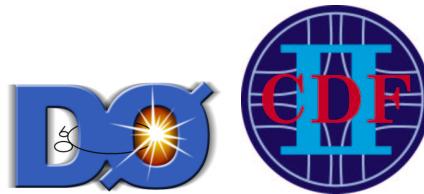


# **$B_d$ and $B_s$ Oscillations at the TeVatron**

Guillelmo Gómez-Ceballos

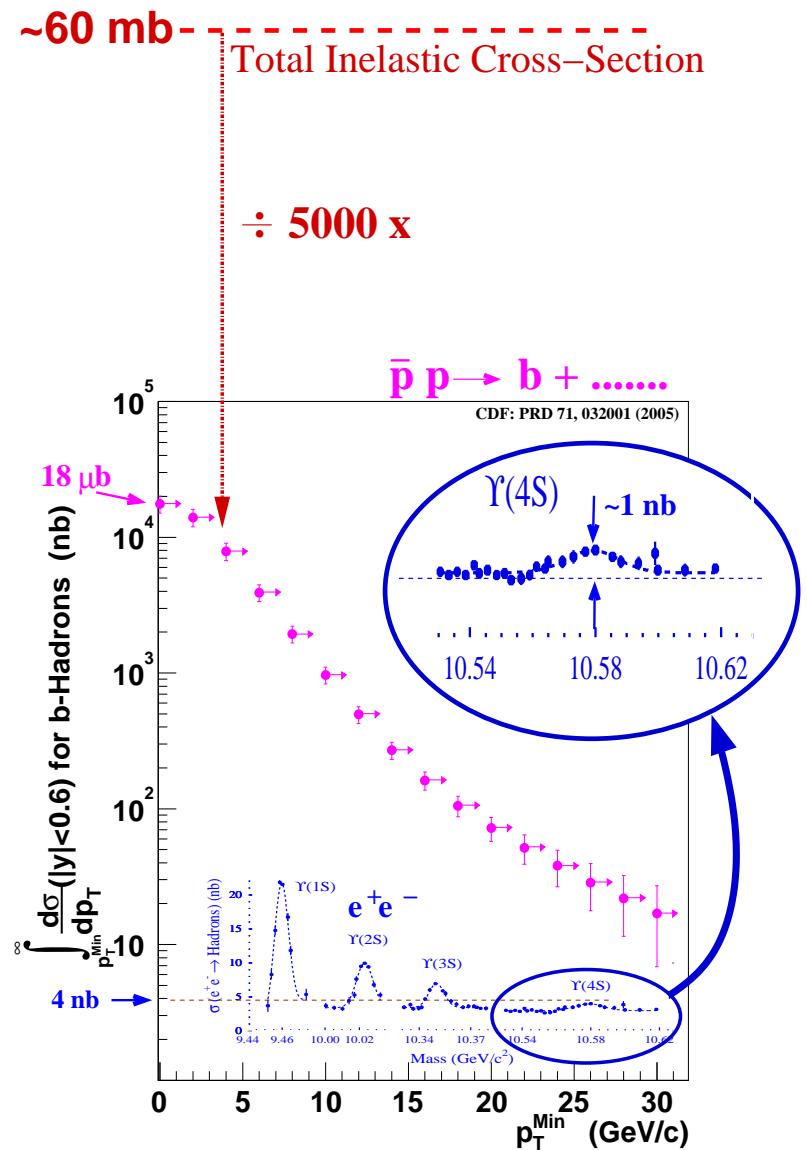
*Instituto de Física de Cantabria*

**On behalf of the DØ and CDF Collaborations**



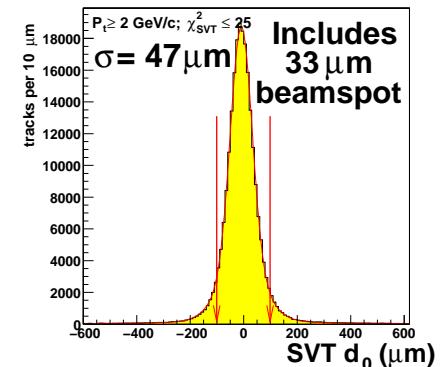
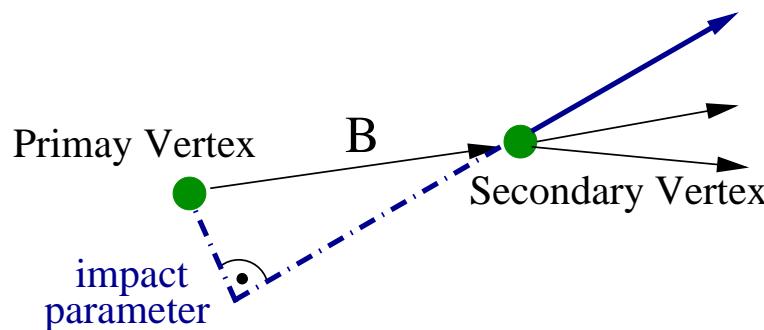
# B-Physics at Hadron Colliders

- + Large production rates  
 $\sigma(p\bar{p} \rightarrow bX, |y| < 0.6) \approx 18\mu b$   
 $10^3$  higher than at  $\Upsilon(4S)$
- + Heavy and excited B states currently uniquely at Tevatron:  
 $B_s, B_c, \Lambda_b, \Xi_b, B^{**}, B_s^{**}, \dots$
- + But QCD background is  $10^3$  higher than signal  
**Triggers are critical**
- + Event signature polluted by many fragmentation tracks;  
High precision **vertex tracker**  
+ dedicated **reconstruction algorithms** needed



# $B$ Triggers

- +  $B$  decays to  $J/\psi \rightarrow \mu^+\mu^- \rightarrow$  Di-muon trigger (CDF/DØ)
  - + easy trigger
  - + clean environment
- + Semileptonic  $B$  decays  $\rightarrow$  Single lepton trigger (DØ) + displaced track (CDF)
  - + large branching ratio
  - + missing momentum (neutrino & neutrals)



- + Fully hadronic  $B$  decays  $\rightarrow$  Two Track trigger (CDF)
  - + requires displaced track trigger
  - + requires fast online tracking

# Theoretical Predictions for $\Delta m$

$B^0/B_s^0$  mix through box diagram:

$$\Delta m_q \propto m_{B_q} \hat{B}_{B_q} f_{B_q}^2 |V_{tb} V_{tq}^*|^2$$

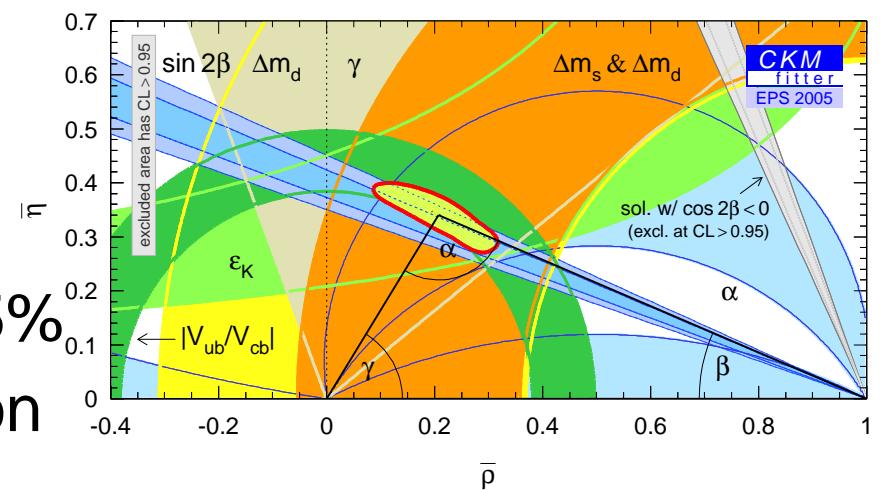
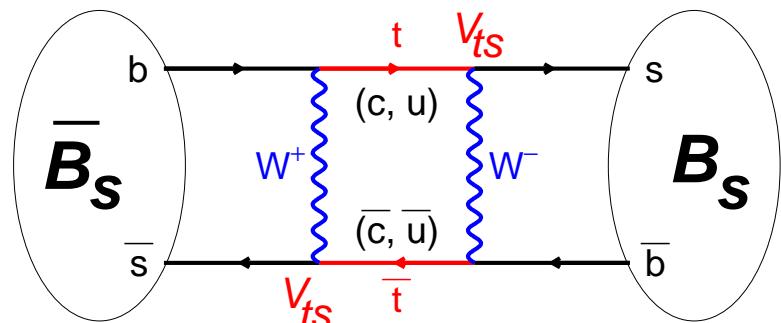
$$q = s, d$$

Uncertainties cancel in ratio:

$$\frac{\Delta m_s}{\Delta m_d} = \frac{m_{B_s}}{m_{B_d}} \xi^2 \frac{|V_{ts}|^2}{|V_{td}|^2}$$

with  $\xi^2 = 1.21 \pm 0.02^{+0.035}_{-0.014}$

- + measure  $\frac{\Delta m_s}{\Delta m_d} \rightarrow$  find  $\frac{|V_{ts}|^2}{|V_{td}|^2}$  to 2.5%
  - +  $\Delta m_d$  measured to high precision
  - +  $B_s$  Mixing hasn't been seen!
  - + Standard Model CKM fit:
- $$\Delta m_s = 18.3^{+6.5}_{-1.5} \text{ ps}^{-1}$$
- + potential new physics discovery



# $\Delta m_s$ Measurement

Why is this measurement so difficult?:

$B_s$  Mesons Mix much faster than  $B_d$  Mesons!

