

# *B* mixing and lifetimes at the Tevatron

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# Outline

## ■ Precision $B$ Lifetimes

- ▶ motivation
- ▶  $L_b$
- ▶  $B_c$
- ▶  $B_s$
- ▶  $B_s \rightarrow KK$
- ▶  $B_s$  lifetime difference

## ■ $B$ Mixing

- ▶ current status
- ▶ ingredients
- ▶ yields and lifetime
- ▶ flavor taggers
- ▶ amplitude scans

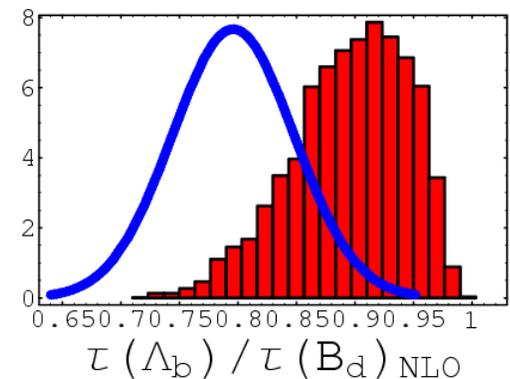
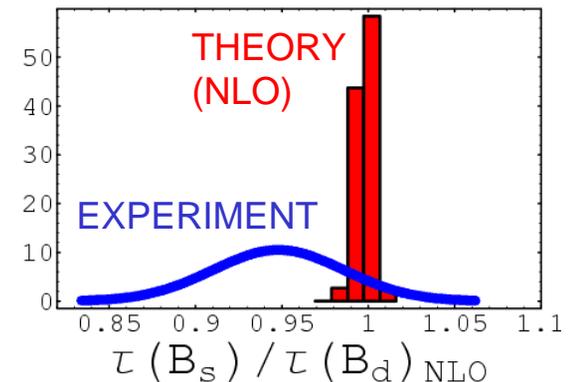
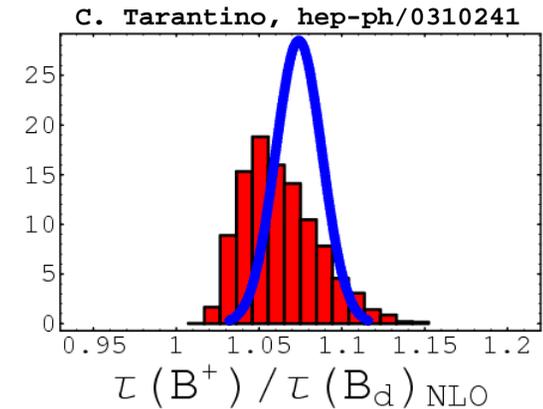
## ■ Summary

# Precision $B$ Lifetimes



# Precision $B$ Lifetimes Motivation

- $b$ -hadron decays dominated by  $b$ -quark
- Light quarks are included with  $1/m_b$  perturbative expansions (HQE)
  - ▶ expect small differences between lifetimes of different species
  - ▶ lifetime ratios reduce theory uncertainties



# Precision $B$ Lifetimes $\Lambda_b$ Lifetime

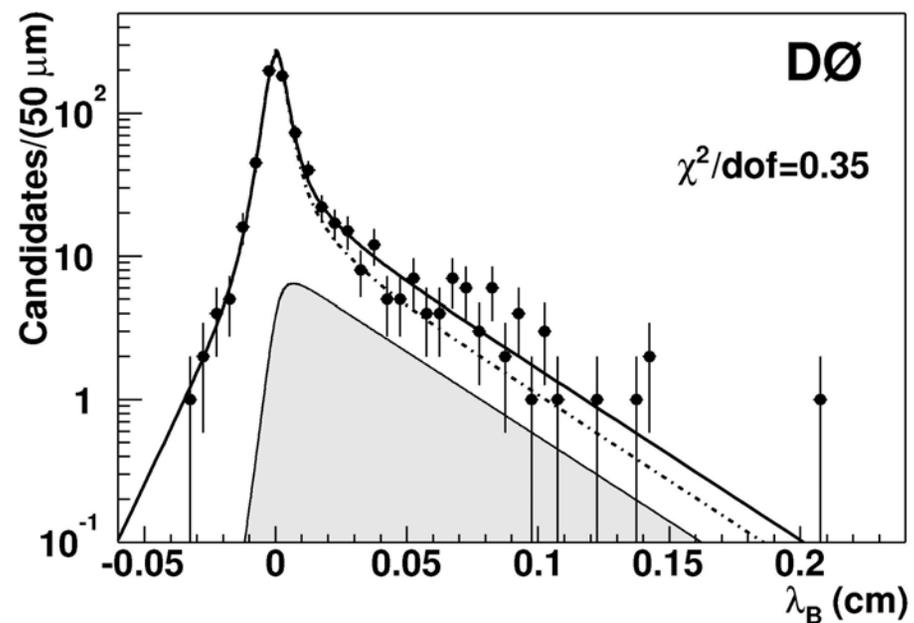
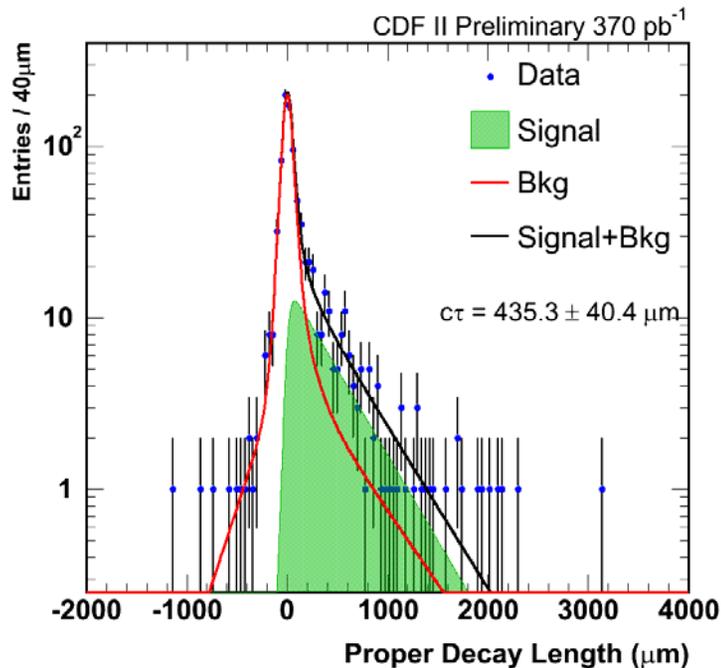
- CDF and DØ have measured  $\Lambda_b \rightarrow J/\psi \Lambda$  lifetime
- Better proper time resolution than  $\Lambda_b \rightarrow \Lambda_c l \nu$  (world average)
- New result by CDF agrees better with theory

CDF  $370 \text{ pb}^{-1}$

DØ  $250 \text{ pb}^{-1}$

$$\tau_{\Lambda_b} = 1.45^{+0.14}_{-0.13} (\text{stat}) \pm 0.02 (\text{syst}) \text{ ps} \quad \tau_{\Lambda_b} = 1.22^{+0.22}_{-0.18} (\text{stat}) \pm 0.04 (\text{syst}) \text{ ps}$$

PRL 94 102001 (2005)



# Precision B Lifetimes $B_c$ Lifetime

- Expected  $\tau(B_u^+) \sim 3 \times \tau(B_c^+)$  assuming 3 decay subprocesses
  - $b(c)$  quark decays,  $c(b)$  quark is spectator
  - $bc$  annihilation decays
- Lifetime extracted from  $B_c^+ \rightarrow J/\psi e^+ \nu_e$  decay
  - electron ID using energy loss and calorimeter shower information

CDF  $360 \text{ pb}^{-1}$

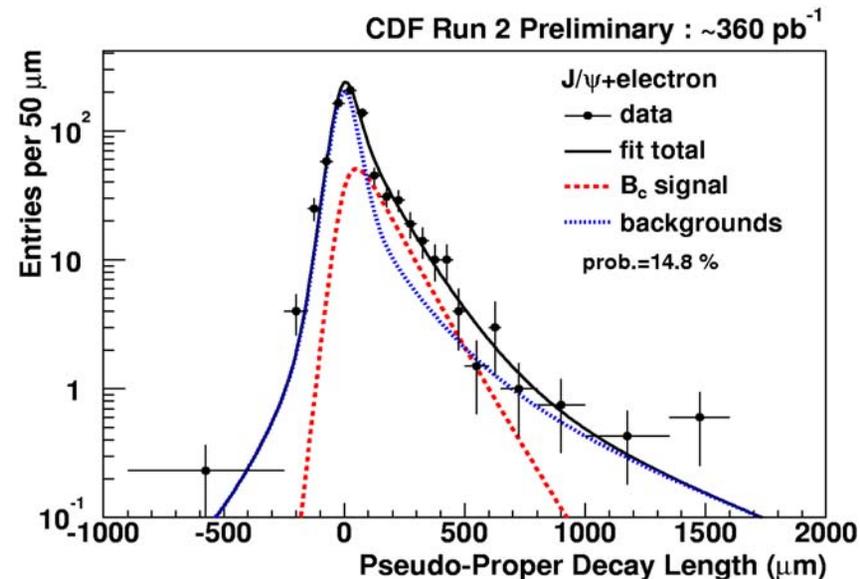
$$\tau_{B_c^+} = 0.463_{-0.065}^{+0.073} (\text{stat}) \pm 0.036 (\text{syst}) \text{ ps}$$

