/d\xi$

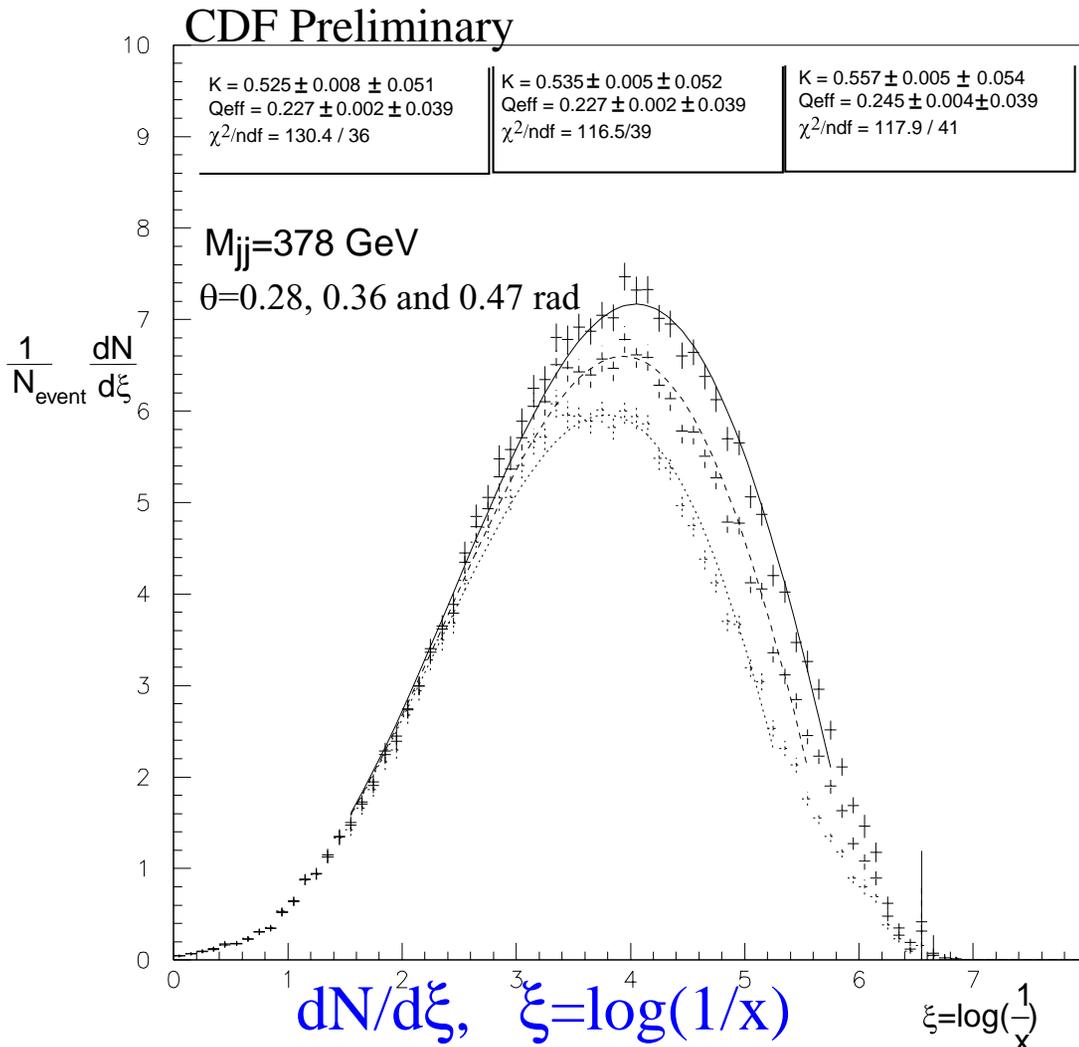
$Q_{eff} \approx \text{constant} = 240 \pm 40 \text{ MeV}$

Momentum Distribution of Particles

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$$K = K_{LPHD}^{charged} F_{next-to-MLLA} \left[\varepsilon_g(E_{jet}) + \frac{1}{r} (1 - \varepsilon_g(E_{jet})) \right]$$

For fixed M_{jj} , K should be cone-size independent



MLLA-fitted values of K :

- $\theta_{cone}=0.47$ $K=0.56 \pm 0.05$ (syst)
- $\theta_{cone}=0.36$ $K=0.54 \pm 0.05$ (syst)
- $\theta_{cone}=0.28$ $K=0.53 \pm 0.05$ (syst)