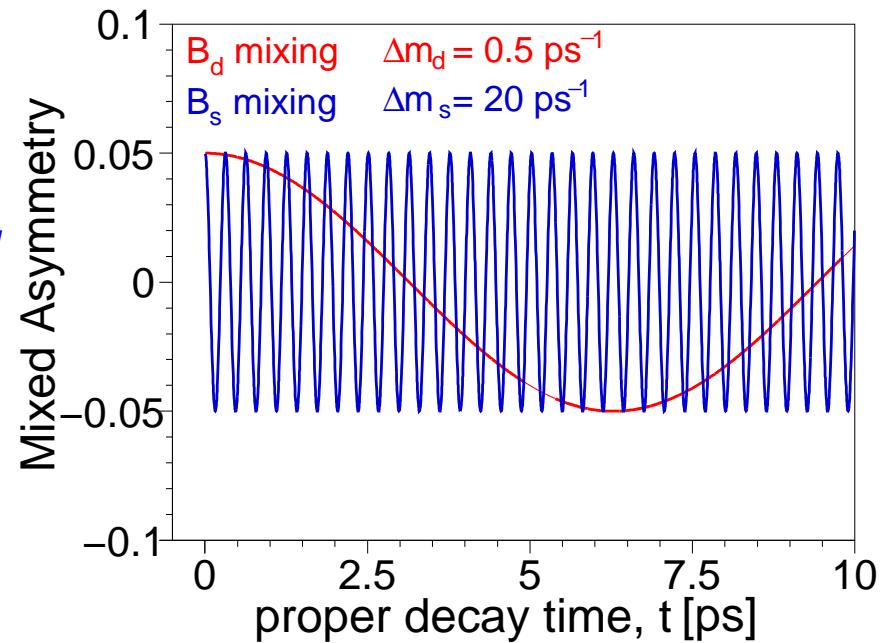
In order to measure:

$$\begin{aligned} \mathcal{A}_{mix}(t) &= \frac{N_{unmix}(t) - N_{mix}(t)}{N_{unmix}(t) + N_{mix}(t)} \\ &= \mathcal{D} * \cos(\Delta m_s t) \end{aligned}$$

We need to:

- + Reconstruct  $B_s$  signal in:
  - + hadronic modes
  - + semileptonic modes
- + Proper decay length resolution: fully reconstructed modes provide better accuracy
- + Tag the production flavor (the -key- problem in a hadron collider!): tagging power  $\varepsilon \mathcal{D}^2$

Efficiency:  $\varepsilon = \frac{N_{wrong} + N_{right}}{N}$ ; Dilution:  $\mathcal{D} = 1 - 2 \frac{N_{wrong}}{N_{wrong} + N_{right}} = \frac{N_{right} - N_{wrong}}{N_{wrong} + N_{right}}$

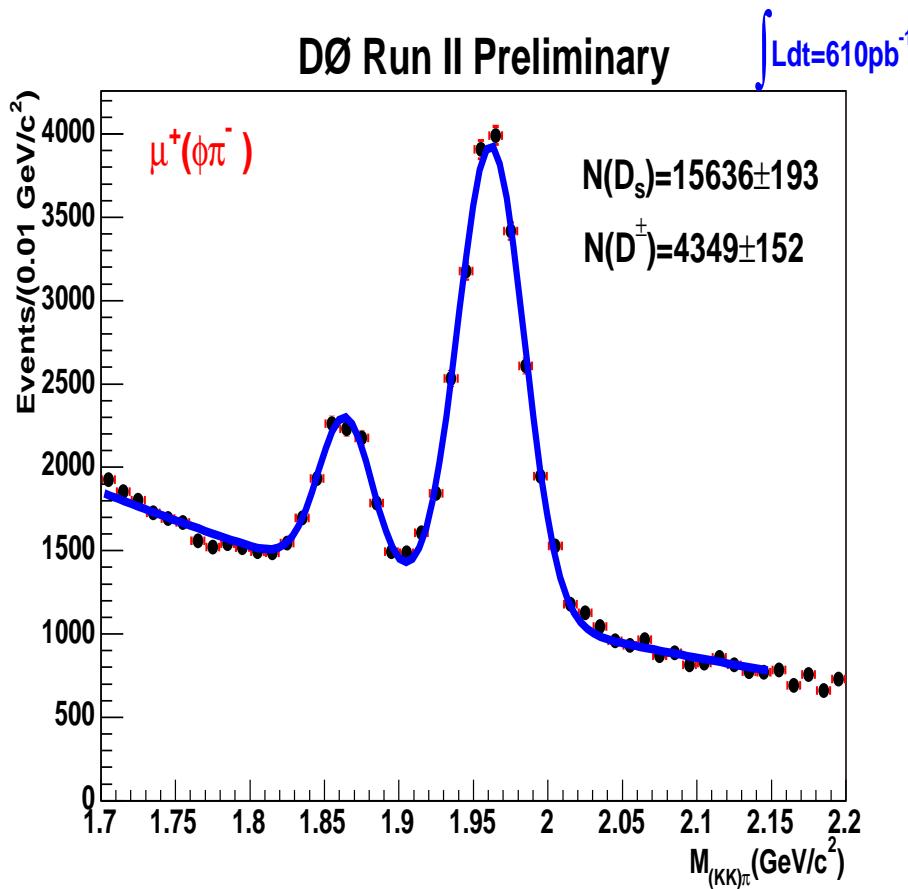


Significance  $\propto \varepsilon \mathcal{D}^2 \frac{S}{\sqrt{S+B}} e^{-\Delta m_s^2 \sigma_t^2 / 2}$

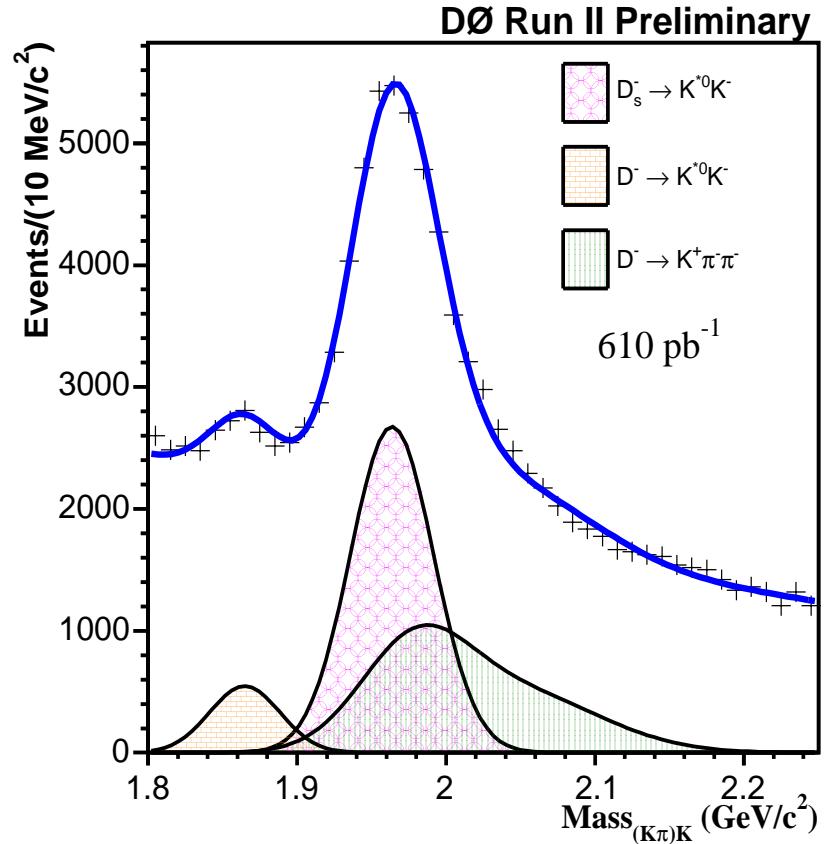
# Reconstructed $B \rightarrow IDX$ Candidates (DØ)

DØ exploits high statistics  $\mu$  trigger semileptonic decays: **worse proper time resolution**, but **high statistics**

$$ct = \frac{L_{xy}}{\gamma\beta}; \gamma\beta = \frac{p_T(B)}{M(B)} = \frac{p_T(\ell D)}{M(B)} * K \quad (K \text{ from MC}); \sigma_{ct} = \left( \frac{\sigma_{L_{xy}}}{\gamma\beta} \right) \oplus \left( \frac{\sigma_{\gamma\beta}}{\gamma\beta} \right) * ct$$