best in the world

theory prediction

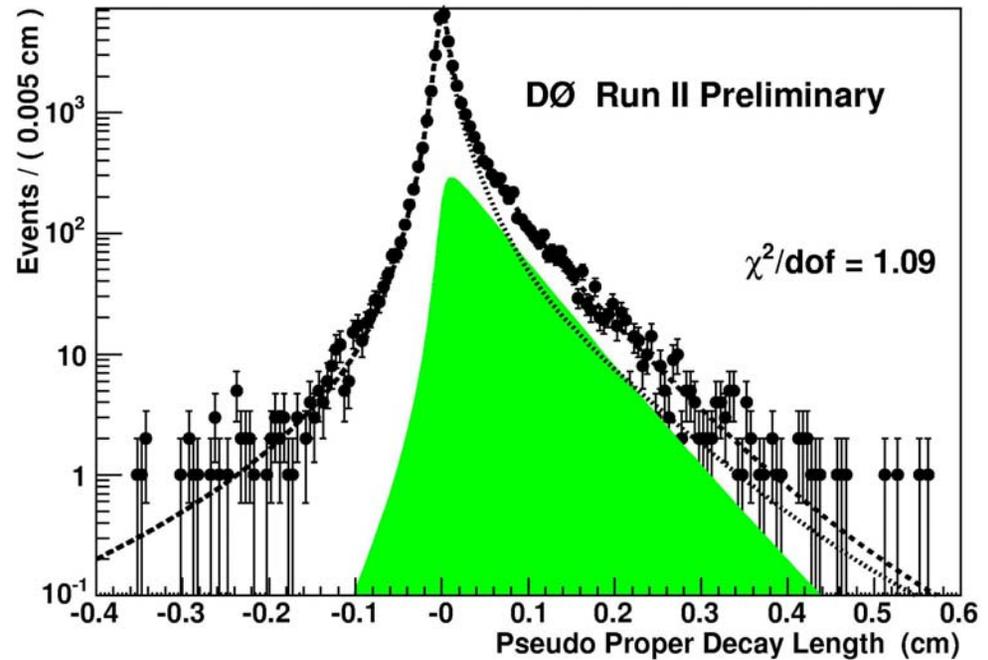
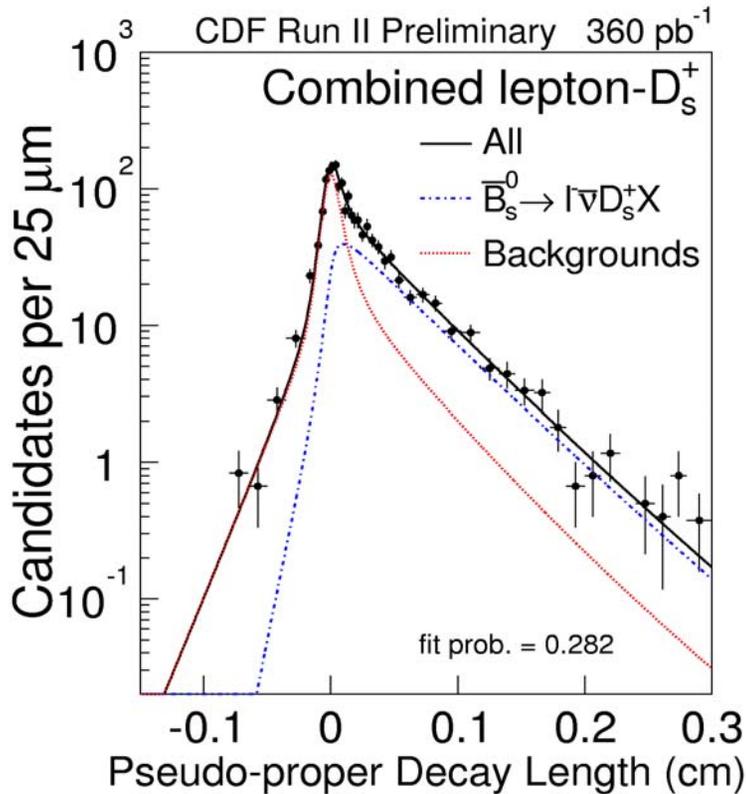
$$\tau_{B_c^+} = 0.55 \pm 0.15 \text{ ps}$$

V. Kiselev, hep-ph/0308214



# Precision $B$ Lifetimes $B_s$ Lifetime

■ DØ and CDF measure  $B_s^0$  lifetime in  $B_s^0 \rightarrow D_s^- l^+ \nu X$



CDF 360 pb<sup>-1</sup>

DØ 400 pb<sup>-1</sup>

$$\tau_{B_s^0} = 1.381 \pm 0.055 \text{ (stat)}_{-0.046}^{+0.052} \text{ (syst)} \text{ ps}$$

$$\tau_{B_s^0} = 1.420 \pm 0.043 \text{ (stat)} \pm 0.057 \text{ (syst)} \text{ ps}$$

best in the world

# Precision $B$ Lifetimes $B_s \rightarrow K^+ K^-$ Lifetime

■ First  $\tau_{B_s \rightarrow K^+ K^-} (\approx \tau_L)$  measurement

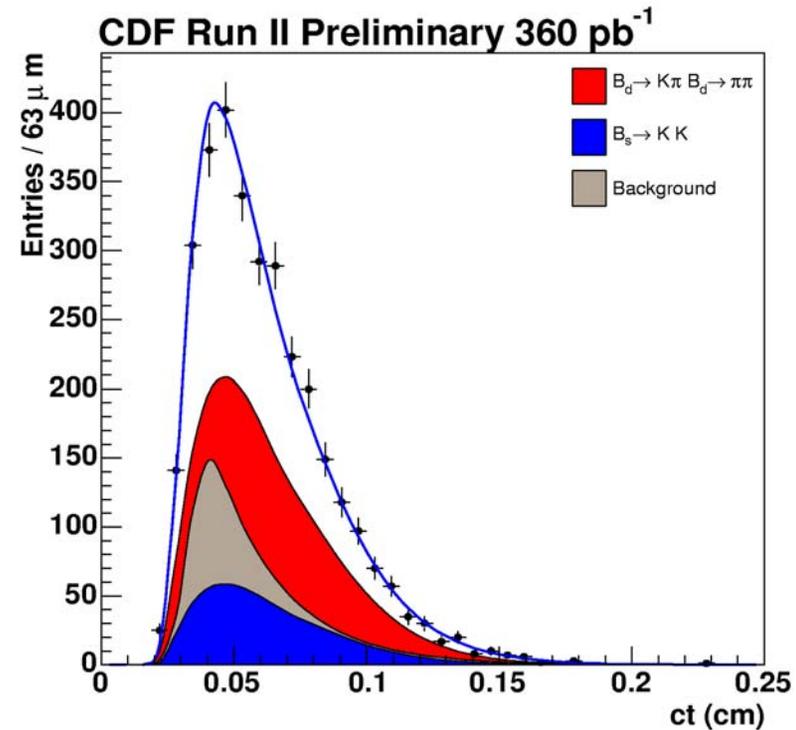
■  $B \rightarrow h_1^+ h_2^-$  is a mixture of

$$B_d^0 \rightarrow \pi^+ \pi^- \quad B_d^0 \rightarrow K^+ \pi^-$$

$$B_s^0 \rightarrow K^+ K^- \quad B_s^0 \rightarrow \pi^+ K^-$$

■ Separate decays statistically

- ▶ kinematics
- ▶ particle ID ( $dE/dx$ )



CDF 360 pb<sup>-1</sup>

HFAG *flavor specific*

$$\tau_L = 1.53 \pm 0.18 (stat) \pm 0.02 (syst) \text{ ps}$$

$$\tau_{B_s} = 1.454 \pm 0.040 \text{ ps}$$

$$\frac{\Delta\Gamma_{CP}(B_s \rightarrow K^+ K^-)}{\Gamma_{CP}(B_s \rightarrow K^+ K^-)} = -0.08 \pm 0.23 (stat) \pm 0.03 (syst)$$

# Precision B Lifetimes $B_s$ Lifetime Difference

■  $B_s \rightarrow J/\psi \phi$

Pseudoscalar  $\rightarrow$  Vector - Vector

■ Decay amplitude decomposed into 3 linear polarization states

▶  $A_0 = S + D \text{ wave} \Rightarrow P \text{ even}$

▶  $A_{||} = S + D \text{ wave} \Rightarrow P \text{ even}$

▶  $A_{\perp} = P \text{ wave} \Rightarrow P \text{ odd}$

■ If CP violation neglected

▶  $B_{s,\text{Light}} \approx CP \text{ even}$

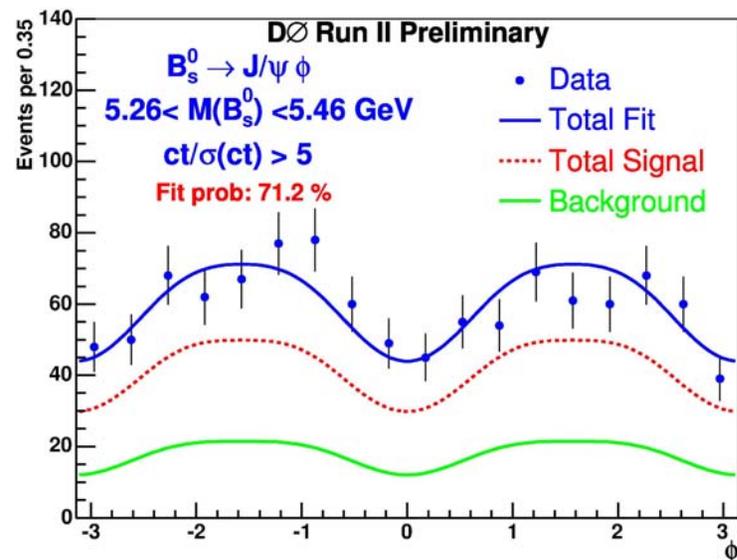
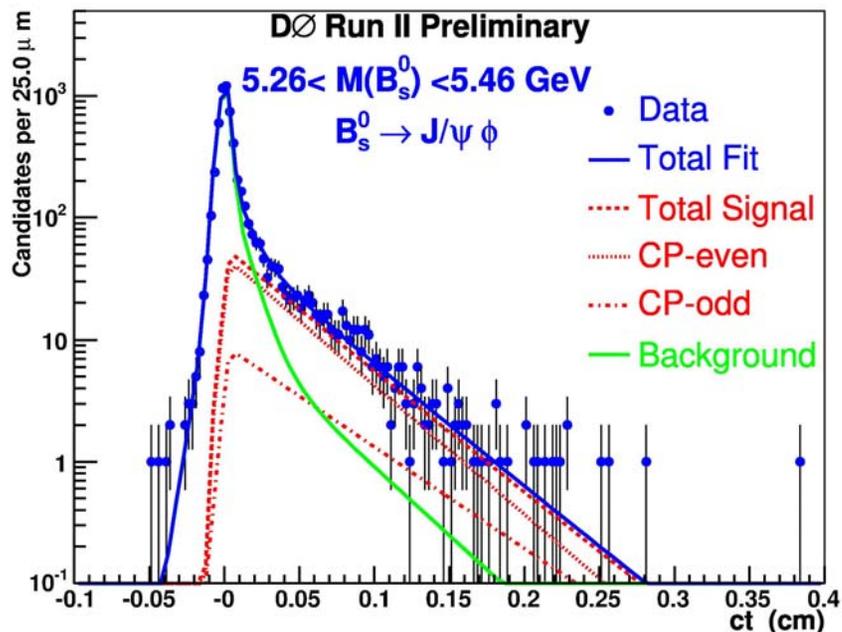
▶  $B_{s,\text{Heavy}} \approx CP \text{ odd}$