Fit of all three distributions with a single Q_{eff}

- $\theta_{cone}=0.47$ $K=0.53 \pm 0.05$ (syst)
- $\theta_{cone}=0.36$ $K=0.52 \pm 0.05$ (syst)
- $\theta_{cone}=0.28$ $K=0.52 \pm 0.05$ (syst)

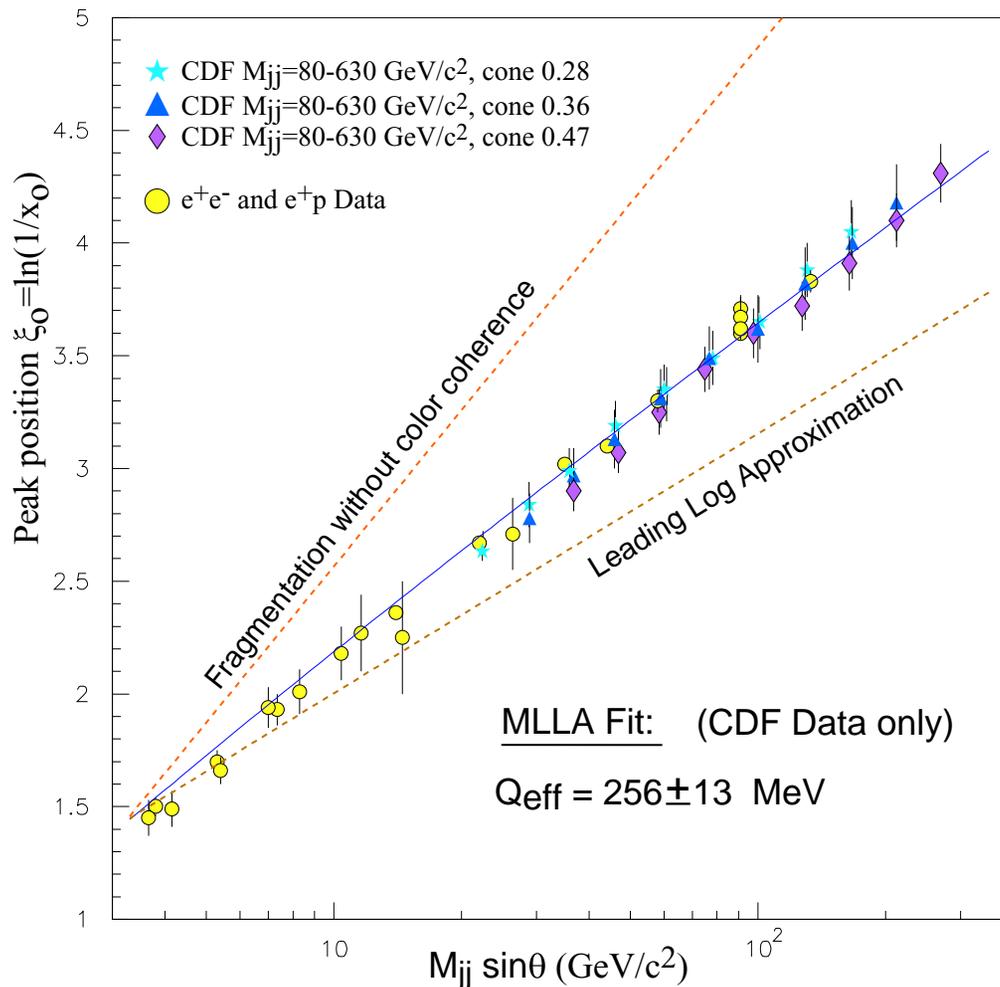
Peak of the Momentum Distribution

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In MLLA peak ξ_0 vs. M_{JJ} : $\xi_0 = 1/2 Y + (cY)^{1/2} - c$,

$Y = \ln(E_{jet} \sin\theta / Q_{eff})$, $c = 0.29$ for $n_f = 3$

CDF Preliminary



Peak ξ_0 vs. $M_{JJ} \sin\theta$ fit:
 $Q_{eff} = 256 \pm 13$ MeV

Intermediate Summary

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Based on the momentum distribution:

- Q_{eff} is not constant but “reasonably universal” and has a plausible value (~ 240 MeV).
- K shows some unexpected (but very moderate) trends, such as a slight fall for smaller angles.
- $(E_{\text{jet}}\theta/Q_{\text{eff}})$ scaling is evident (peak evolution)

Conclusion:

- Data supports the perturbative dominance scenario.
- Moderate deviations from the theory may indicate presence of higher order and hadronization effects.

