



# Measurements of B Hadron Lifetimes at CDF

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⊕ Introduction

⊕ **Measurements of...**

⊕  $B_c$  lifetime (semi-leptonic)

⊕ Flavor-specific  $B_s$  lifetime (fully hadronic)

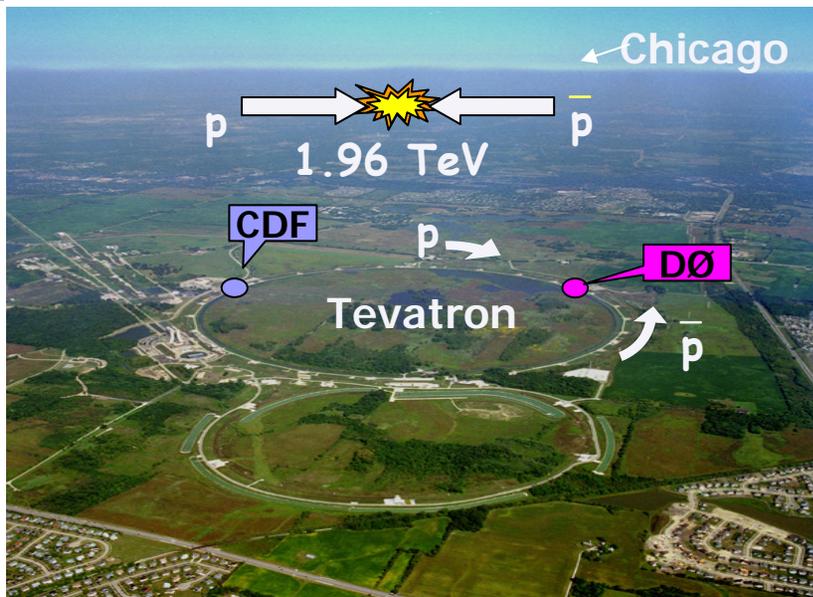
⊕  $\Lambda_b$  lifetime (fully hadronic)

⊕  $B^+$  lifetime (fully hadronic)

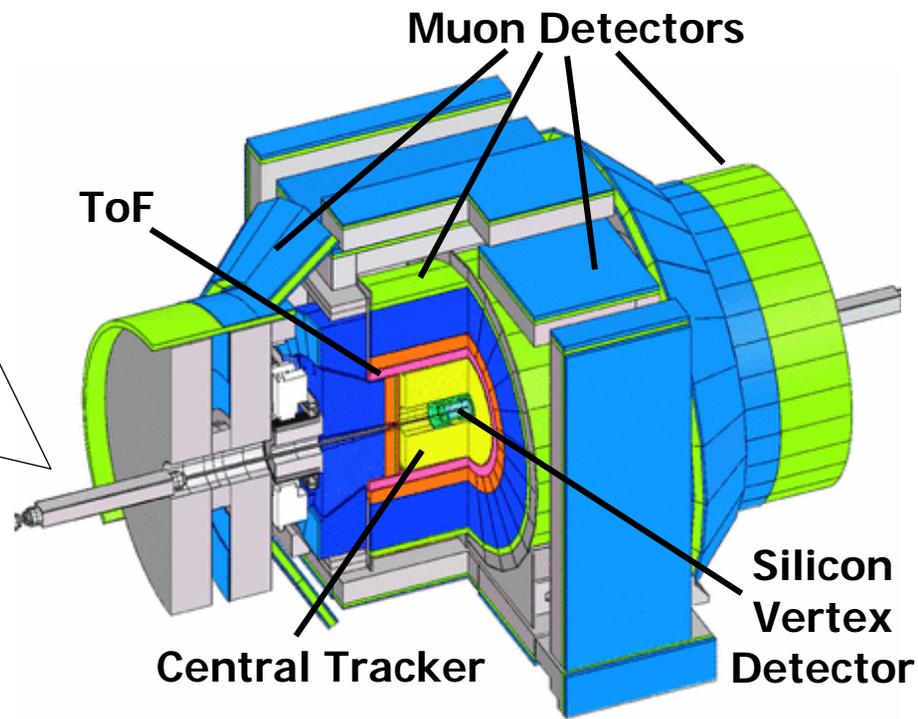
- proof of principle measurement  
using a data driven technique

⊕ Summary

# Tevatron and CDF Detector



- ⊕ Tevatron performing well!
- ⊕  $> 3 \text{ fb}^{-1}$  on tape
- ⊕ In this talk  $1-2 \text{ fb}^{-1}$  results!