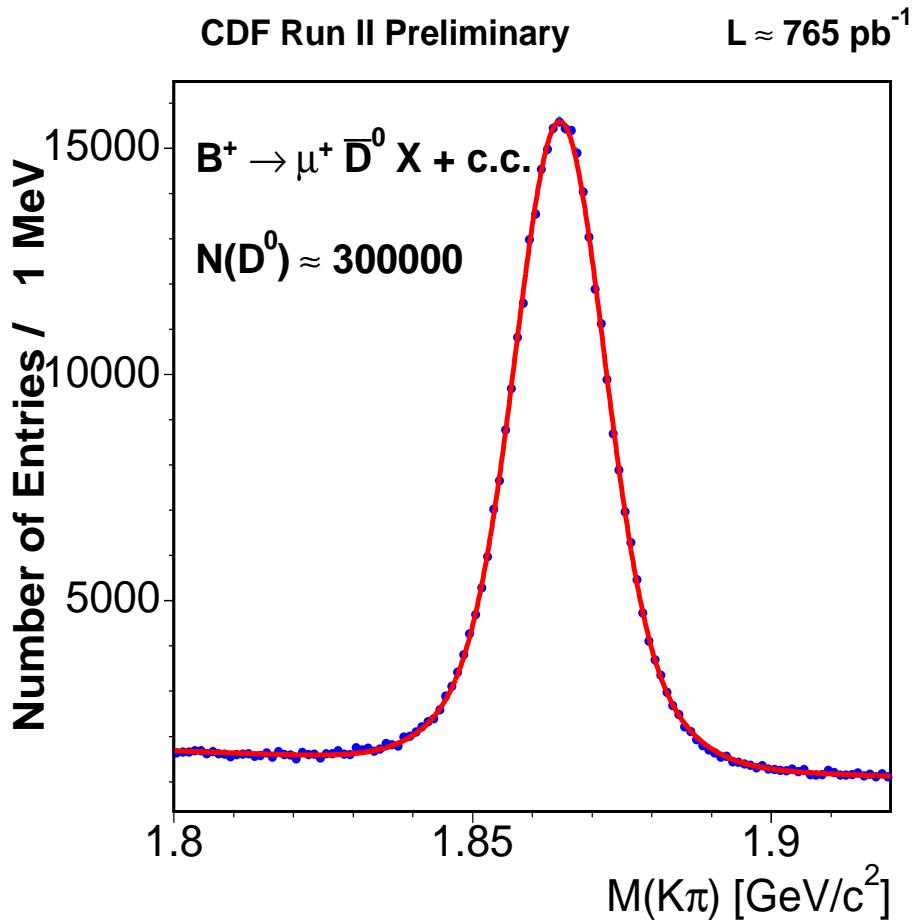
$D_s \rightarrow \phi\pi, \phi \rightarrow K^+K^-$



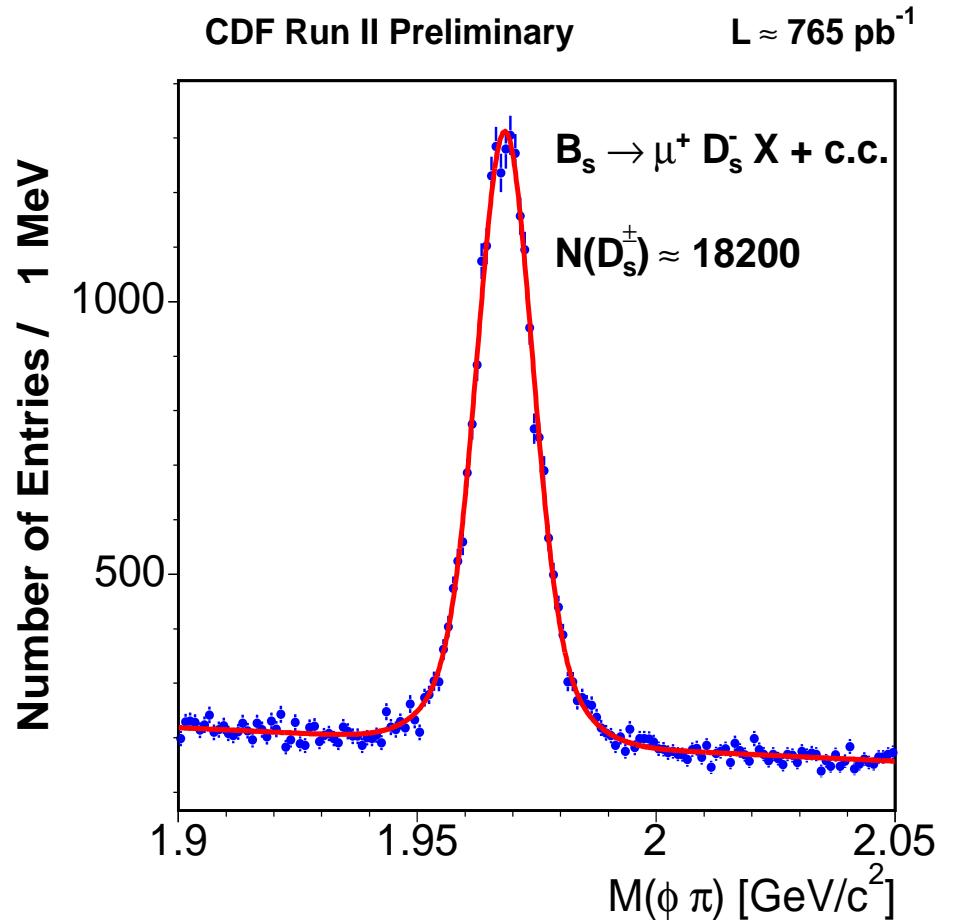
$D_s \rightarrow K^* K, K^* \rightarrow K\pi$

# Reconstructed $B \rightarrow IDX$ Candidates (CDF)

The most recent analysis uses semileptonic modes collected by the Two Track Trigger, new analysis in progress with  $\sim 765 \text{ pb}^{-1}$



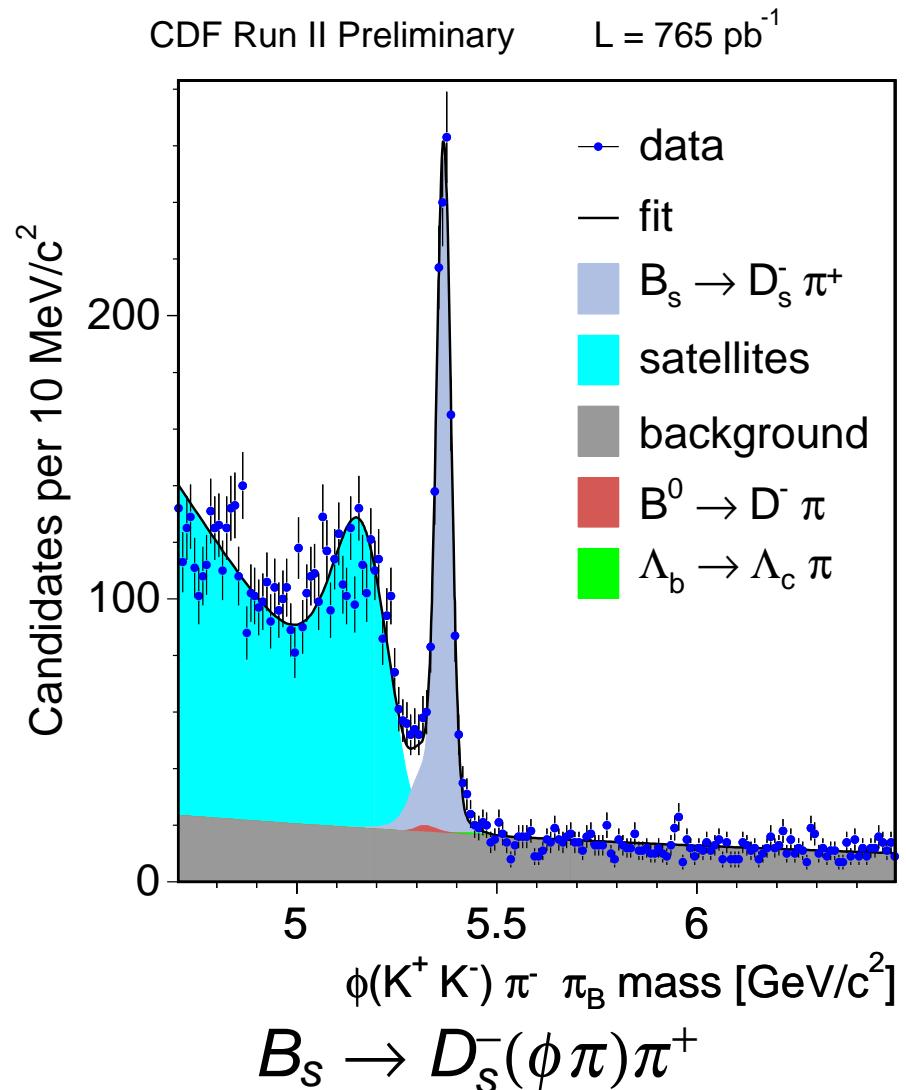
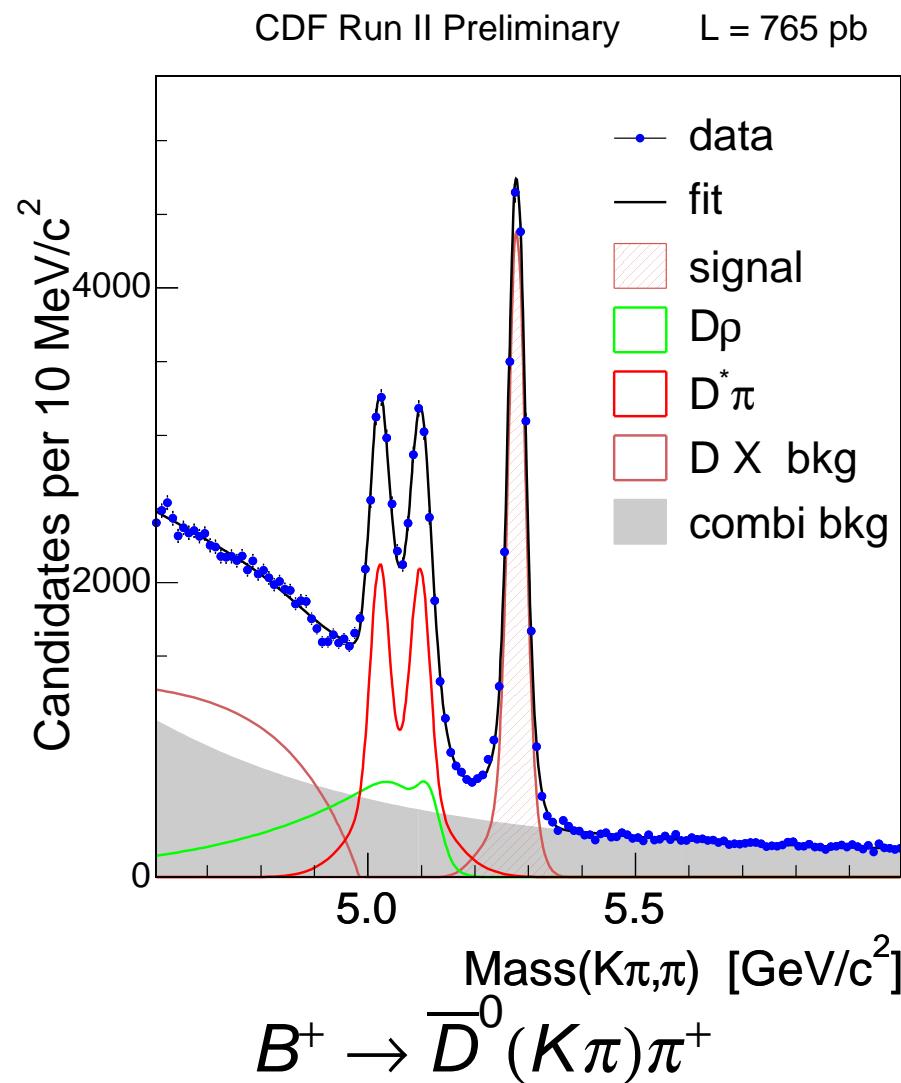
$$B^+ \rightarrow \mu^+ \bar{D}^0 (K\pi) X$$