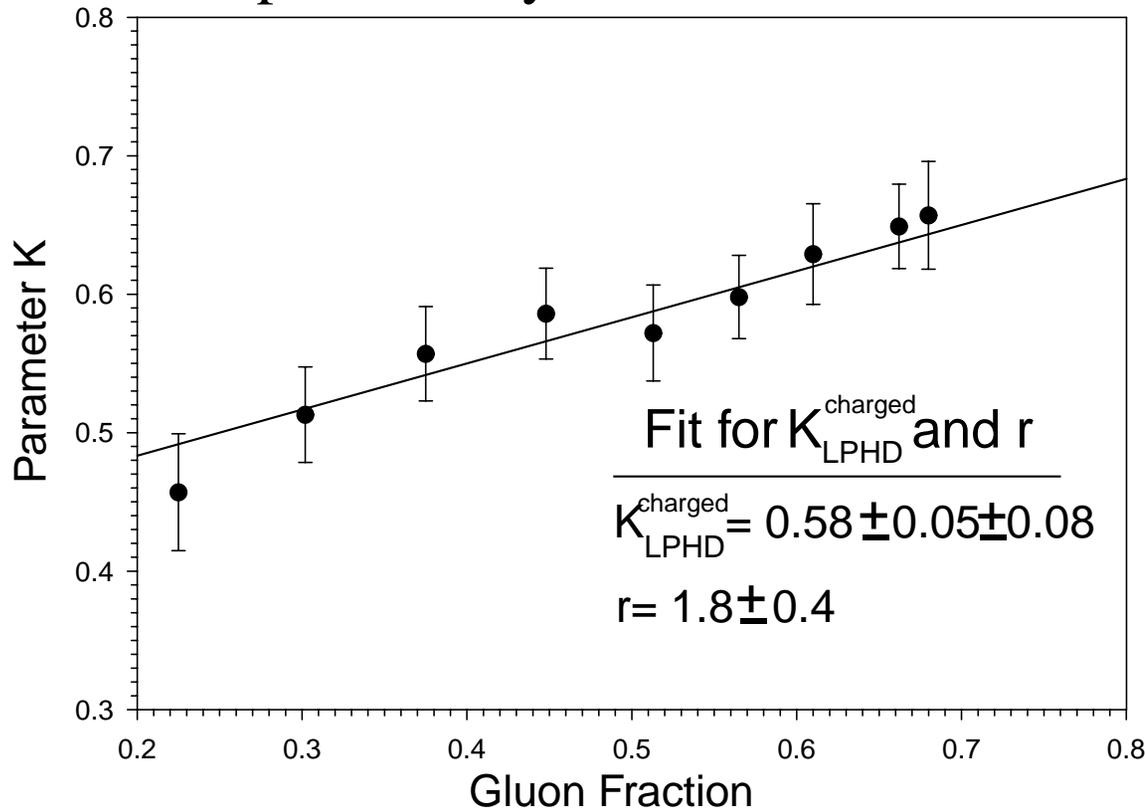
Momentum Distribution of Particles

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$$K = K_{LPHD}^{charged} F^{next-to-MLLA} \left[\varepsilon_g(E_{jet}) + \frac{1}{r} (1 - \varepsilon_g(E_{jet})) \right]$$

(Linear if plotted K vs ε_g)

CDF preliminary



(assuming $F^{next-to-MLLA} = 1.35 \pm 0.15$)

K vs. gluon jet fraction

fit:

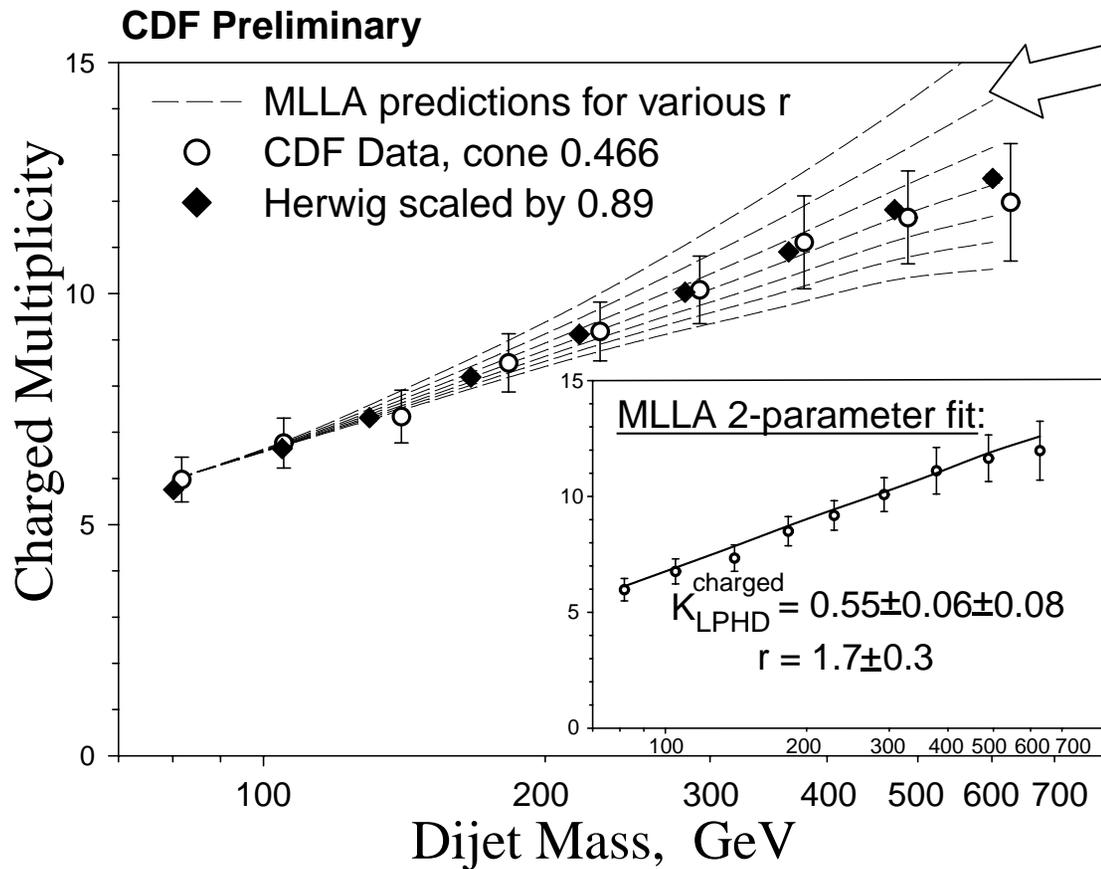
–indirect $r = 1.8 \pm 0.4$

– $K_{LPHD}^{charged} = 0.58 \pm 0.10$

The measurement is “indirect”: the result relies on MLLA-predicted $dN_g(\xi, E_{Jet})/d\xi$

Multiplicity in Dijet Events

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dashed curves from top to bottom
 $r=1.0, 1.2, 1.4, 1.6, 1.8, 2.0, 2.25$

MLLA fit of N_{jet} vs. M_{JJ} :
 -indirect $r=1.7 \pm 0.3$
 - $K_{LPHD}^{\text{charged}} = 0.55 \pm 0.10$

(assuming $F^{\text{next-to-MLLA}} = 1.35 \pm 0.15$)

The measurement is
 “indirect”: result relies
 on MLLA-governed
 dependence $N_g(E_{\text{Jet}})$

Another Intermediate Summary

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Analysis in the framework of MLLA:

Assuming next-to-MLLA correction $F^{\text{next-to-MLLA}} = 1.35 \pm 0.15$:

Momentum spectrum:

$$K_{LPHD}^{\text{charged}} = 0.58 \pm 0.10$$

$$r = 1.8 \pm 0.4$$

Multiplicity:

$$K_{LPHD}^{\text{charged}} = 0.55 \pm 0.10$$

$$r = 1.7 \pm 0.3$$

- Self-consistent, even though multiplicity measurement does not rely on the shape of the spectrum!
- r was treated as a free parameter, but still indirect!