▶ angular distributions are different

■ Angular analysis separates CP eigenstates  $\Rightarrow$  measure two lifetimes

# Precision $B$ Lifetimes $B_s$ Lifetime Difference

- Results consistent with SM
- Consistent with no CP violation



DØ  $0.8 \text{ fb}^{-1}$

$$\Delta\Gamma = 0.15 \pm 0.10^{+0.03}_{-0.04} \text{ ps}^{-1}$$

$$\bar{\tau}(B_s^0) = 1.53 \pm 0.08^{+0.01}_{-0.04} \text{ ps}^{-1}$$

$$R_{\perp} = |A_{\perp}(0)|^2 = 0.19 \pm 0.05 \pm 0.01$$

$$|A_{\perp}(0)|^2 - |A_{\parallel}(0)|^2 = 0.35 \pm 0.07 \pm 0.01$$

$$\delta_1 - \delta_2 = 2.5 \pm 0.4 \pm 0.02$$

# *B* Mixing



# B Mixing Theoretical Prediction

B Mixing

- SM prediction for the ratio of  $B_s$  and  $B^0$  mixing frequencies

$$\frac{\Delta m_s}{\Delta m_d} = \frac{m_{B_s}}{m_{B_d}} \xi^2 \frac{|V_{ts}|^2}{|V_{td}|^2}$$

$$\xi^2 = 1.21 \pm 0.02^{+0.035}_{-0.014}$$

- $\Delta m_d$  precisely measured

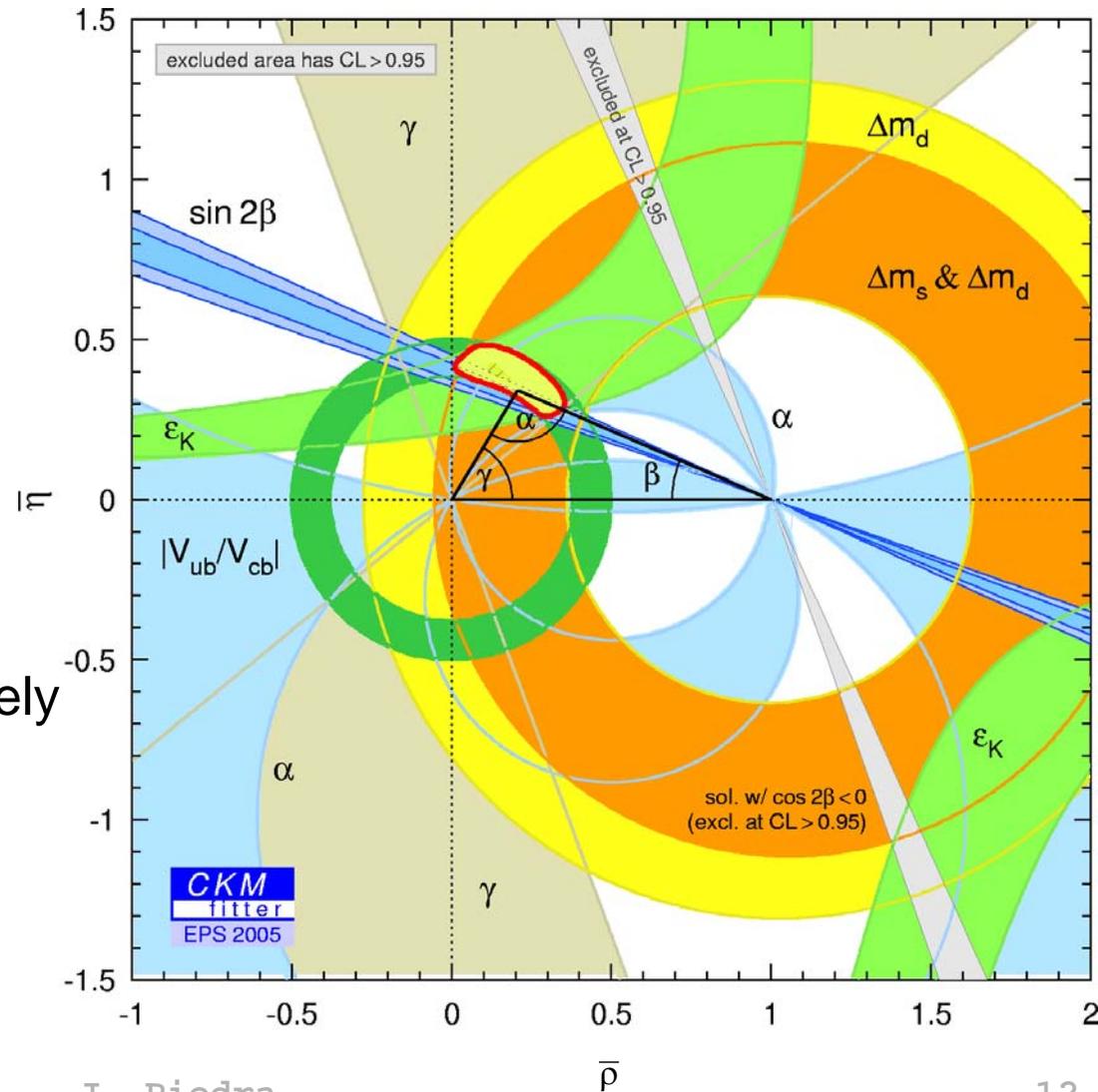
$$\Delta m_d = 0.508 \pm 0.004 \text{ ps}^{-1}$$

- $\Delta m_s$  not yet measured precisely

CKM fit

$$\Delta m_s = 18.3^{+6.5}_{-1.5} \text{ ps}^{-1}$$

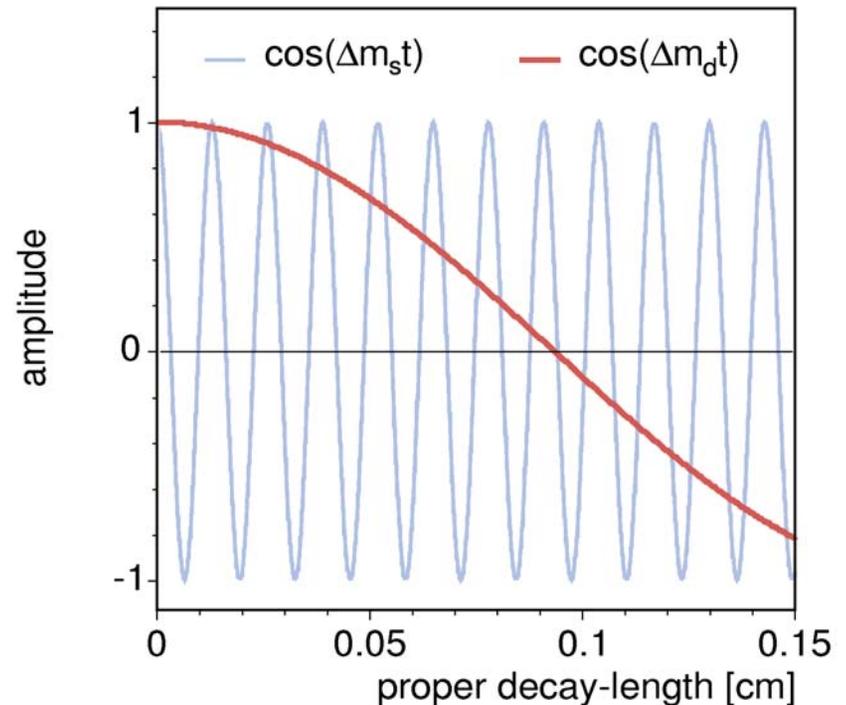
- Potential NP discovery



## $\Delta m_s$ challenge, fast oscillations

- ▶ precise vertex
- ▶ precise momentum
- ▶ tagging essential
- ▶ many signal events
- ▶ low background