$$B_s \rightarrow \mu^+ D_s^- (\phi\pi) X$$

# Fully Hadronic Decays (CDF)

More than 2300  $B_s$  signal candidates with  $\sim 765 \text{ pb}^{-1}$



# Proper Decay Time Reconstruction

---

Algorithm:

- + measure transverse momenta  $p_T$  of all decay products
- + measure the decay length  $L_{xy}$  from the P.V. to decay vertex
- + boost meson back to its rest frame

Fully reconstructed decays  $B_s \rightarrow D_s(3)\pi$

- + all daughters reconstructed
- + formula for proper decay time:  $ct = L_{xy} \frac{m_B}{p_T}$

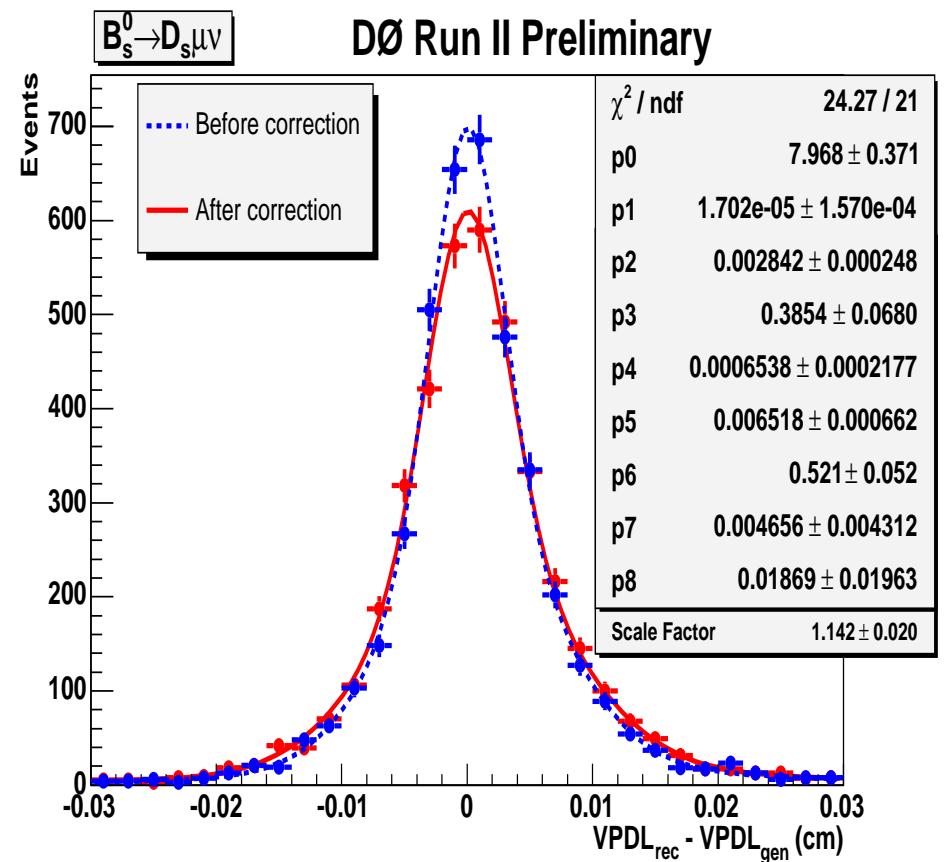
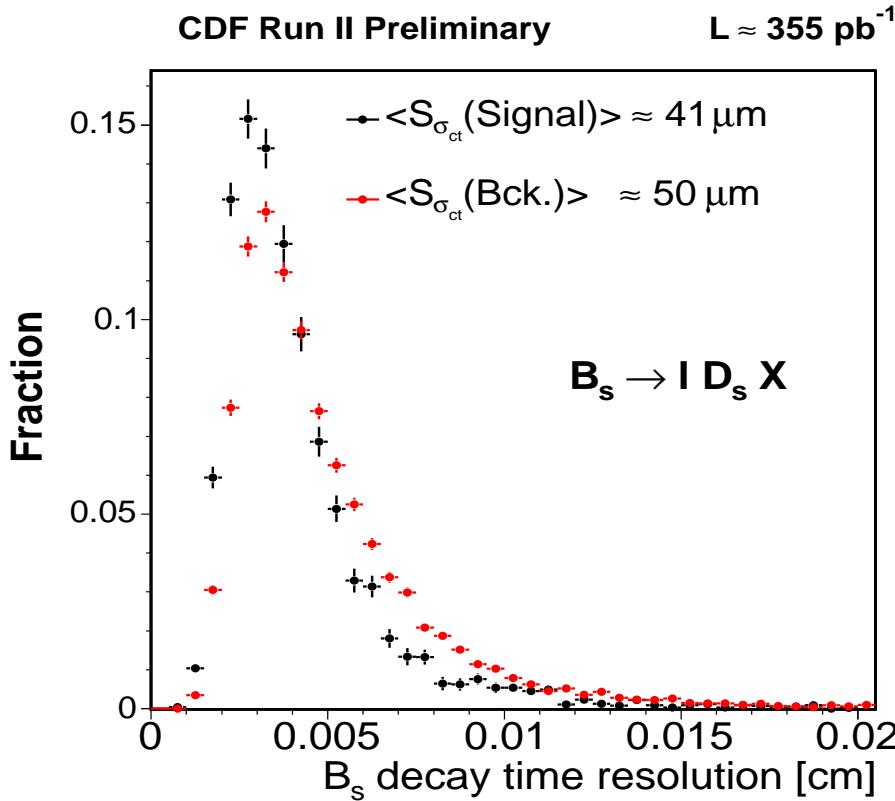
Inclusively reconstructed decays  $B_s \rightarrow \ell\nu D_s X$

- + some decay products escape detection ( $\nu$ , neutrals, etc)
- + missing momentum  $\Rightarrow$  increased ct error ( $\sigma_{ct}$ )
- + formula for proper decay time:

$$ct = L_{xy} \frac{m_B}{p_T} \cdot K, \quad \text{where } K = \left\langle \frac{p_T^{\ell D}}{p_T^B} \right\rangle \text{ from MC}$$

# $\sigma_{ct}$ Resolution Studies

The proper decay length resolution is the limiting factor at high  $\Delta m_s$   
 Studies on this topic play a very important role!



$\sigma_{ct}$ : signal/background  
 (CDF)

$\sigma_{ct}$ : before/after tuning  
 (DØ)

# $B$ Flavor Tagging

## Opposite Side Tagging:

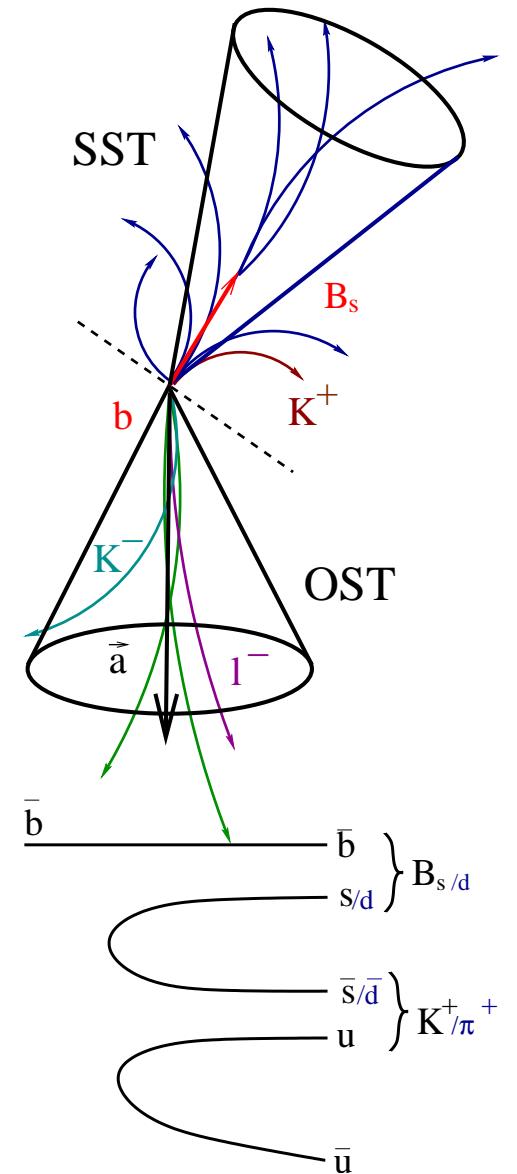
- **Jet-Charge-Tagging:** (used at CDF/DØ)  
sign of the weighted average charge of opposite B-Jet
- **Soft-Lepton-Tagging:** (used at CDF/DØ)  
identify soft lepton ( $e, \mu$ ) from semileptonic decay of opposite B:  $b \rightarrow l^- X$  ( $BR \approx 20\%$ ),