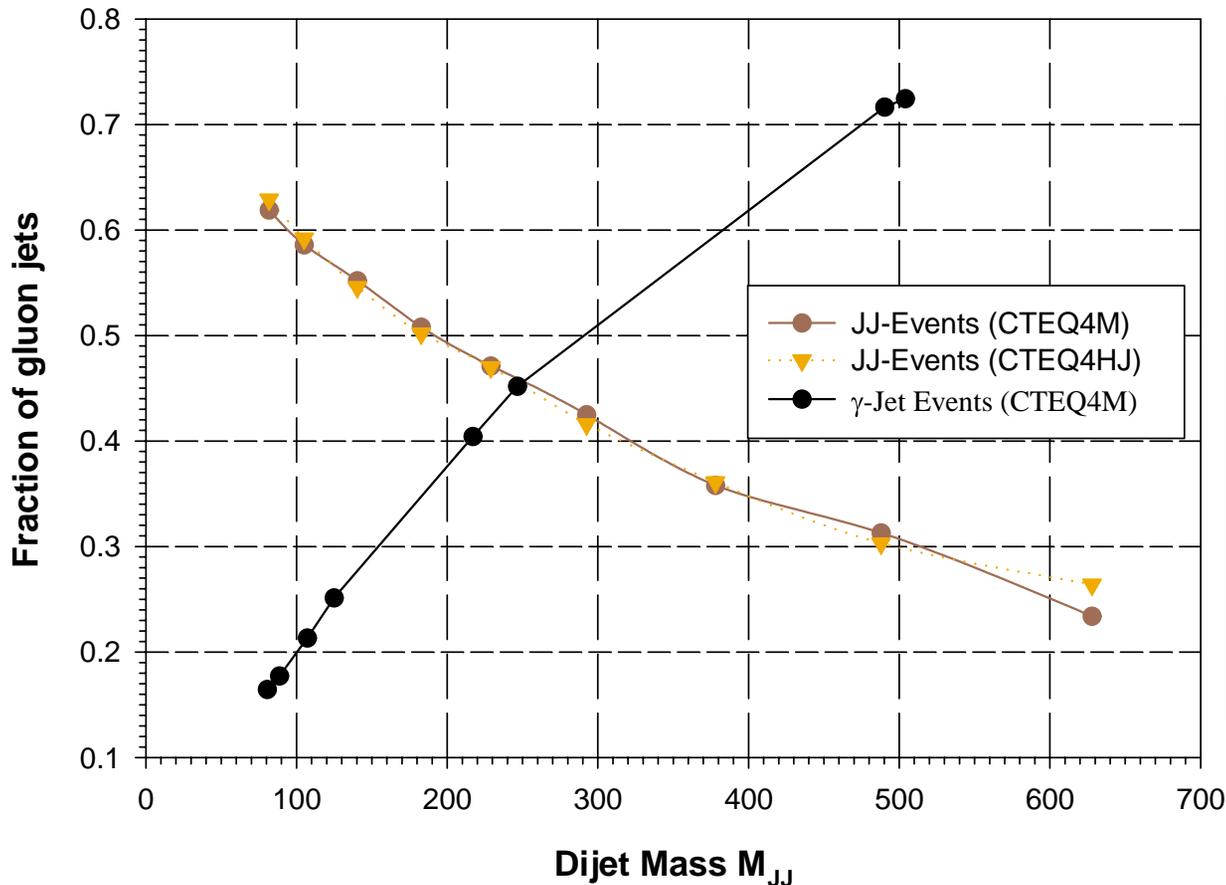
Does it all make sense? Is it consistent with everything else?

Ratio of Gluon/Quark Jet Multiplicities.

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To measure ratio r in a model-independent way, one may compare two samples with different gluon/quark jet fractions.