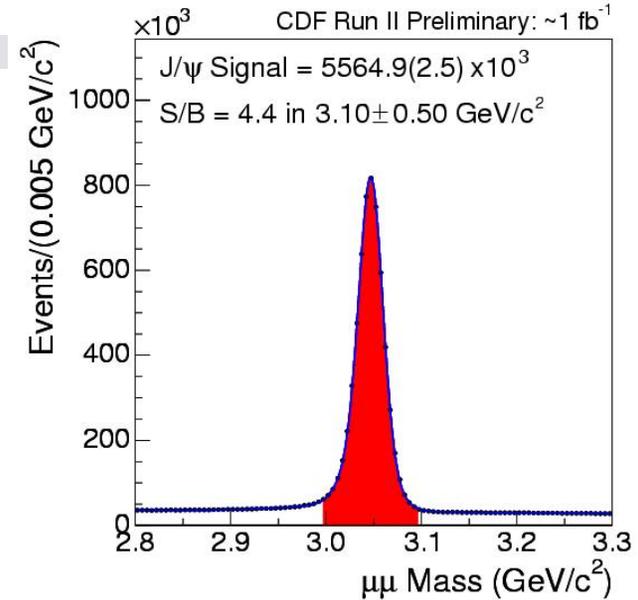


- ⊕ SVXII + L00
  - ⊕ hit resolution:  $9-11 \mu\text{m}$
- ⊕ Central Tracker
  - ⊕  $\sigma_{p_T}/p_T^2 < 0.1\%$ ,  $dE/dx$
- ⊕ Time-of-Flight
  - ⊕ Particle ID
- ⊕ Muon detectors
  - ⊕ Lepton triggers, Lepton ID

# Triggers for B Lifetime Measurements

## Di-Muon Trigger

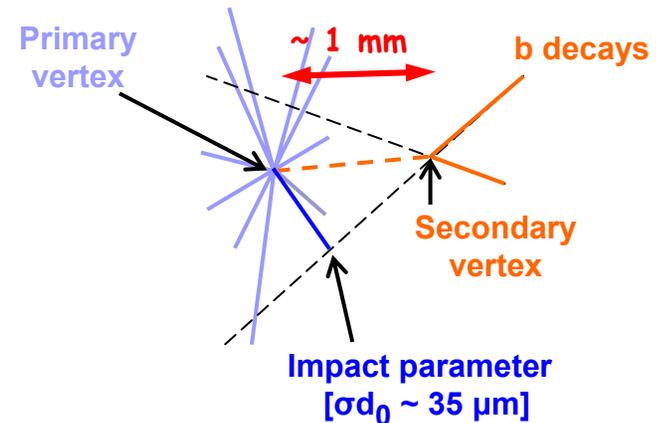
- Two muons with  $p_T > 1.5 \text{ GeV}$  in central pseudo-rapidity region.
- J/ $\Psi$  modes, masses, lifetimes, x-section ...
- Today  $B_c$  lifetime in J/ $\Psi \ell X$ ,  $\ell=e,\mu$



## Displaced vertex trigger

- $p_T(\text{Trk}) > 2 \text{ GeV}/c$ ,  $120 \mu\text{m} < d_0(\text{Trk}) < 1\text{mm}$
- X-section, branching ratios,  $B_s$  mixing...
- Today  $B_s$ ,  $\Lambda_b$  and  $B^+$  lifetimes

Decay length distribution biased!!