Dilution due to  $\bar{b} \rightarrow \bar{c} \rightarrow \Gamma X$  and oscillation

- **Kaon-Tagging:** (in progress at CDF)  
due to  $b \rightarrow c \rightarrow s$  it is more likely that a  $\bar{B}$  meson contains a  $K^-$  than a  $K^+$  in the final state (particle ID is mandatory)

## Same Side Tagging : (in progress at CDF)

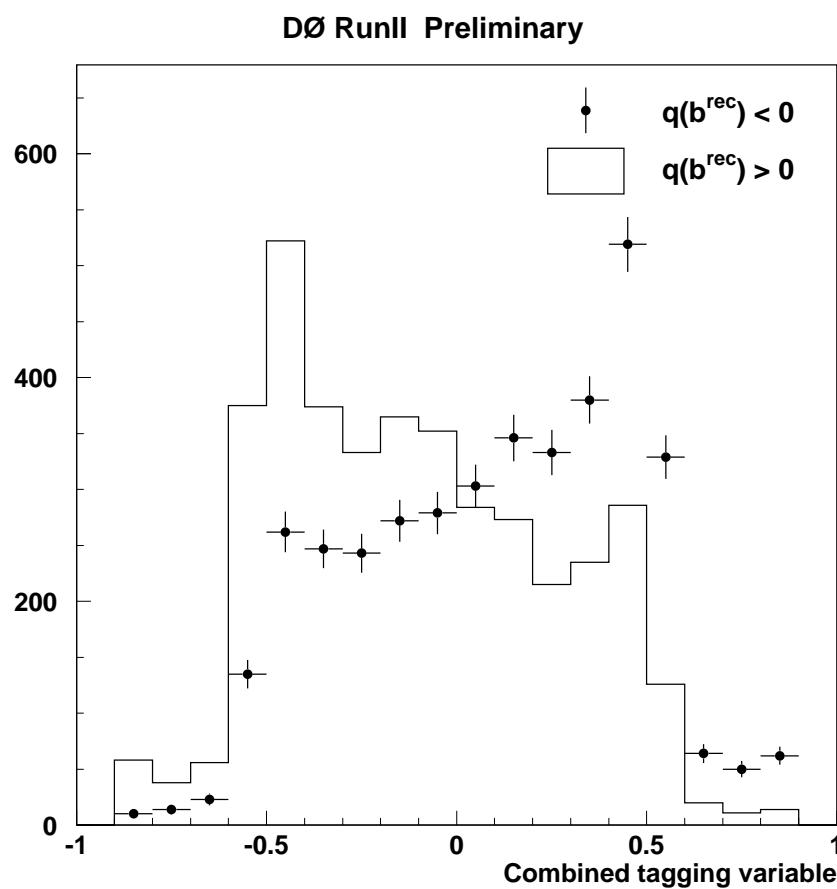
- $B_{s/d}$  is likely to be accompanied close by a  $K^+/\pi^+$  (particle ID is mandatory)



# Opposite Side Taggers at DØ

Combined Tagger:

- + Soft Muon
- + Soft Electron
- + Secondary vertex



Tagger	$\varepsilon D^2 (\%)$
Muon	$1.27 \pm 0.13$
Electron	$0.28 \pm 0.06$
Sec. Vert.	$0.54 \pm 0.08$
Combined ( $ d  > 0.3$ )	$1.94 \pm 0.14$

Tagging performance measured  
in  $\mu D^{0/*}$  candidates

# Opposite Side Taggers at CDF

---

tagger	$\varepsilon D^2$ hadronic (%)	$\varepsilon D^2$ semileptonic (%)
muon	$0.56 \pm 0.09 \pm 0.03$	$0.55 \pm 0.05 \pm 0.02$
electron	$0.26 \pm 0.05 \pm 0.02$	$0.31 \pm 0.03 \pm 0.01$
JQ/vertex	$0.23 \pm 0.07 \pm 0.01$	$0.25 \pm 0.03 \pm 0.01$
JQ/displaced	$0.35 \pm 0.08 \pm 0.02$	$0.37 \pm 0.05 \pm 0.02$
JQ/high- $p_T$	$0.15 \pm 0.06 \pm 0.02$	$0.08 \pm 0.02 \pm 0.01$
combined	$1.55 \pm 0.16 \pm 0.05$	$1.55 \pm 0.08 \pm 0.03$

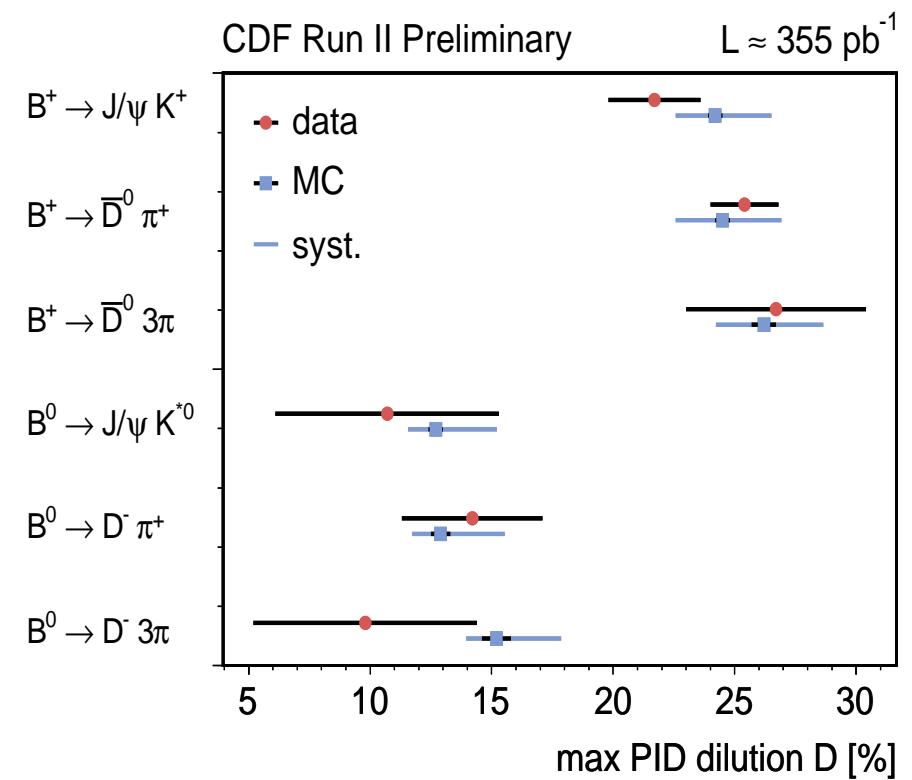
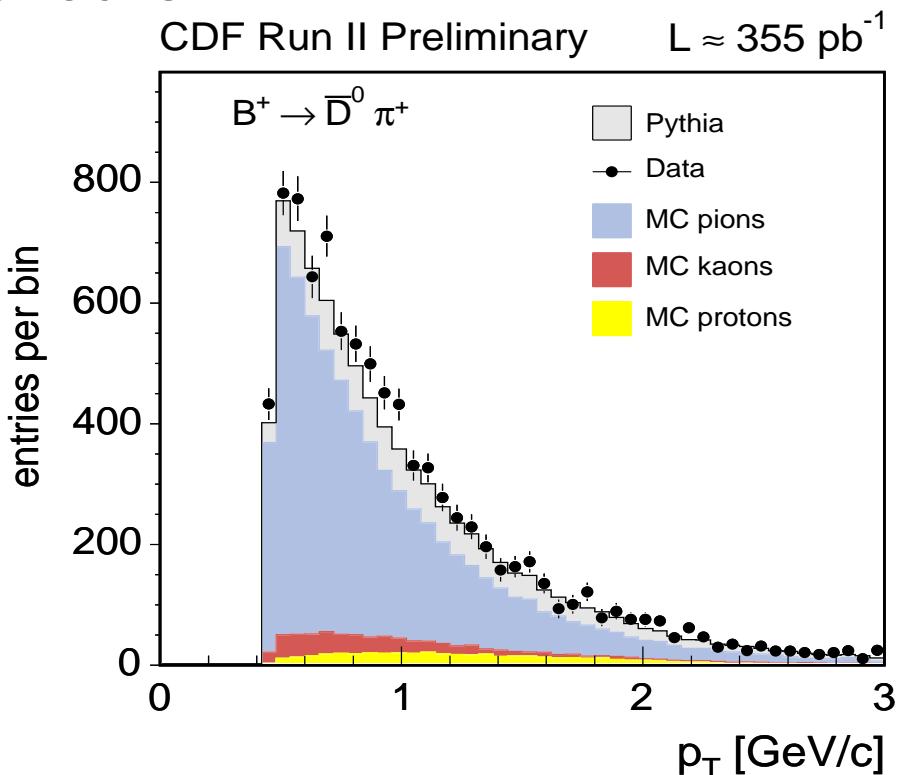
- + Taggers are mutually exclusive
- + 3 different jet types in Jet Charge (JQ) tagger
- + Performance on hadronics and semileptonics consistent within errors

# Same Side Kaon Tagger at CDF (I)

Have to rely on Monte Carlo for prediction of SS(K)T performance for  $B_s$  decays!