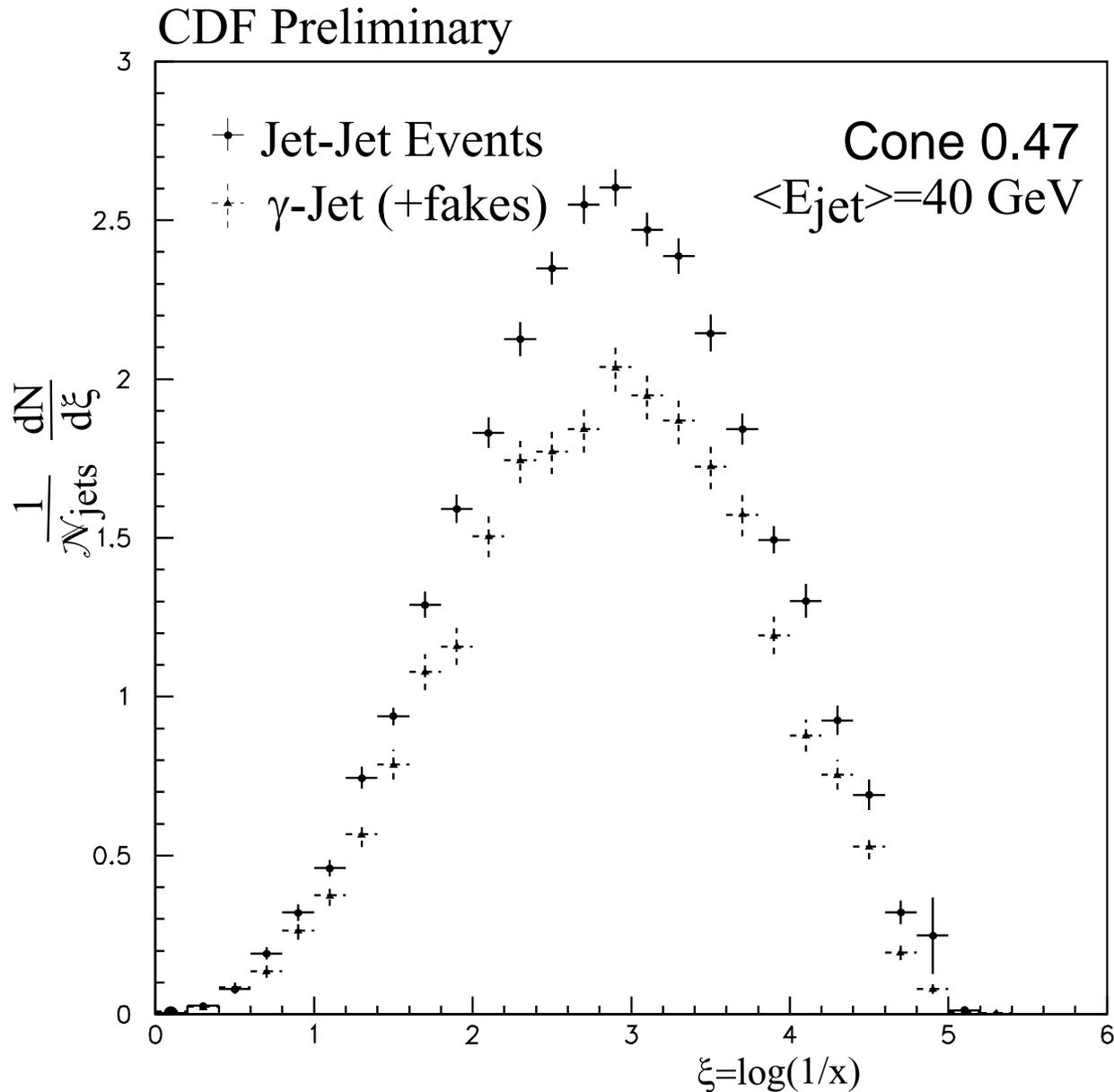
Dijet events vs photon+jet events is one of the choices.



•Fractions of gluon jets in dijet and photon+jet events (Herwig5.6)