$$\Delta m_d = 0.5 \text{ ps}^{-1}$$
$$\Delta m_s \equiv 14.4 \text{ ps}^{-1}$$

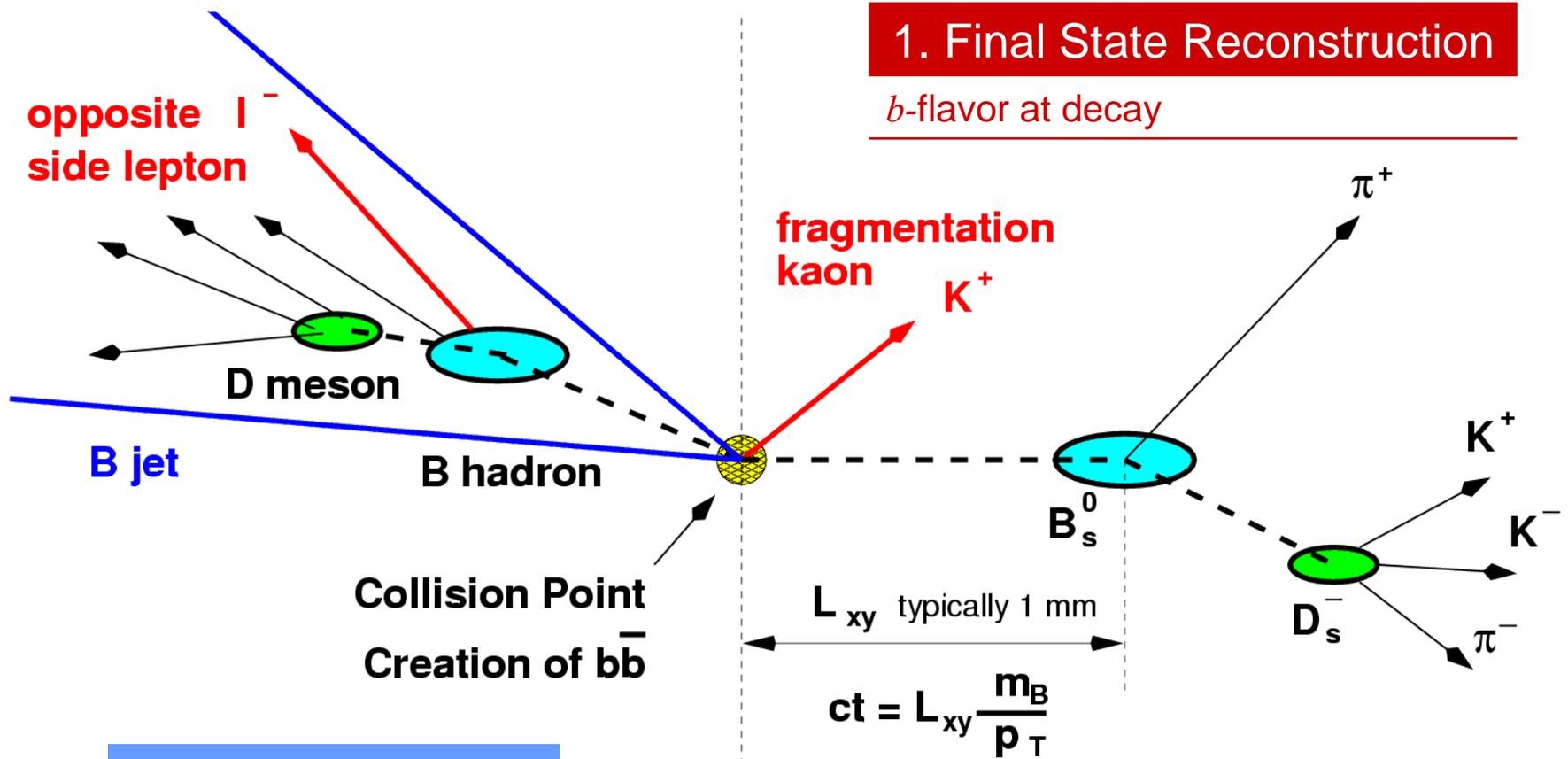


## Sensitivity to mixing

*NIM A 384 491, Moser & Roussarie*

$$\text{significance} = \sqrt{\frac{S}{S+B}} \sqrt{\frac{\epsilon \mathcal{D}^2}{2}} e^{-\frac{1}{2} \sigma_{ct}^2 \Delta m_s^2}$$

# B Mixing Ingredients



1. Final State Reconstruction

*b*-flavor at decay

3. *b*-Flavor Tagging

*b*-flavor at production

2. Proper Decay Time

In *B* rest frame

4. Amplitude Scan for  $B_s$  Mixing

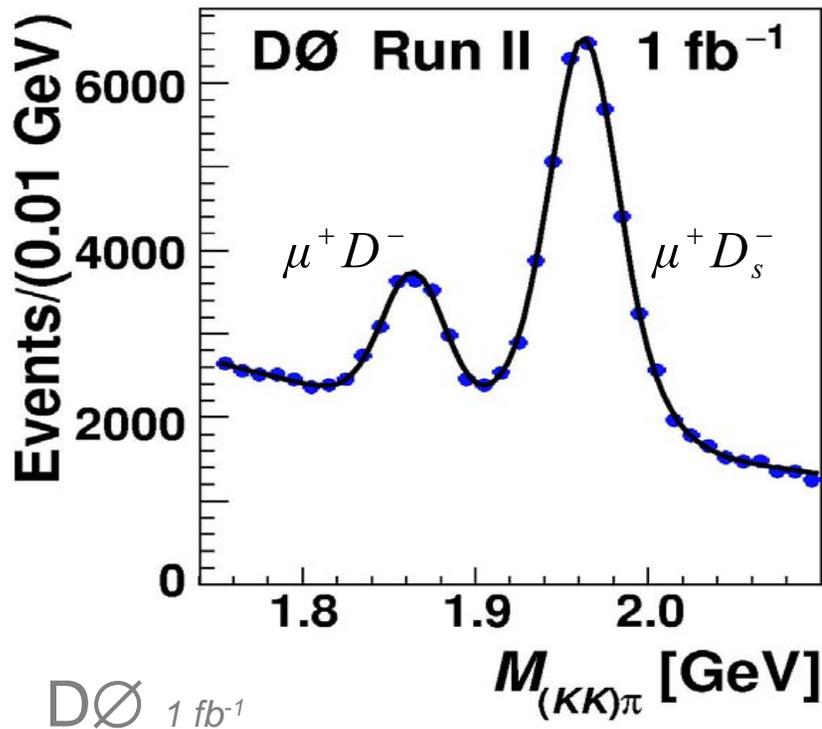
Set a lower limit on  $\Delta m_s$

Opposite Side

Trigger Side

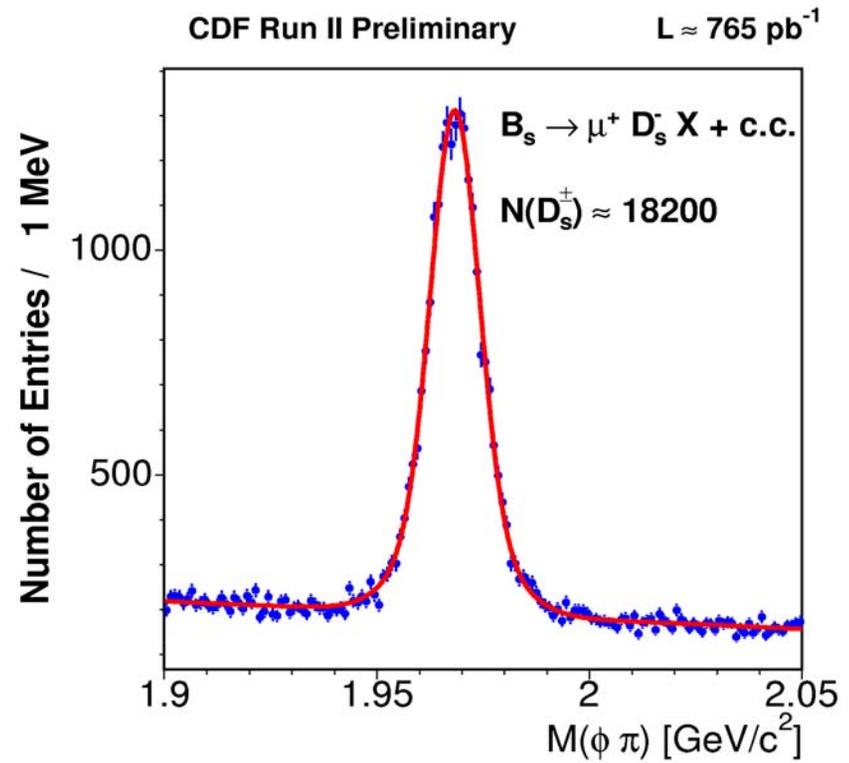
# *B* Mixing Reconstructed $B_s \rightarrow l^+ D_s^- X$

- Worse proper time resolution but high statistics
- DØ exploits semileptonic decays from  $\mu$  trigger
- CDF uses both electrons and muons