- + Extensive data/MC comparisons on all tagging related quantities
- + Different tagging algorithms probe different aspects of the fragmentation

Very good agreement in high statistics  $B^+$  and  $B^0$  modes in all checks!

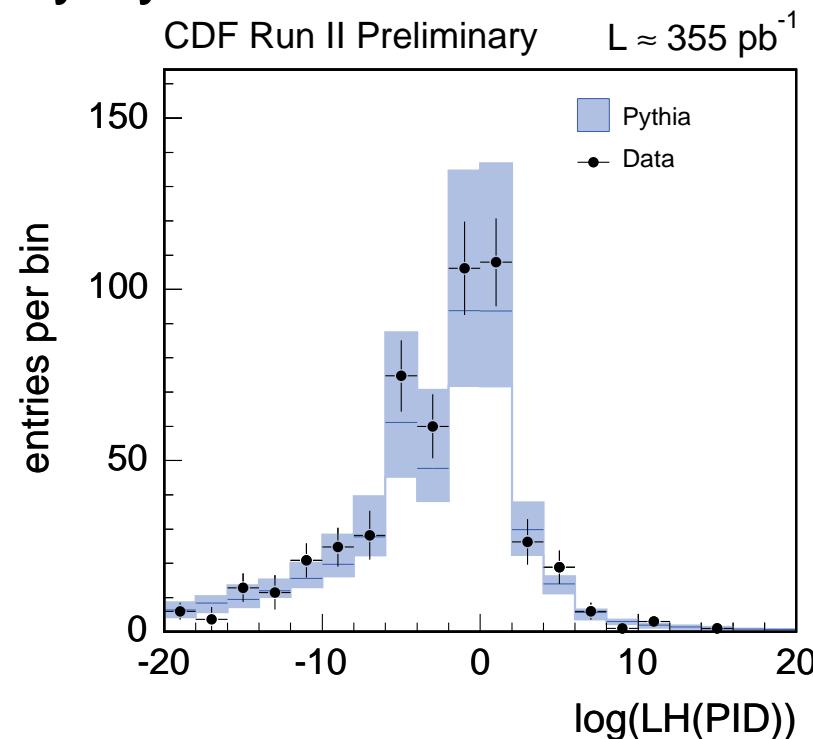


# Same Side Kaon Tagger at CDF (II)

Small discrepancies covered by systematics

Systematic studies cover:

- + Fragmentation Model
- +  $b\bar{b}$  Production Mechanisms
- +  $B^{**}$  content
- + Detector/PID resolution
- + Multiple interactions
- + PID content around  $B$
- + Data/MC agreement



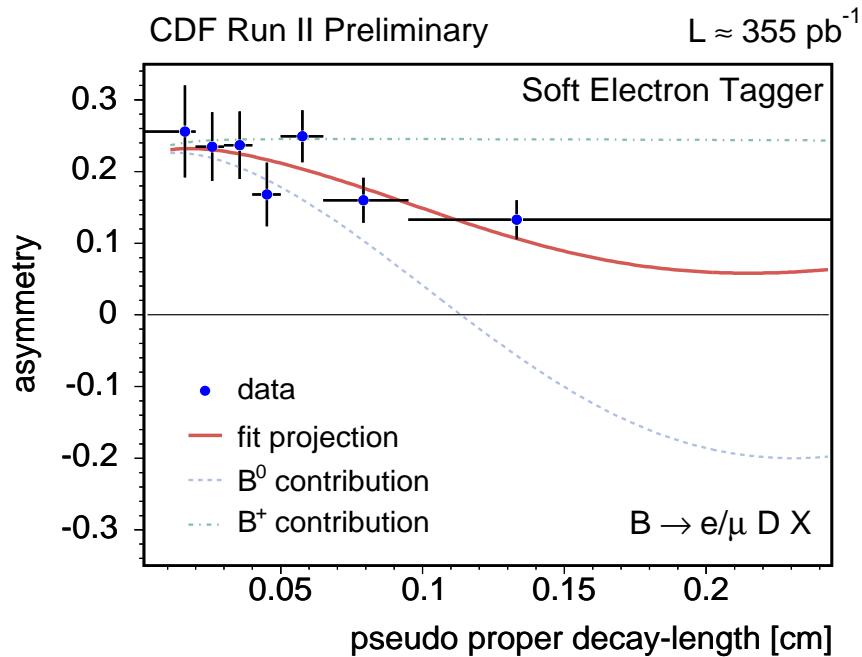
Select the most likely kaon track (PID \*) as tagging track  
Final evaluation of the tagging performance in progress

\*) TOF & dE/dx are used for particle identification

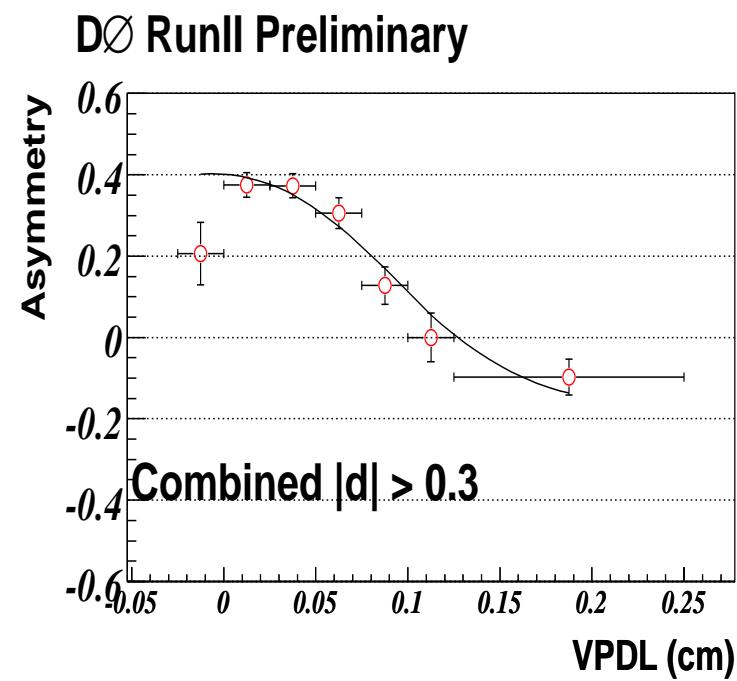
# Crucial Test of the Whole “Machinery”: $B_d$ Mixing

- + For setting limit on  $\Delta m_s$ , knowledge of tagger performance is crucial → measure tagging dilution in kinematically similar  $B^0/B^+$  samples (for OST)
- +  $\Delta m_d$  and  $\Delta m_s$  fit is very complex, > 1000 parameters
  - + combining several  $B$  flavor and several decay modes
  - + combining several taggers
  - + mass and lifetime templates for various backgrounds

$\Delta m_d$  measurement is very important to test the fitter



CDF: Soft Electron Tagger



DØ: Combined Tagger

# $\Delta m_d$ Measurement

---

Combined taggers (semileptonic channels) DØ:

$$\Delta m_d = 0.498 \pm 0.026(\text{syst}) \pm 0.016(\text{stat}) \text{ps}^{-1}$$

Combined opposite side taggers (semileptonic channels) CDF:

$$\Delta m_d = 0.511 \pm 0.020(\text{syst}) \pm 0.014(\text{stat}) \text{ps}^{-1}$$

Combined opposite side taggers (hadronic channels) CDF:

$$\Delta m_d = 0.536 \pm 0.028(\text{syst}) \pm 0.006(\text{stat}) \text{ps}^{-1}$$

Results consistent with world average ( $\Delta m_d = 0.508 \pm 0.004$ )

The whole framework ready to fit for  $B_s$  Oscillations...