Momentum Spectrum

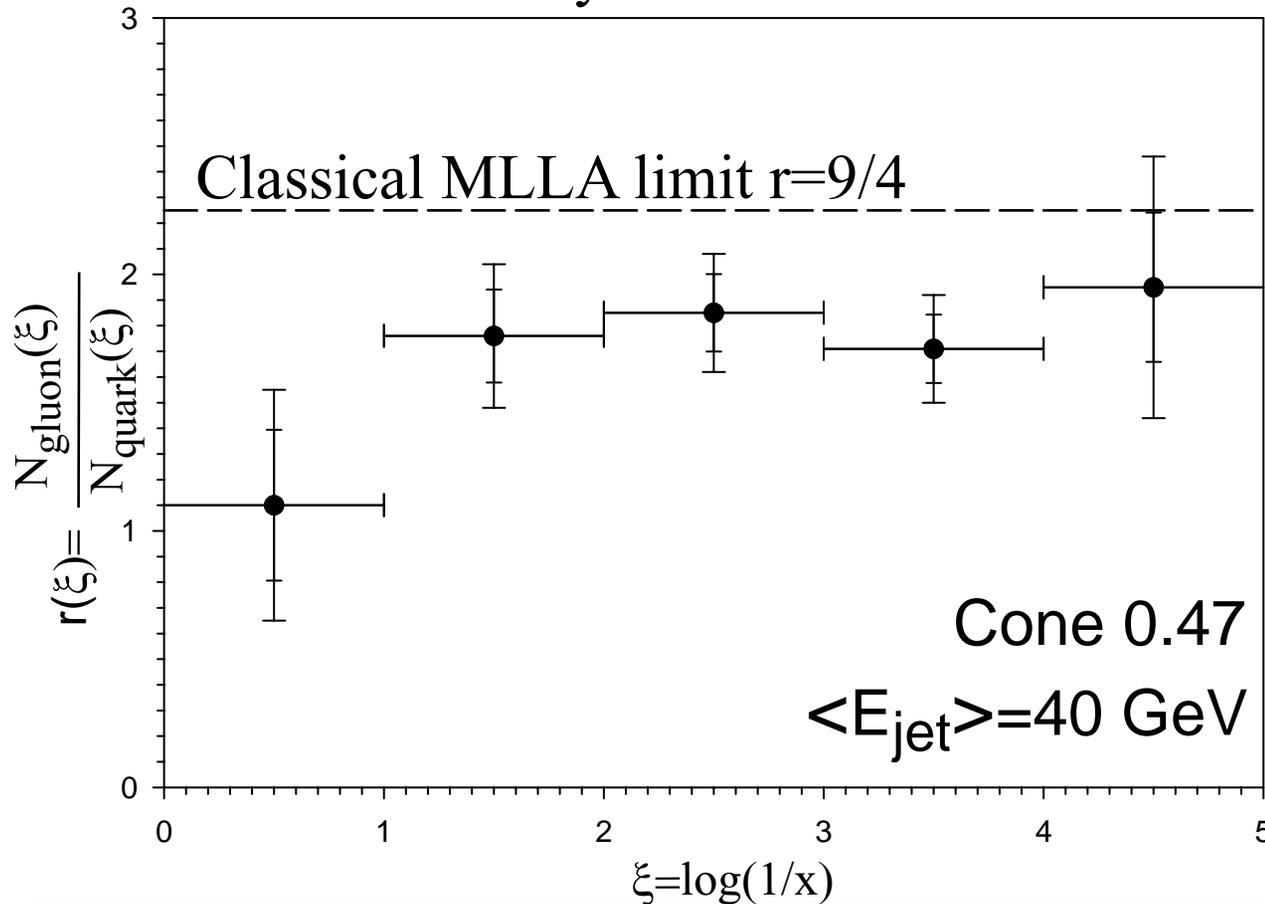
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- Purity of the photon+jet sample $\sim 70\%$
- Distributions are clearly different.
- Ratio r is greater than one!