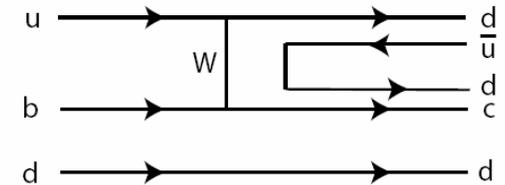
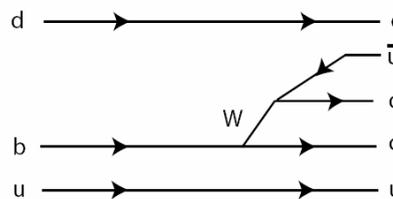
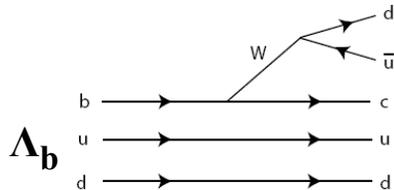
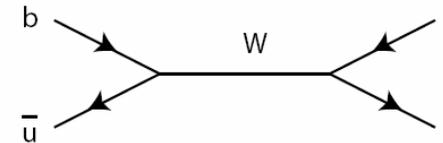
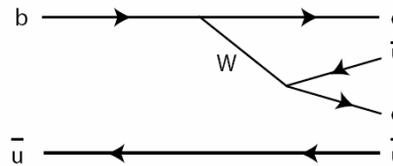
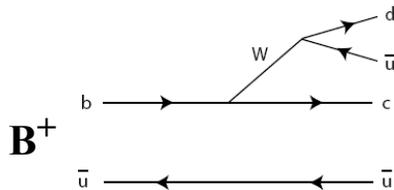


# Interests in B Hadron Lifetimes

## Heavy Quark Expansion

$$\Gamma = \frac{G_F^2 m_b^5}{192\pi^3} |V_{cb}|^2 \cdot \left[ \underbrace{A_0 + A_2 \left( \frac{\Lambda_{QCD}}{m_b} \right)^2}_{\text{orange}} + \underbrace{A_3 \left( \frac{\Lambda_{QCD}}{m_b} \right)^3}_{\text{green}} \right]$$

I. Bigi et. al,  
Ann. Rev. Nucl. Part. Sci. 47  
(1997) 591.



**Spectator model:**  
b hadron lifetimes  
are equal.

**Pauli Interference:**  
prolongs lifetimes,  
+5% for B<sup>+</sup>, +3% for Λ<sub>b</sub>

**Weak Annihilation  
and Exchange:**  
reduce lifetimes -7% Λ<sub>b</sub>

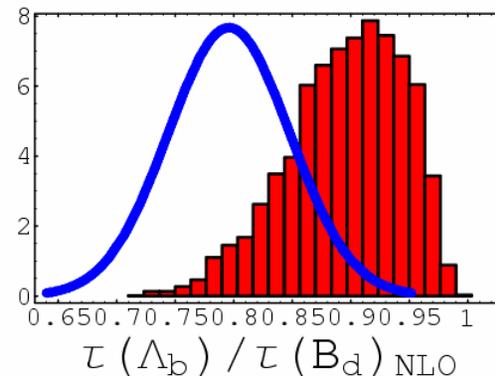
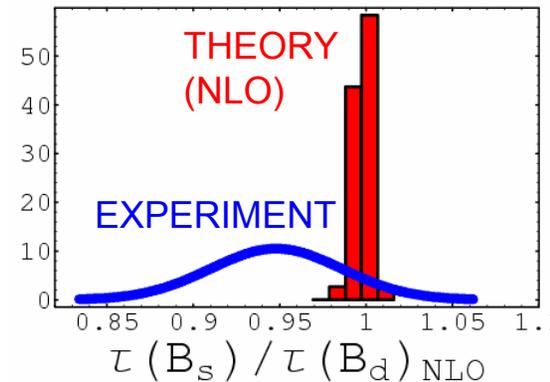
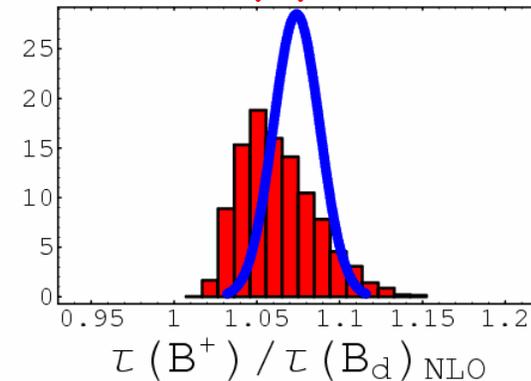
$$\tau(B^+) \geq \tau(B^0) \approx \tau(B_S^0) > \tau(\Lambda_b) \gg \tau(B_c)$$