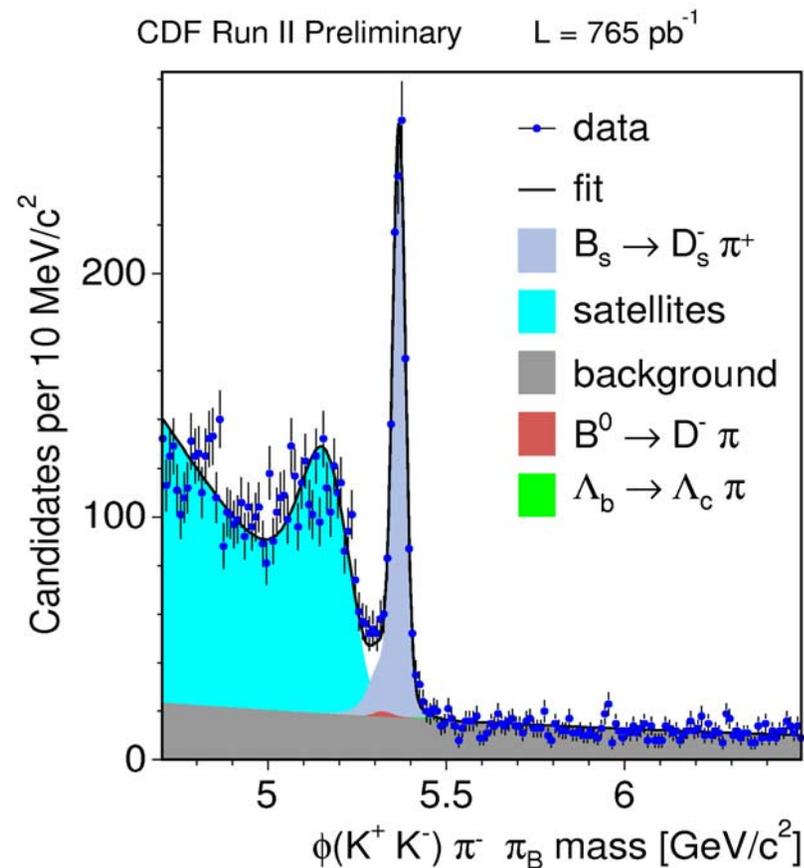
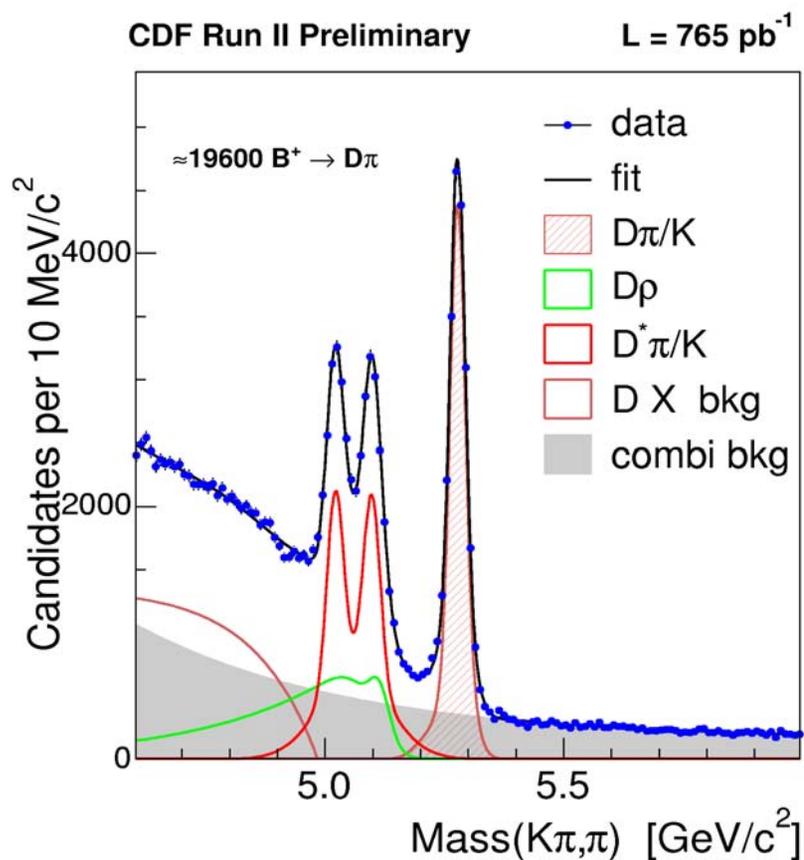
$$N_{\mu^+ D_s^-} = 26710 \pm 556 \text{ (stat)}$$

$$D_s^- \rightarrow \phi \pi^-, \phi \rightarrow K^+ K^-$$



# Reconstructed $D_s^- (\pi^+ \pi^-) \pi^+$

- CDF collects hadronic  $B$  decays by triggering on impact parameter
- More than 2300  $B_s$  signal candidates



# B Mixing Proper Decay Time

## ■ Procedure

- ▶ measure  $p_T$  of  $B$  daughter tracks
- ▶ measure the decay length  $L_{xy}$
- ▶ boost  $B$  back to its rest frame

## ■ Fully reconstructed decays

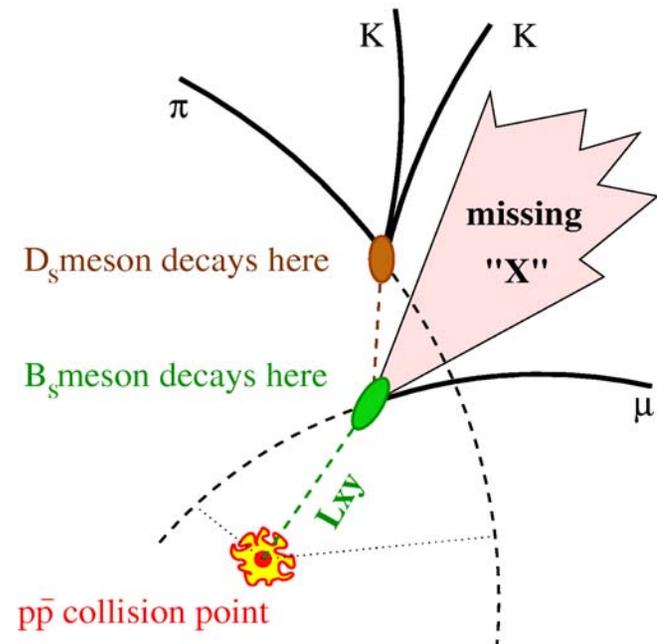
- ▶ all daughters reconstructed

## ■ Partially reconstructed decays

- ▶ some tracks escape detection
- ⇒ need simulation (next slide)

$$ct = \frac{L_{xy}}{\gamma\beta} \quad k_{MC} \equiv \left\langle \frac{p_T^{ID}}{p_T^B} \right\rangle_{MC}$$

$$\gamma\beta = \frac{p_T^B}{m_B} \approx \frac{p_T^{ID}}{m_B} \frac{1}{k_{MC}}$$



# B Mixing Semileptonic Decay Time

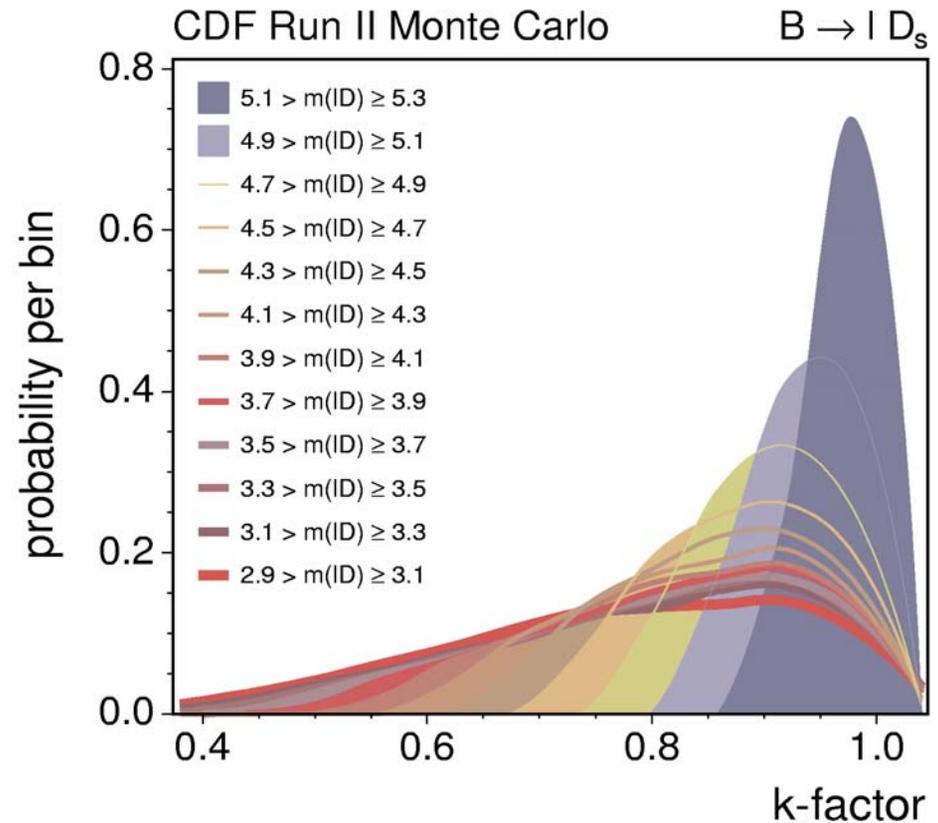
- Missing particles  $\Rightarrow$  missing  $p_T$
- Determine pseudo- $ct$  from data

$$ct^* = L_{xy} \frac{m_B}{p_T^{lD}}$$

- $ct = ct^* K$ , estimate  $K$  from MC
  - include  $K$  effect in signal PDF

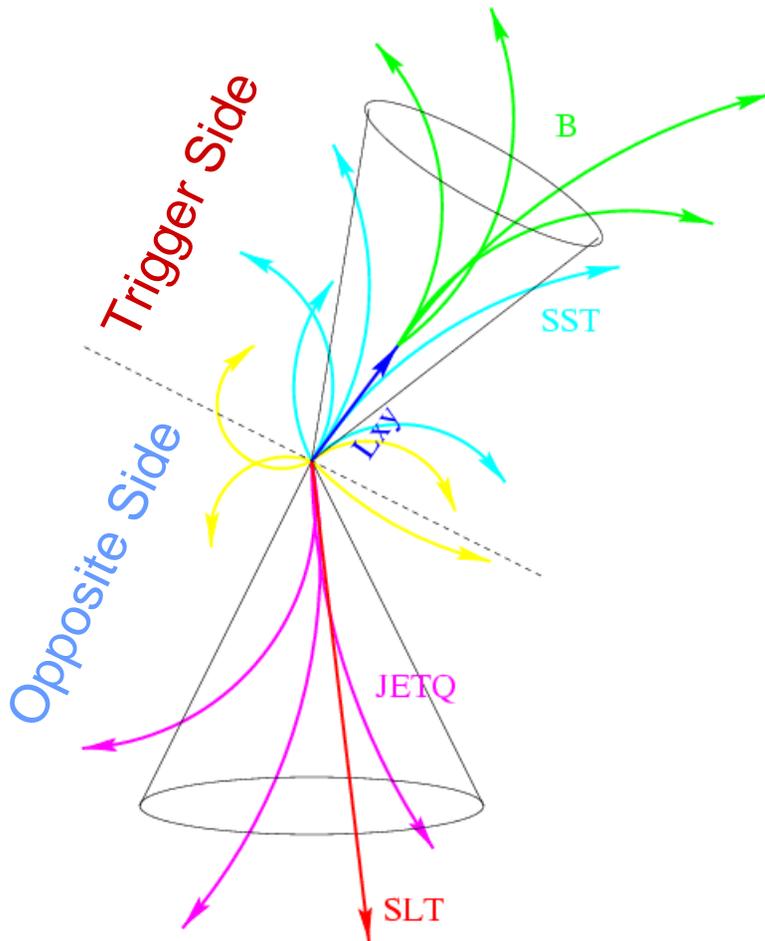
$$P(ct^*) = \frac{K}{2c\tau} e^{-\frac{ct^* K}{c\tau}} \theta(ct^*) \otimes Gauss \otimes F(K) \xi(ct^*)$$