Ratio of Gluon/Quark Momentum Distributions

CDF Preliminary

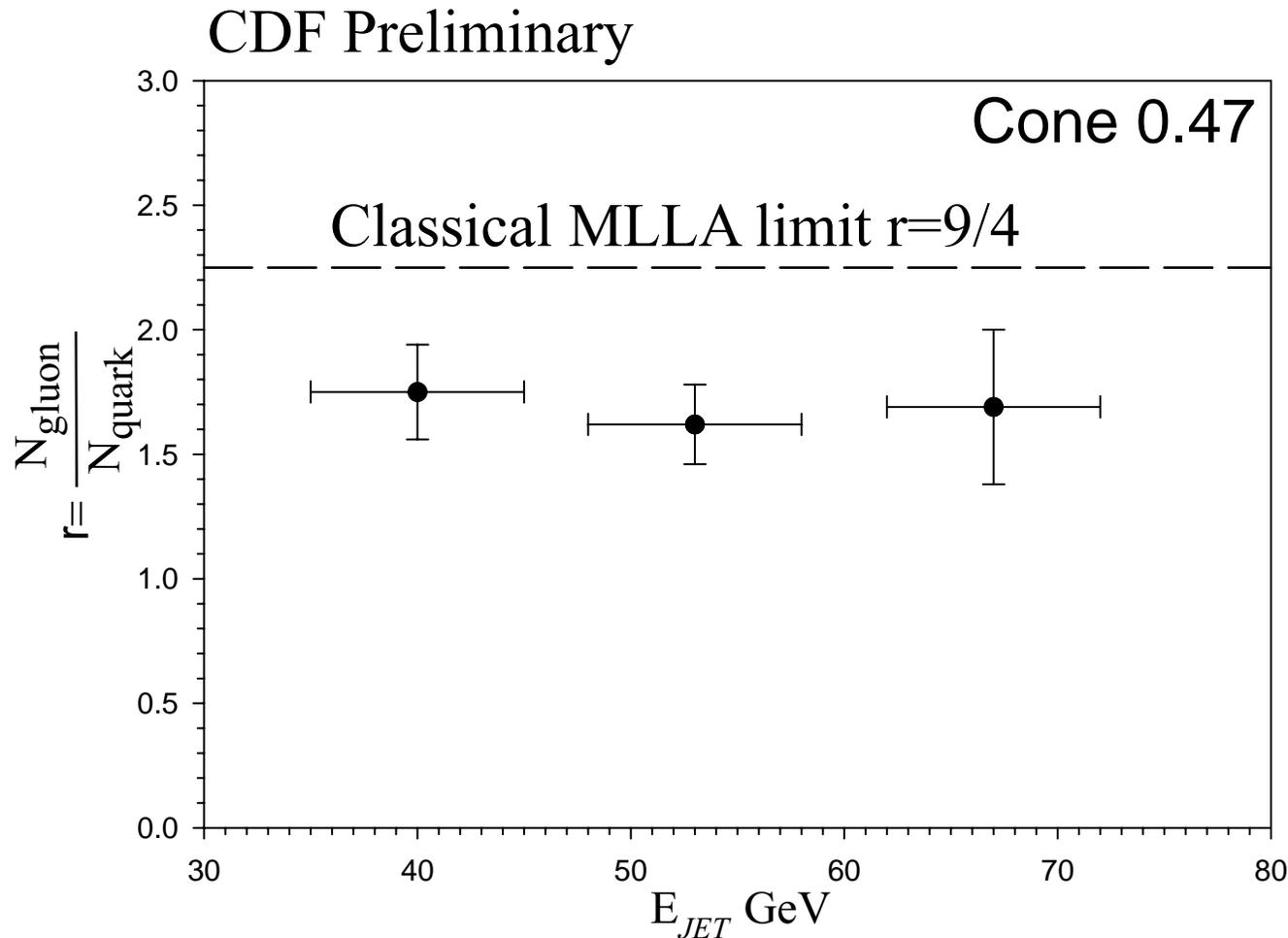


$$r(\xi) = \frac{N_{gluon}(\xi)}{N_{quark}(\xi)}$$

r may depend on particle momentum, being larger for soft particles, but errors are too large for conclusive judgements

Dependence of r on Jet Energy

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$$r = \frac{N_{gluon}}{N_{quark}}$$

For $E_{jet} = 40$ GeV, $r = 1.76 \pm 0.1$

Consistency Checks

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Measurement in MLLA context

Model-independent measurement expectation

r , ratio of particle multiplicities in gluon and quark jets:

$$r=1.7\pm 0.3 \text{ (shape)}$$

$$r=1.8\pm 0.4 \text{ (total multiplicity)}$$

$$r=1.76\pm 0.11\pm 0.15$$

(comparison of dijet and γ -jet events)

Parton-to-hadron Conversion rate $K_{LPHD}^{charged}$:

$$K_{LPHD}^{charged}=0.58\pm 0.10 \text{ (shape)}$$

$$K_{LPHD}^{charged}=0.55\pm 0.10 \text{ (multiplicity)}$$

isotopic invariance $\rightarrow 1/2 - 2/3$

fraction of jet energy carried by charged particles $f=0.55\pm 0.01$
[TASSO]

MLLA cut-off scale Q_{eff} : $Q_{eff} = 240 \pm 40 \text{ MeV (shape)}$
 $Q_{eff} = 256 \pm 13 \text{ MeV (peak position)}$

Conclusions

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- This study is the first detailed and comprehensive wide-range experimental comparison of the MLLA predictions to the data.
- Our results show reasonable and consistent agreement with the predictions of the MLLA, supporting the applicability of perturbative methods for jet fragmentation.
- Observed moderate deviations from the theory may indicate presence of higher order and hadronization effects.
- Run II of the Tevatron (2001) with significantly improved CDF detector and higher luminosity will present a perfect opportunity to continue these studies.