# Interests in B Hadron Lifetimes *Continued...*

C. Tarantino,  
hep-ph/0310241

- ⊕ The  $B^+, B^0$  lifetimes are precisely measured at B-factories.
- ⊕ Experimental error on  $\tau(B_s^0)/\tau(B^0)$  far higher than theory error!
- ⊕ World average of  $\tau(\Lambda_b)/\tau(B^0)$  too low compared to  $O(1/m_b^3)$  HQE prediction. CDF 2006 measurement was precise but too high!
- ⊕ Lifetime ratio world averages:

$\tau(B^+)/\tau(B^0) = 1.071 \pm 0.009$	Theory $O(1/m_b^4)$ $1.06 \pm 0.02$
$\tau(B_s^0)/\tau(B^0) = 0.939 \pm 0.021$ <small>PDG 2007</small>	$1.00 \pm 0.01$
$\tau(\Lambda_b)/\tau(B^0) = 0.904 \pm 0.032$	$0.88 \pm 0.05$



# $B_c$ : A Special Case...

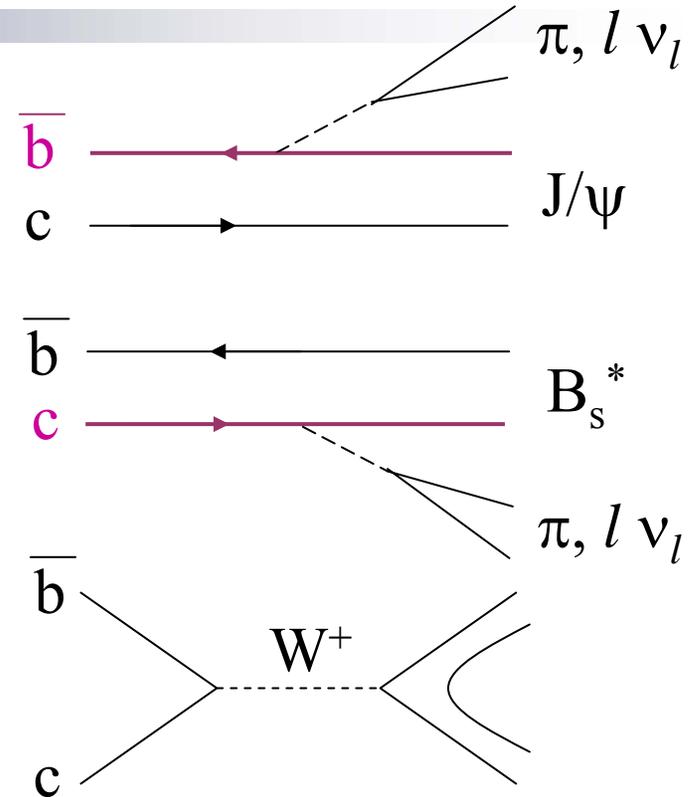
- ⊕ Doubly heavy  $\bar{b}c$  bound state
- ⊕ Decays via weak decays of b- or c-quark or via weak annihilation

$$\Gamma_{B_c} = \Gamma_b (\approx 25\%) + \Gamma_c (\approx 65\%) + \Gamma_w$$

- ▶ Shorter lifetime than light B mesons

Theory prediction:

$$\tau(B_c) = 0.47 - 0.59 \text{ ps}$$



arXiv:hep-ph/0308214v1  
 Phy Rev. D 64, 14003 (2001)  
 Phy Lett. B 452, 129 (1999)  
 hep-ph/0002127

# Lifetime in $B_c \rightarrow J/\psi e, \mu \nu$

✦ **Missing momentum**, correct pseudo-lifetime:

$$\text{✦ } ct = K \times ct^*$$

$$\text{✦ } ct^* = \frac{M(B_c) L_{xy}(J/\psi + l)}{p_T(J/\psi + l)}$$

$$\text{✦ } K = p_T(J/\psi + l) / p_T(B_c)$$

✦ Main challenge is **multiple backgrounds**:

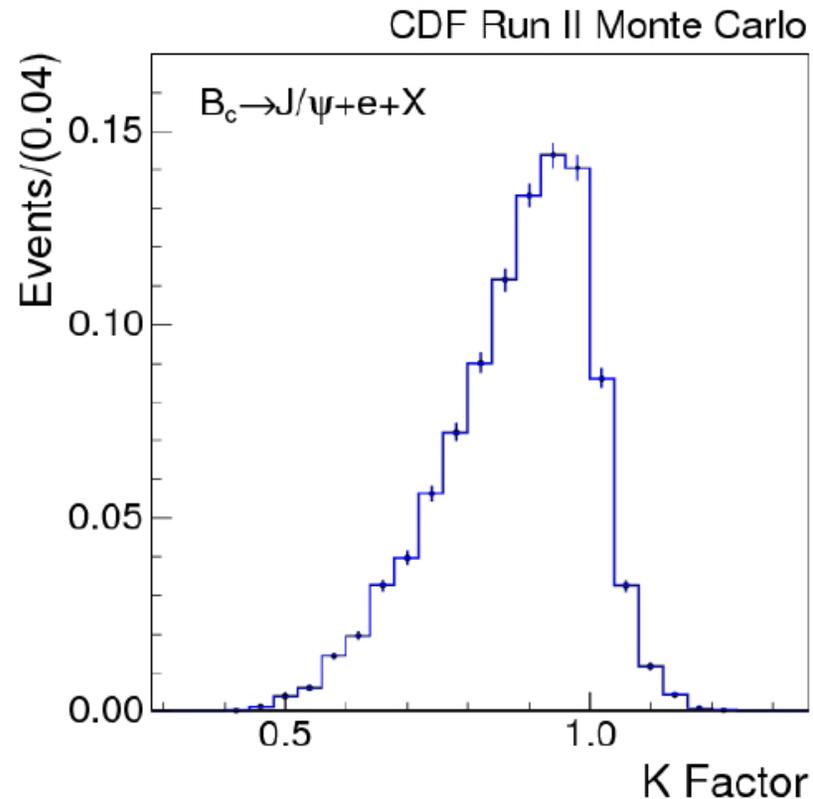
✦ real  $J/\psi$  + fake lepton

✦ fake  $J/\psi$  + real lepton

✦ real  $J/\psi$  + real lepton  $\rightarrow$  from  $bb$  events

✦ prompt  $J/\psi$  + lepton

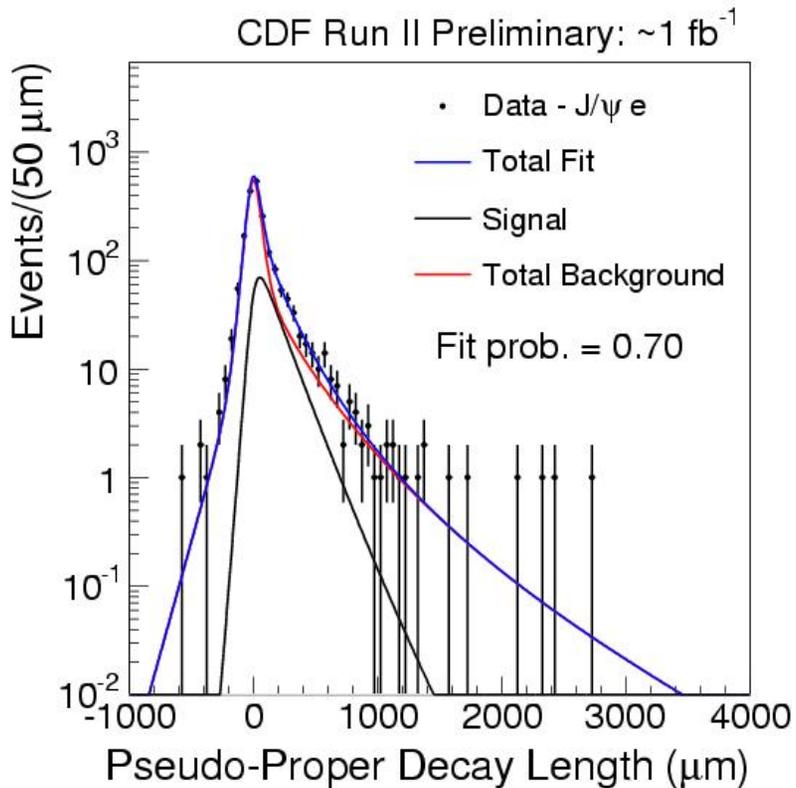
✦ residual conversion ( $J/\psi + e$  only)