- Use different  $F(K)$  for different  $m(lD)$  ranges



# *B* Mixing *b*-Flavor Tagging

- A flavor tagger determines the *b*-flavor at production time
- $b\bar{b}$  production  $\Rightarrow$  flavor tagging on the **Trigger Side** or the **Opposite Side**



- **Soft Lepton Tagger** **SLT**
  - ▶ look for  $B \rightarrow l\nu DX$  decay on the **OS**
  - ▶ lepton charge indicates *b*-flavor
- **Jet Charge Tagger** **JQT**
  - ▶ look for a jet from **OS** *b*-hadron
  - ▶ jet charge indicates *b*-flavor
- **Same Side (Kaon) Tagger** **SS(K)T**
  - ▶ look for a fragmentation track on the **TS**
  - ▶ it is charge correlated with the *b*-flavor

# B Mixing Opposite Side Taggers

- A flavor tagger not always can be applied  $\varepsilon \equiv \frac{\text{correct tags} + \text{incorrect tags}}{N}$
- It can give a wrong answer. The dilution  $\mathcal{D}$  measures the purity

$$\mathcal{D} \equiv \frac{\text{correct tags} - \text{incorrect tags}}{\text{correct tags} + \text{incorrect tags}}$$

- The dilution attenuates the observed oscillations

$$P(t)_{B^0 \rightarrow B^0, \bar{B}^0} \cong \frac{1}{2\tau} e^{-\frac{t}{\tau}} [1 \pm \mathcal{D} \cos(\Delta mt)]$$

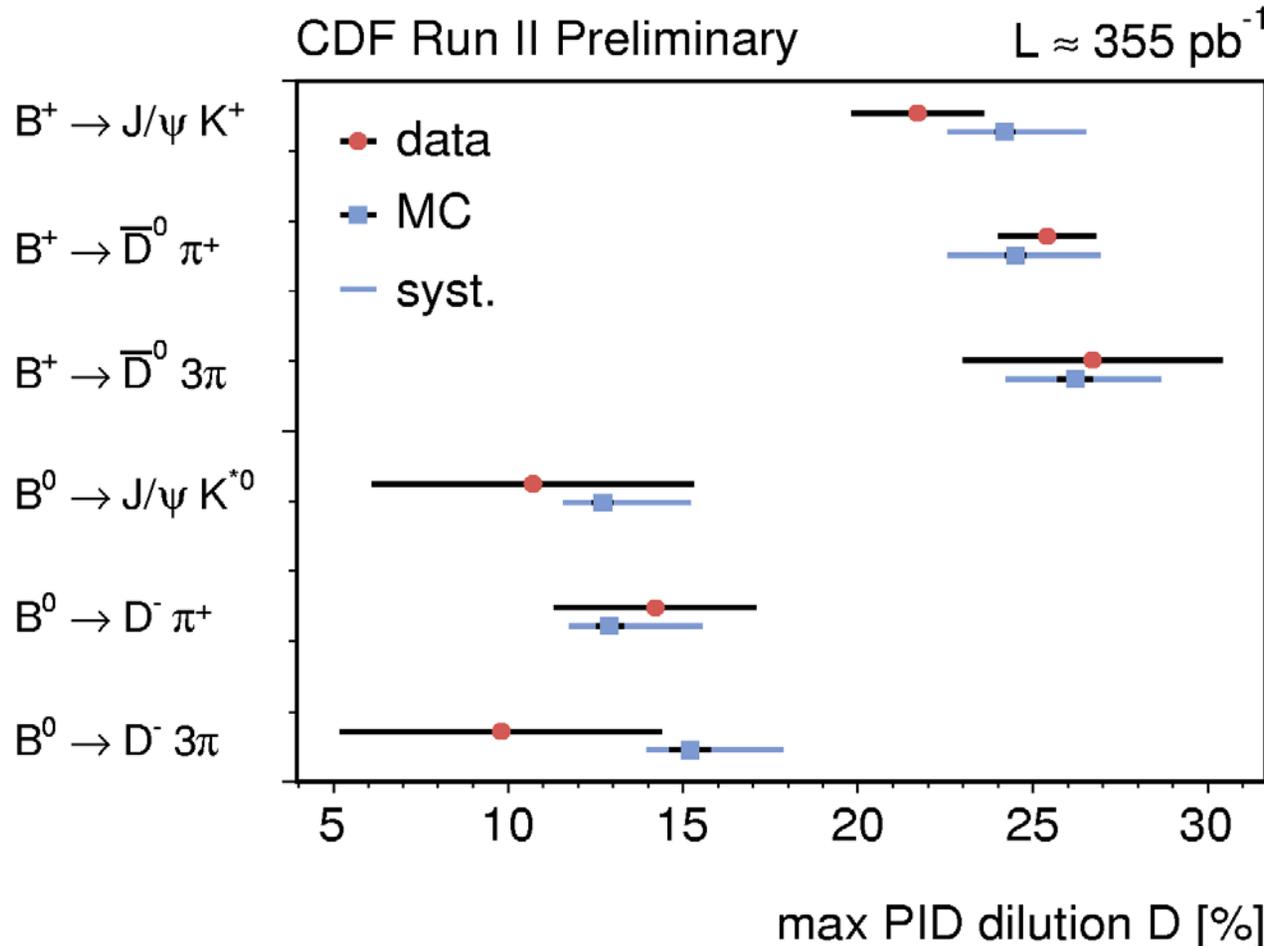
$\varepsilon \mathcal{D}^2$ (%)	$\mathcal{D} \emptyset$	CDF
muons	$1.48 \pm 0.17$	$0.55 \pm 0.05$
electrons	$0.21 \pm 0.07$	$0.30 \pm 0.03$
jets	$0.50 \pm 0.11$	$0.70 \pm 0.06$
<b>combined</b>	<b><math>2.48 \pm 0.22</math></b>	<b><math>1.55 \pm 0.08</math></b>

# B Mixing SSKT at CDF

B Mixing

# SSKT at CDF

- Must rely on MC prediction of SSKT performance for  $B_s$  decays
  - ▶ Extensive data/MC comparisons on all tagging related quantities

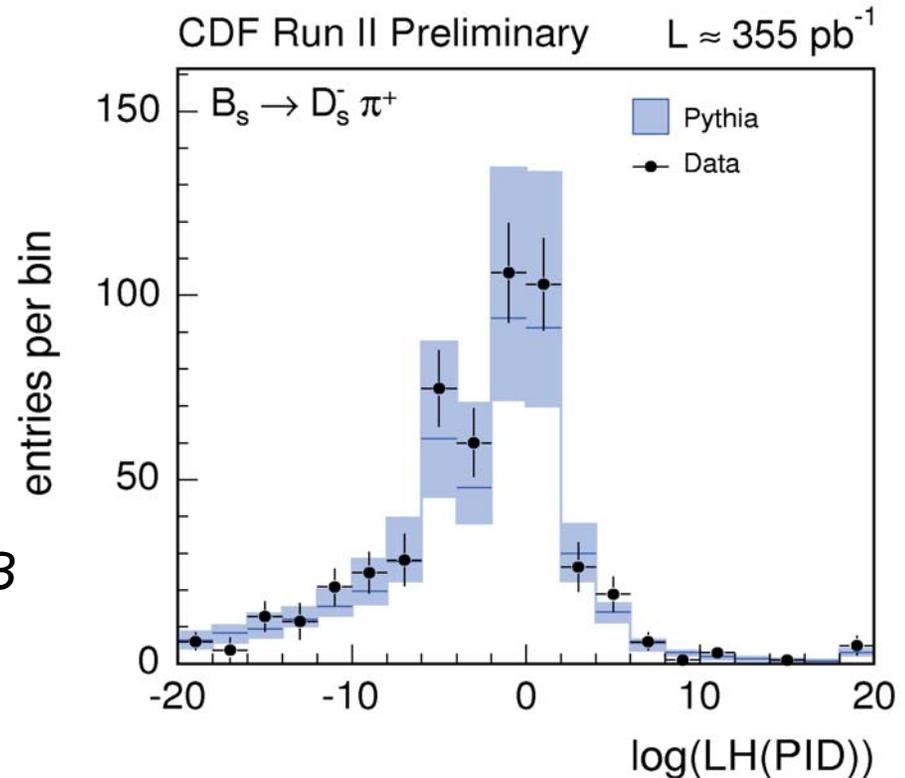


EXCELLENT AGREEMENT IN HIGH STATISTICS  $B^+$  AND  $B^0$  MODES

# *B* Mixing SSKT at CDF

## Systematic studies cover

- ▶ quark fragmentation model
- ▶  $b\bar{b}$  production mechanisms
- ▶ excited  $B$  mesons content
- ▶ detector / PID resolution
- ▶ particle species content around  $B$
- ▶ data / MC agreement



## Select using PID the most likely kaon track

- ▶  $\text{LH(PID)} \equiv \text{TOF and } dE/dx \text{ combined likelihood}$

CDF  $_{MC}$

$$\mathcal{E}\mathcal{D}_{SSKT}^2 \left( B_s^0 \rightarrow D_s^- \pi^+ \right) = 4.0_{-1.2}^{+0.8} \%$$