# Fourier analysis

Two domains to fit for oscillation:

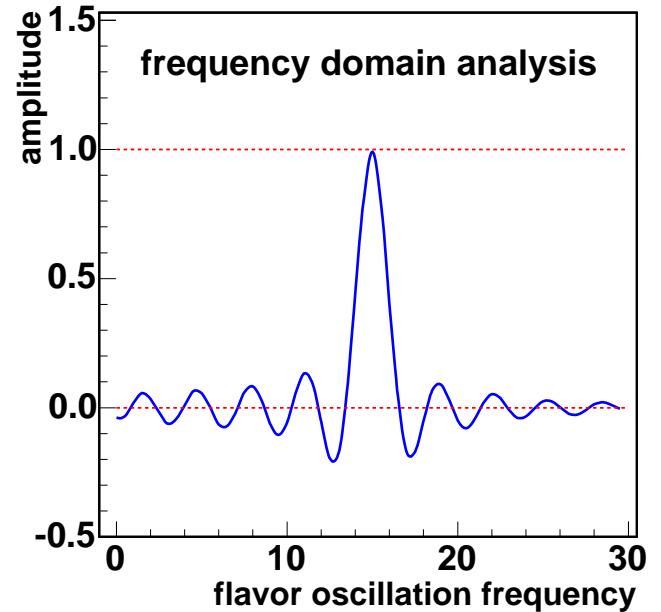
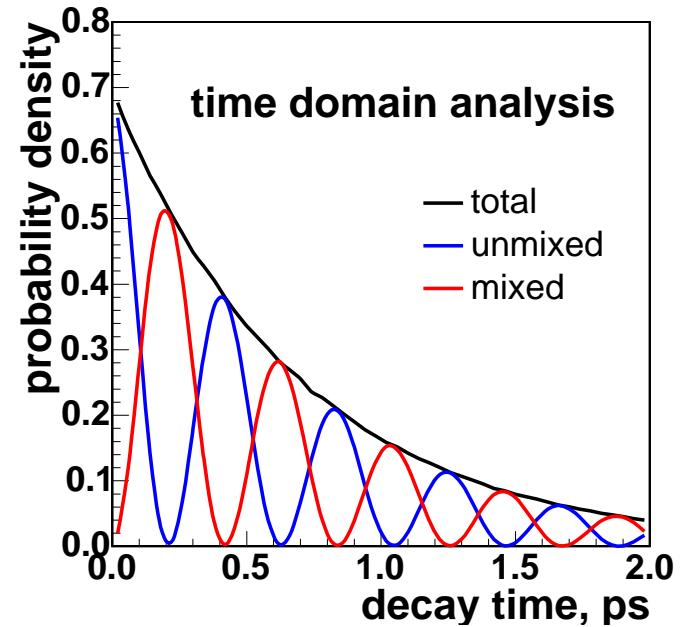
- + time: fit for a cos-wave
- + frequency: examine  $f$ -spectrum

Time domain approach:

- + good old method
- + fit for  $\Delta m_s$  in  $P(t) \sim (1 \pm D \cos \Delta m_s t)$

Frequency domain approach:

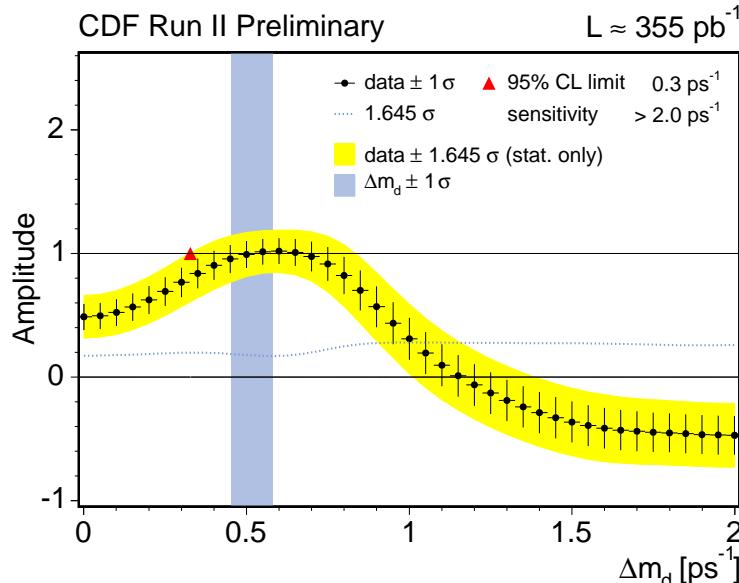
- + introduce amplitude:  
 $P(t) \sim (1 \pm \mathcal{A} D \cos \Delta m_s t)$
- + fit for  $\mathcal{A}$  at different  $\Delta m_s$   
⇒ obtain frequency spectrum
- + method is called **amplitude scan**
- + traditionally used for  $B_s$  mixing search  
⇒ easy to combine experiments
- + true  $\Delta m_s \Rightarrow \mathcal{A} = 1$ , else  $\mathcal{A} = 0$



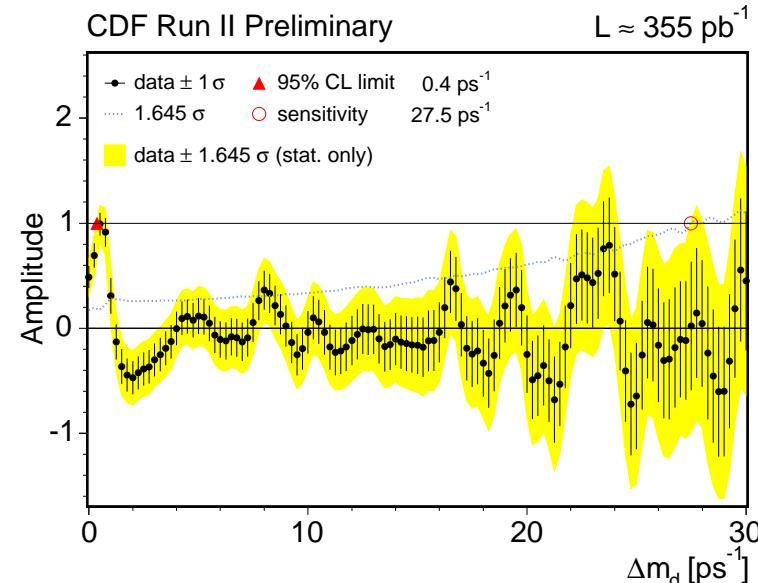
# Amplitude scan notations

Example of  $B^0$  mixing:

- + amplitude error bars: come from unbinned likelihood fit
- + yellow:  $1.645\sigma$  around data points defines 95% CL region
- +  $\Delta m$  values where  $\mathcal{A} + 1.645\sigma < 1$  are excluded at 95% CL
- + dashed line:  $1.645\sigma$  as a function of  $\Delta m$
- + sensitivity: the  $\Delta m$  where  $1.645\sigma = 1$
- + on average, we expect to observe mixing within sensitivity

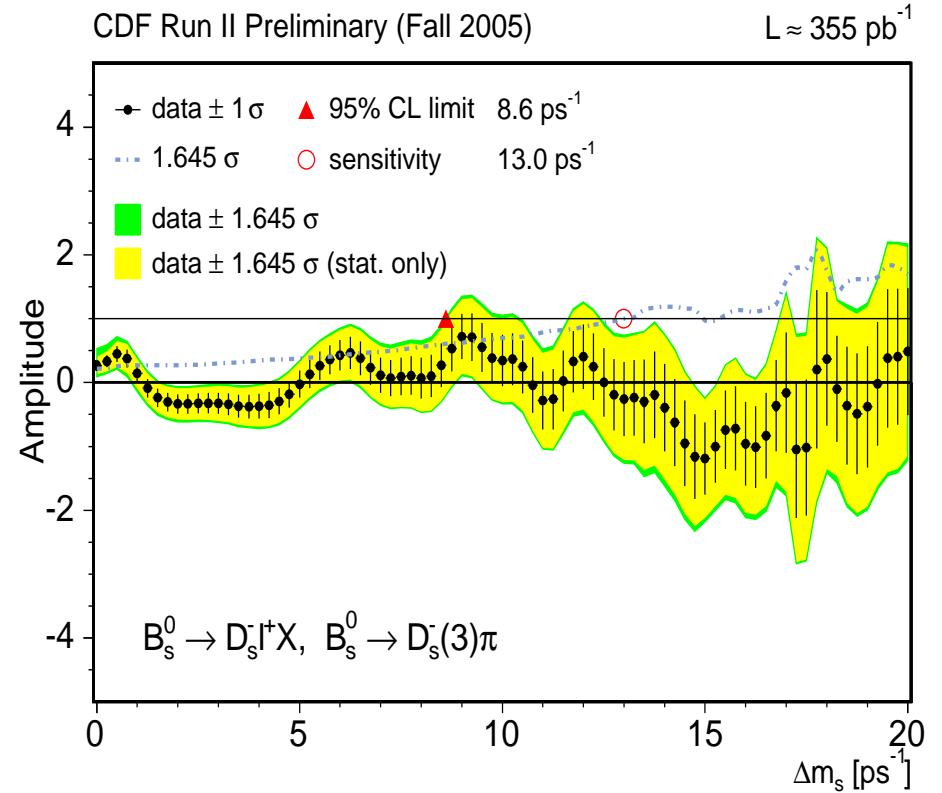
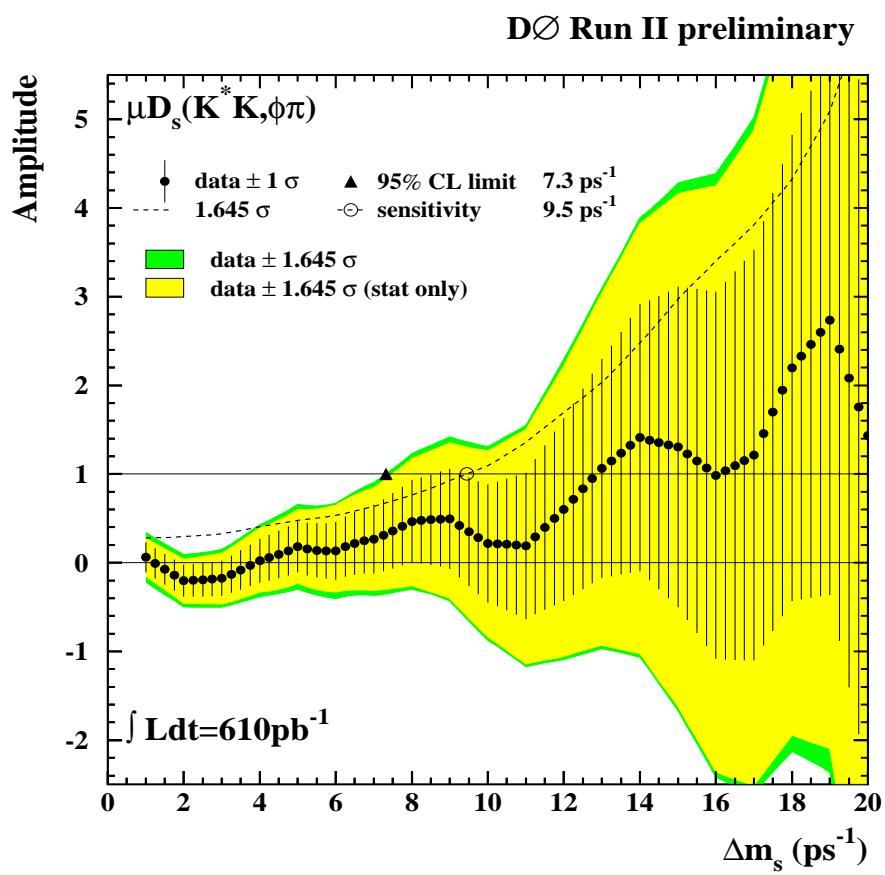


narrow range  $\mathcal{A}$  scan



same analysis, wider  $\mathcal{A}$  range

# $B_s$ Mixing Limits in Run II



DØ:

Observed Limit at 95% C.L.:  $7.3 \text{ ps}^{-1}$   
(Sensitivity:  $9.5 \text{ ps}^{-1}$ )

CDF:

Observed Limit at 95% C.L.:  $8.6 \text{ ps}^{-1}$   
(Sensitivity:  $13.0 \text{ ps}^{-1}$ )

World Average:

Observed Limit at 95% C.L.:  $16.6 \text{ ps}^{-1}$  (Sensitivity:  $20.0 \text{ ps}^{-1}$ )

# Coming Improvements

---

DØ:

- Addition of other taggers
- Use of other semileptonic decay modes
- Use of hadronic decay modes
- Unbinned fitting procedure (!!)

CDF:

- Improved selection in hadronic modes using Neural Networks
- Use partially reconstructed hadronic modes
- Use semileptonic events from other triggers
- Improve vertex resolution
- Use Same-Side Kaon tagger (!!!)

Use all the data in our hands!!!

# Summary

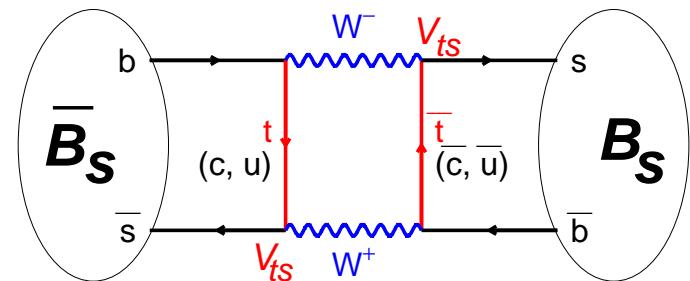
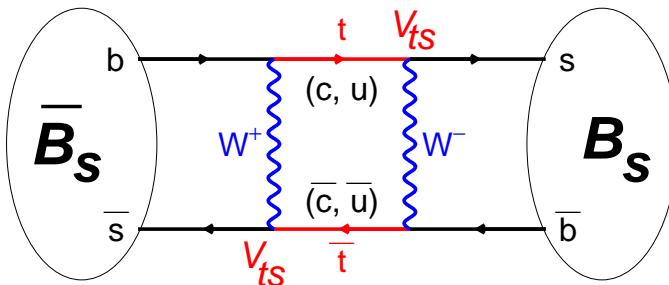
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- Tevatron experiments are in unique position to exploit  $B_s$  system
- $\Delta m_d$  results are quite robust and consistent with world average
- $\Delta m_s$  results:
  - + limit at 7.3 (8.6)  $\text{ps}^{-1}$  at DØ(CDF)
  - + sensitivity at 9.5 (13.0)  $\text{ps}^{-1}$  at DØ(CDF)
- Effect on the World 2004 results:
  - + limit  $14.6 \rightarrow 16.6 \text{ ps}^{-1}$
  - + sensitivity  $18.2 \rightarrow 20.0 \text{ ps}^{-1}$
- Significant potential for improvements!!!

---

# Back Up Slides

# Neutral $B$ Meson Mixing



Two-state mixing system

- + “heavy” and “light” weak eigenstates
- +  $B$  and  $\bar{B}$  mass eigenstates

$$|B_s\rangle = \frac{1}{\sqrt{2}}(|B_{s,H}\rangle + |B_{s,L}\rangle)$$

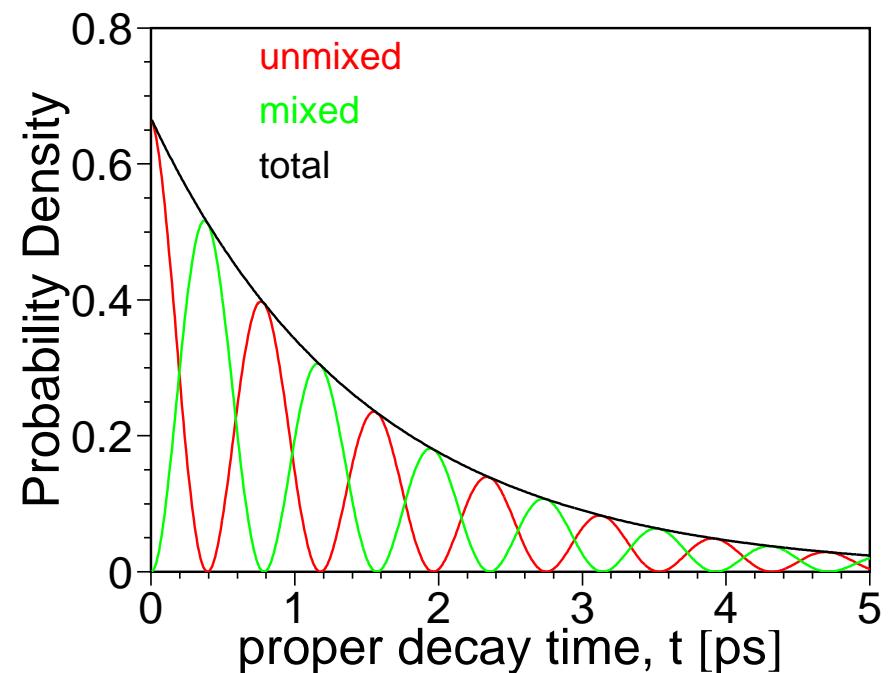
$$|\bar{B}_s\rangle = \frac{1}{\sqrt{2}}(|B_{s,H}\rangle - |B_{s,L}\rangle)$$

Solution in proper time

$$P(t)_{B^0 \rightarrow B^0} = \frac{1}{2\tau} e^{-t/\tau} (1 + \cos \Delta m t)$$

$$P(t)_{B^0 \rightarrow \bar{B}^0} = \frac{1}{2\tau} e^{-t/\tau} (1 - \cos \Delta m t)$$

- + mixing par.  $\Delta m = m_H - m_L$



# CKM Matrix

What is the origin of flavor symmetry breaking?  
 → quark mixing, CKM matrix

quark mass eigenstates

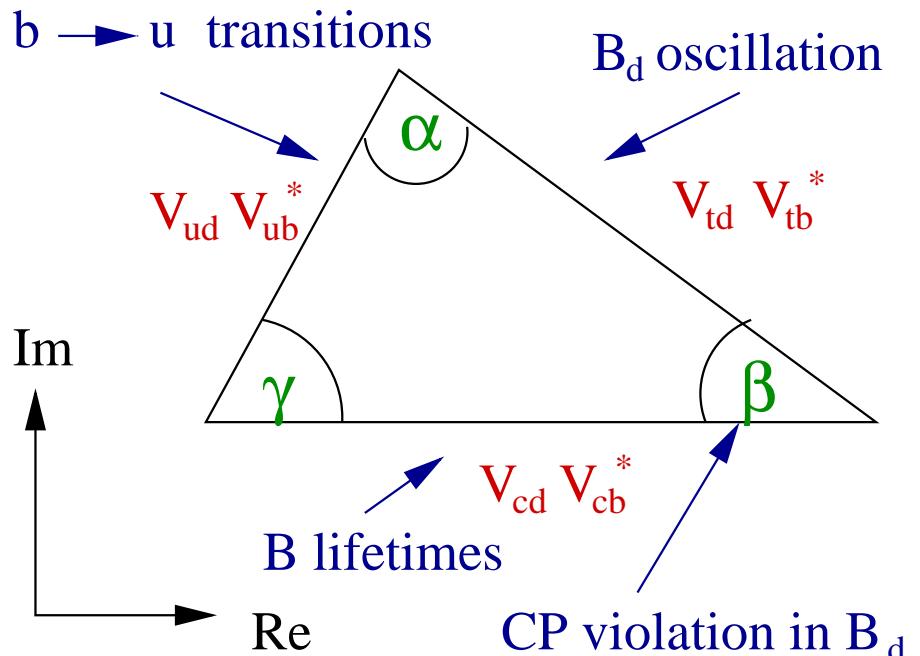
≠ weak interaction eigenstates

$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \begin{pmatrix} d \\ s \\ b \end{pmatrix}$$

$$V * V^\dagger = 1$$

CKM elements not predicted by SM  
 B decays measure **5 CKM** elements

Goal: Measure sides/angles of CKM triangle sides in all possible ways



# $\Delta m_s$ : World Average