# *B* Mixing Flavor Analysis on $B^+$ and $B^0$

## ■ Calibrate opposite side flavor taggers prior to $\Delta m_s$ analysis

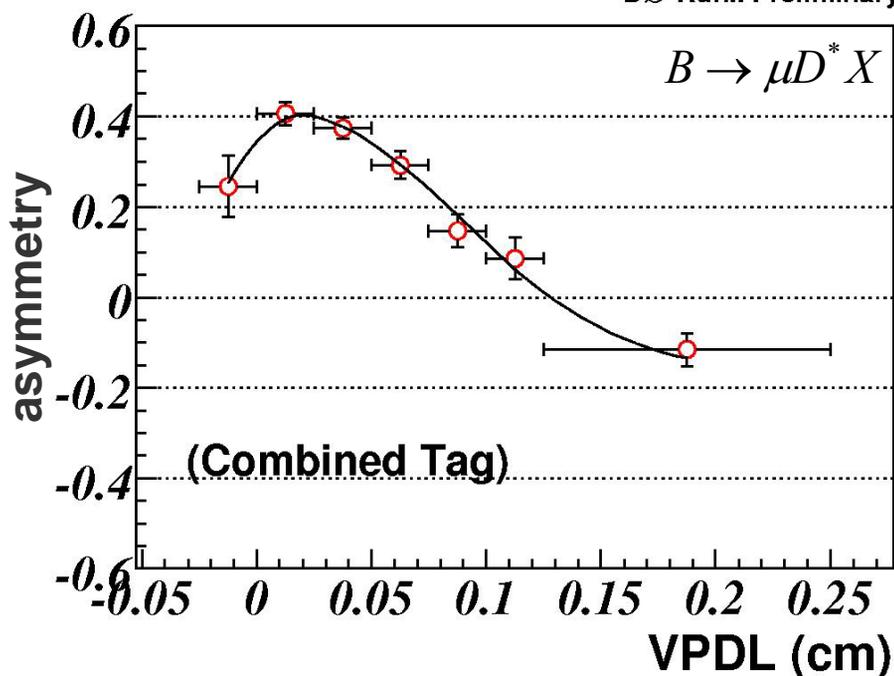
- ▶ combine several  $B^{+,0}$  decays
- ▶ combine all taggers

## ■ Direct $\Delta m_d$ measurement

- ▶ crosscheck for  $B_s$  mixing
- ▶ 'easy' slow oscillations

$$\mathcal{A} = \frac{P(ct)_{unmix} - P(ct)_{mix}}{P(ct)_{unmix} + P(ct)_{mix}} \sim \mathcal{D} \cos(\Delta m_d t)$$

DØ RunII Preliminary



DØ semileptonic	$\Delta m_d = 0.506 \pm 0.020$ (syst) $\pm 0.016$ (stat) $\text{ps}^{-1}$
CDF semileptonic	$\Delta m_d = 0.511 \pm 0.020$ (syst) $\pm 0.014$ (stat) $\text{ps}^{-1}$
CDF hadronic	$\Delta m_d = 0.536 \pm 0.028$ (syst) $\pm 0.006$ (stat) $\text{ps}^{-1}$
world average	$\Delta m_d = 0.508 \pm 0.004$ $\text{ps}^{-1}$

# *B* Mixing Fourier Analysis

## Two domains to fit for oscillations

- ▶ **time** → fit for a cosine wave
- ▶ **frequency** → examine f-spectrum

## Time domain approach

- ▶ fit for  $\Delta m_s$  in  $P(t) \sim 1 \pm \mathcal{D}\cos(\Delta m_s t)$

## Frequency domain approach

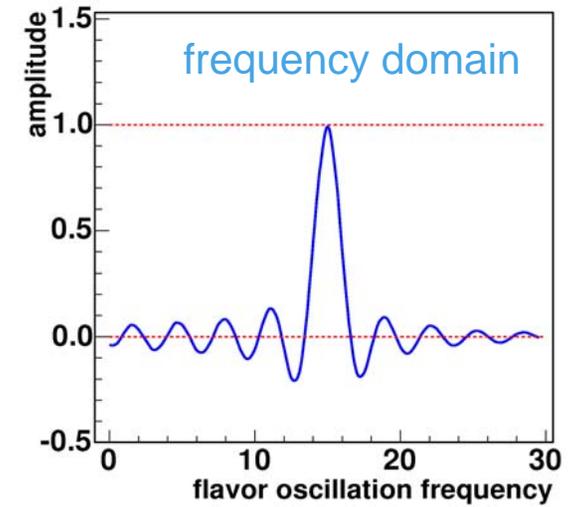
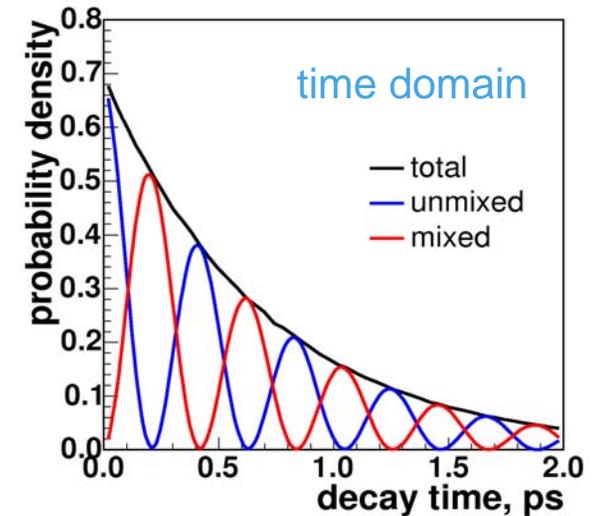
- ▶ introduce amplitude,  $P(t) \sim 1 \pm \mathcal{A}\mathcal{D}\cos(\Delta m_s t)$

- ▶ fit for  $\mathcal{A}$  at different  $\Delta m_s$

⇒ obtain frequency spectrum  $\mathcal{A}(\Delta m_s)$

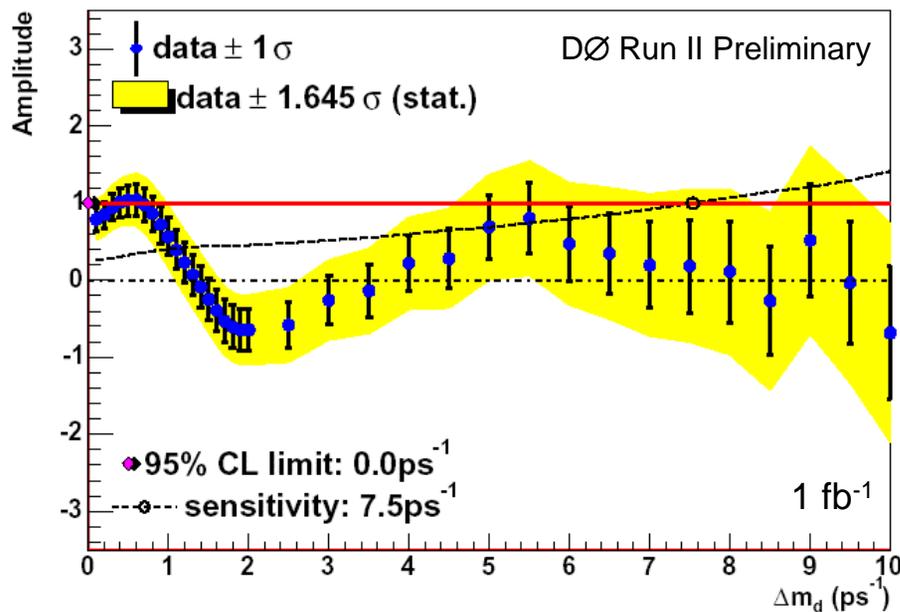
- ▶ method is called amplitude scan

- ▶ with flavor taggers calibrated  $\mathcal{A} = 1$  for the true  $\Delta m_s$  else  $\mathcal{A} = 0$

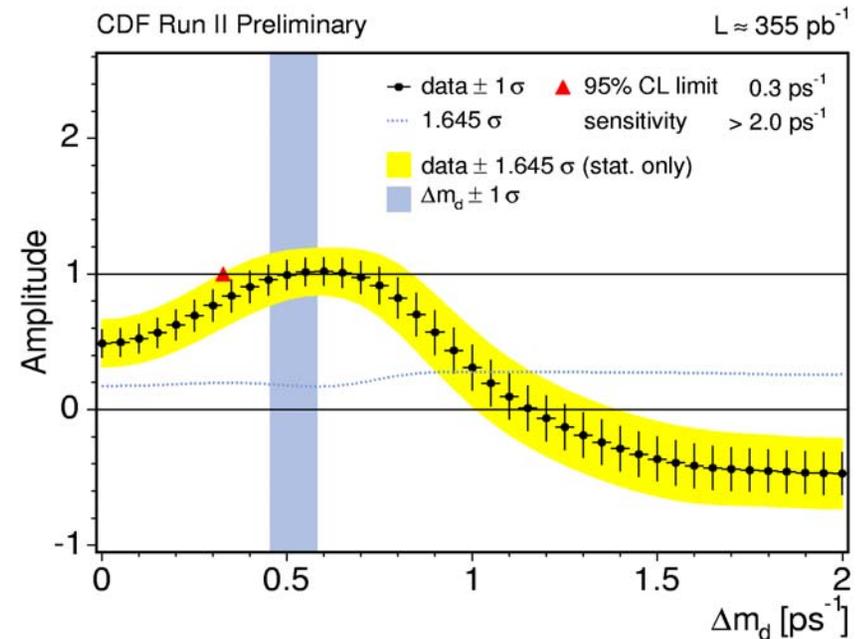


# B Mixing Amplitude Scans on $\Delta m_d$

- The yellow band is  $\pm 1.645\sigma_{\mathcal{A}}$  around data points
- $\Delta m$  values where  $\mathcal{A} + 1.645\sigma_{\mathcal{A}} < 1$  are excluded at 95% CL
- Sensitivity is where  $1.645\sigma_{\mathcal{A}} = 1$



$B \rightarrow \mu^+ D^- X$

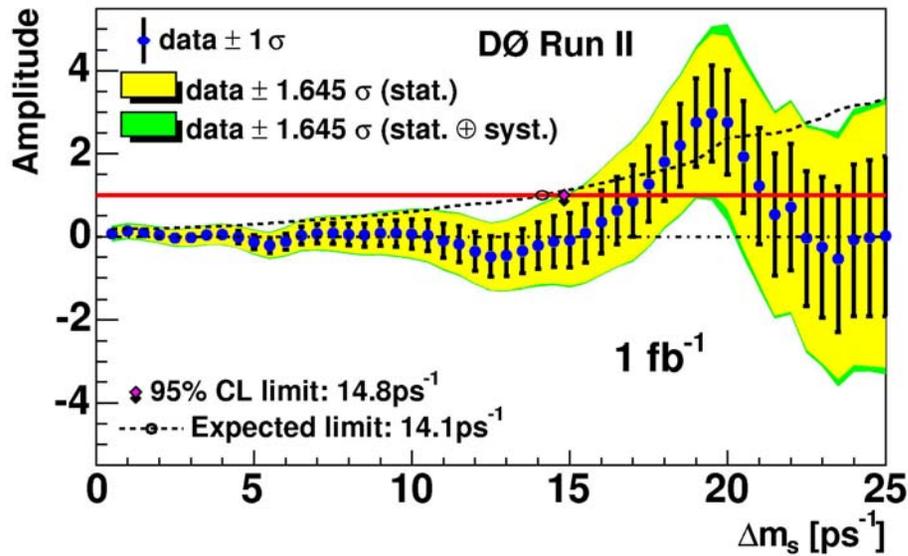


$B^0 \rightarrow J/\psi K^{*0}, B^0 \rightarrow D^- \pi^+$

Amplitude scan works on  $B^0$  decay modes

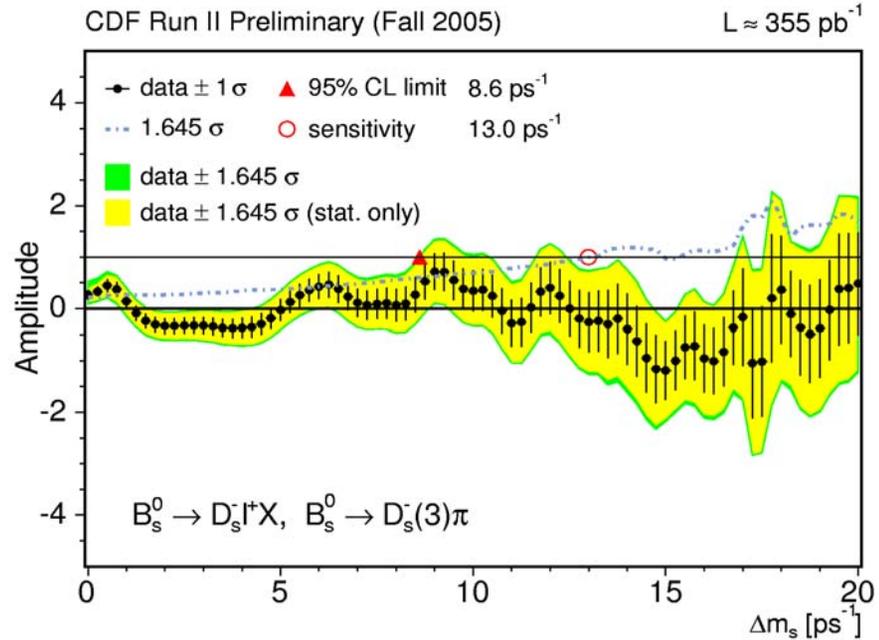
# B Mixing Amplitude Scans on $\Delta m_s$

$A/\sigma_A(\Delta m_s = 19 \text{ ps}^{-1}) = 2.5 \rightarrow 5\% \text{ p-value}$



DØ 1 fb<sup>-1</sup>

95% CL limit	14.8 ps <sup>-1</sup>
sensitivity	14.1 ps <sup>-1</sup>



CDF 355 pb<sup>-1</sup>

95% CL limit	8.6 ps <sup>-1</sup>
sensitivity	13.0 ps <sup>-1</sup>

# Summary

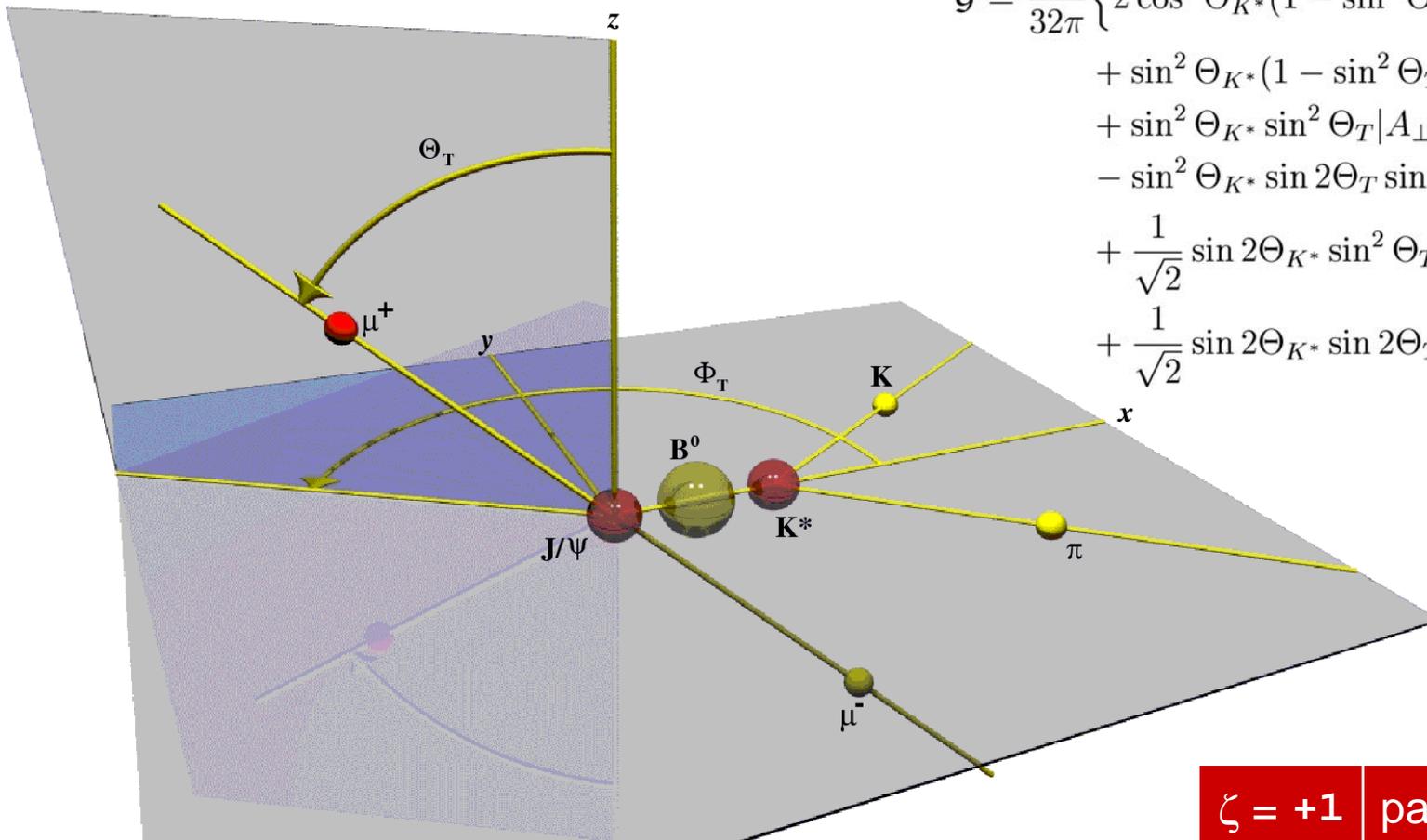
- New CDF  $\Lambda_b$  lifetime reduces distance with theory
- Best  $B_c$  lifetime in the world at CDF
- Best  $B_s$  lifetime in the world at DØ
- CDF measures by the first time  $B_s \rightarrow KK$  lifetime
- DØ finds  $B_s$  lifetime difference within SM ( $0.8 \text{ fb}^{-1}$ )
  
- DØ mixing squeezes their semileptonic decays
  - ▶  $\Delta m_s > 14.8 \text{ ps}^{-1}$  @ 95% CL ( $1 \text{ fb}^{-1}$ )
- CDF mixing expected to be probing SM soon
  - ▶  $\Delta m_s > 8.6 \text{ ps}^{-1}$  @ 95% CL ( $355 \text{ pb}^{-1}$ )



Backup

# Precision $B$ Lifetimes Transversity Basis

$$\mathcal{G} = \frac{9}{32\pi} \left\{ \begin{aligned} &2 \cos^2 \Theta_{K^*} (1 - \sin^2 \Theta_T \cos^2 \Phi_T) |A_0|^2 \\ &+ \sin^2 \Theta_{K^*} (1 - \sin^2 \Theta_T \sin^2 \Phi_T) |A_{||}|^2 \\ &+ \sin^2 \Theta_{K^*} \sin^2 \Theta_T |A_{\perp}|^2 \\ &- \sin^2 \Theta_{K^*} \sin 2\Theta_T \sin \Phi_T \text{Im}(A_{||}^* A_{\perp}) \zeta \\ &+ \frac{1}{\sqrt{2}} \sin 2\Theta_{K^*} \sin^2 \Theta_T \sin 2\Phi_T \text{Re}(A_0^* A_{||}) \\ &+ \frac{1}{\sqrt{2}} \sin 2\Theta_{K^*} \sin 2\Theta_T \cos \Phi_T \text{Im}(A_0^* A_{\perp}) \zeta \end{aligned} \right\}$$



- Transversity basis  $\equiv J/\psi$  rest frame
- $\phi$  flight direction  $\equiv +x$
- $KK$  plane  $\equiv xy$  plane

$\zeta = +1$	particle
$\zeta = -1$	antiparticle
$\zeta = 0$	untagged $B_s$