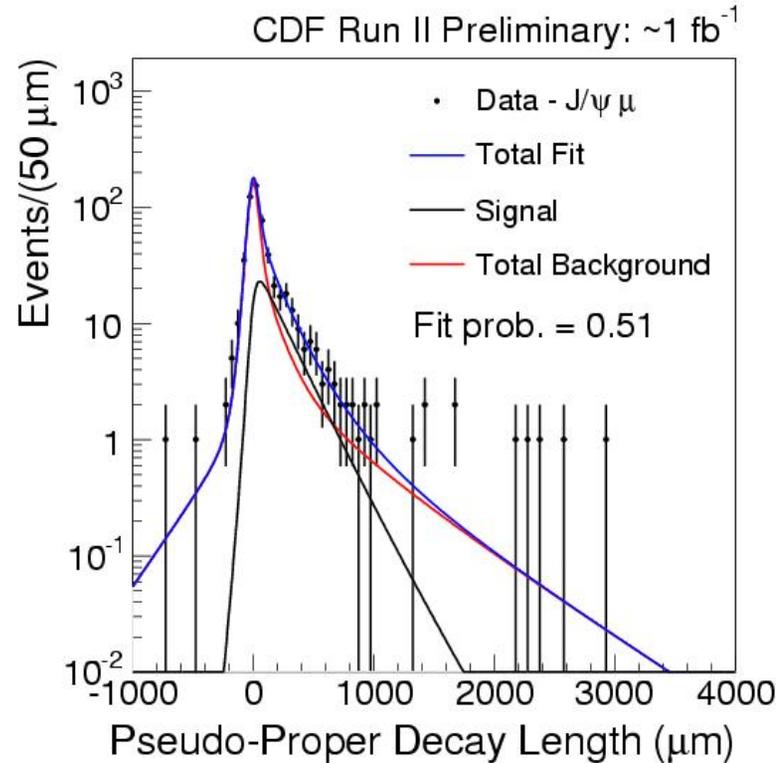
**5564.9k** signal  $J/\psi$

events from **1  $\text{fb}^{-1}$**  data

# Lifetime in $B_c \rightarrow J/\psi e, \mu \nu$

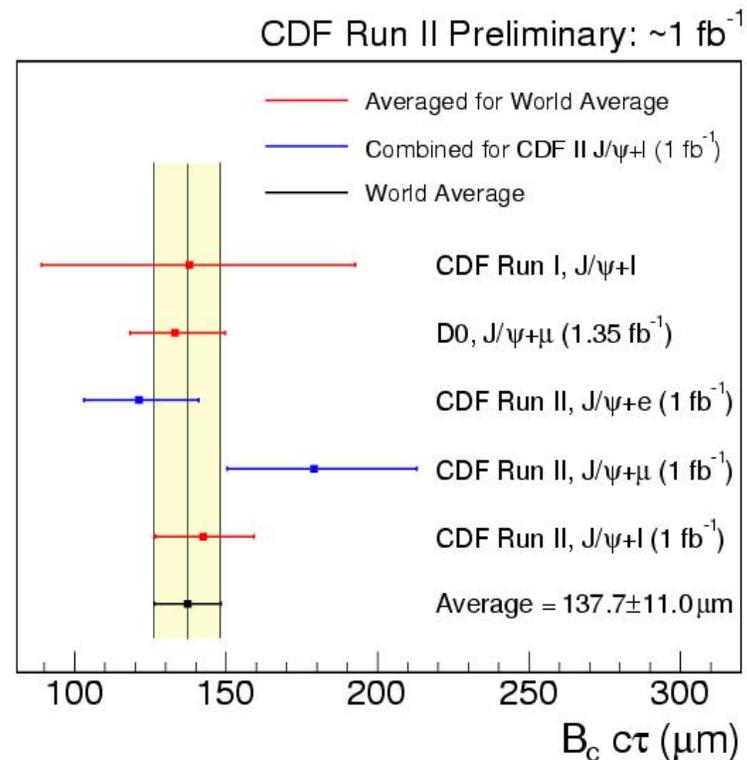
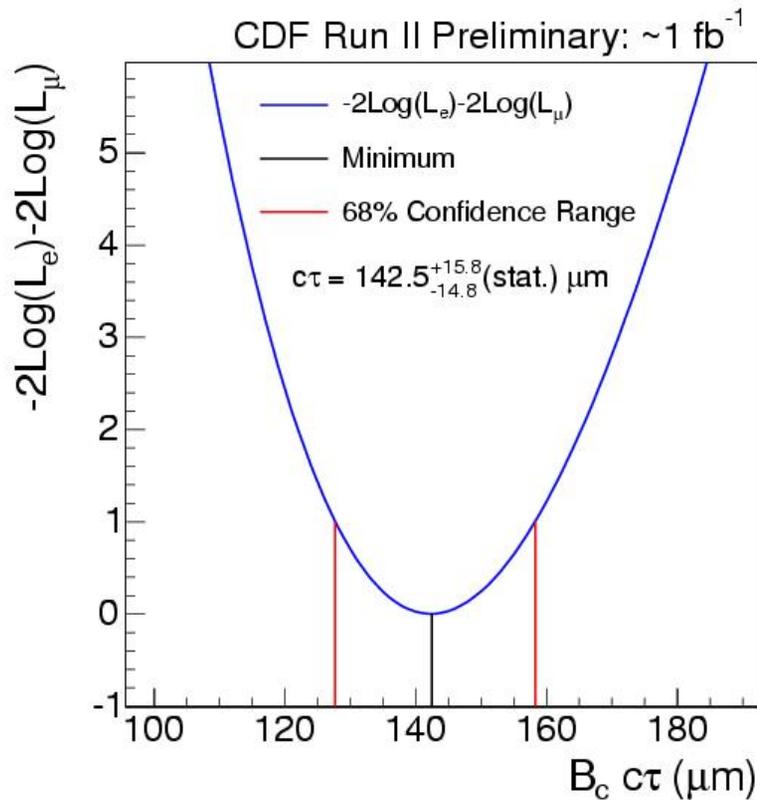


$$c\tau(B_c) = 121.7^{+18.0}_{-16.3} \text{ (stat)} \mu\text{m}$$



$$c\tau(B_c) = 179.1^{+32.6}_{-27.2} \text{ (stat)} \mu\text{m}$$

# Lifetime in $B_c \rightarrow J/\psi e, \mu \nu$



$$\tau(B_c) = 0.475^{+0.052}_{-0.049} \text{ (stat)} \pm 0.018 \text{ (syst) ps}$$

**World best measurement!**

Tevatron weighted average:

$$\tau = 0.459 \pm 0.037 \text{ ps}$$

Theory:  $\tau = 0.47 - 0.59 \text{ ps}$

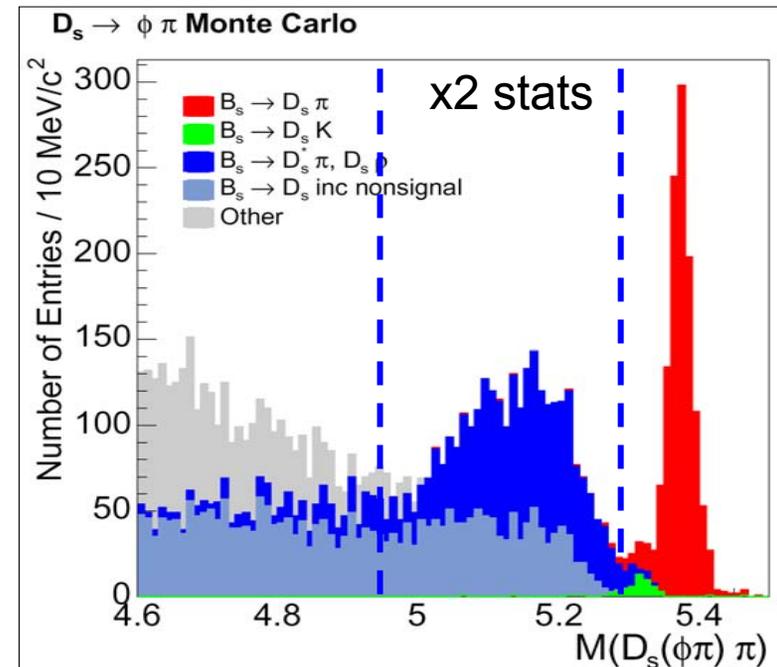
# $B_s$ Lifetime in $B_s \rightarrow D_s^+(\phi\pi)\pi^- X$

## ⊕ Data sample:

- ⊕ **1.3 fb<sup>-1</sup>**, collected with displaced vertex trigger
- ⊕ ~ 1100 fully reconstructed events
- ⊕ ~ 2000 partially reconstructed events

## ⊕ Lifetime bias is modeled with a **trigger efficiency curve** from MC

- ## ⊕ Partially reconstructed channels: $B_s \rightarrow D_s^* \pi, D_s \rho^-(\pi^0 \pi^-)$ triple the statistics!



Bs lifetime difference:  
presented by Farrington

# $B_s$ Lifetime in $B_s \rightarrow D_s^+(\phi\pi)\pi^- X$

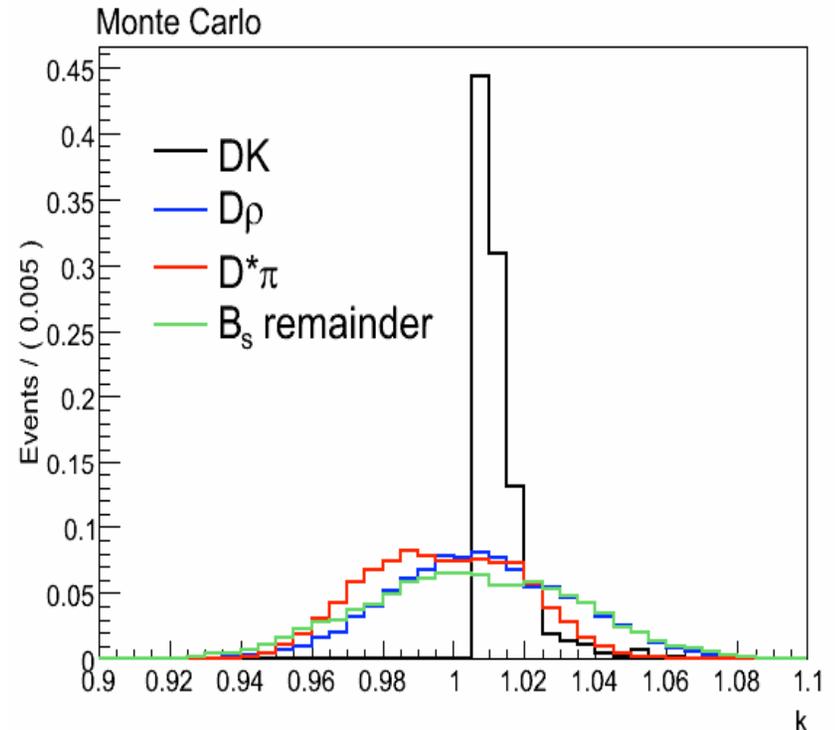
- ⊕ For partially reconstructed modes a **k-factor** accounts for missing momentum and mass

$$ct = \frac{L_{xy} \cdot m_B^{rec}}{p_T} \cdot K$$

- ⊕ Extensive test on  $B^0$ ,  $B^+$  control samples

## ⊕ Two-step fit

- ⊕ **mass fit**: relative fraction of various modes and background
- ⊕ **lifetime fit**: shapes from MC/data, fractions from mass fit.
  - ▶ **Extract lifetime only**



Lifetime for control samples:

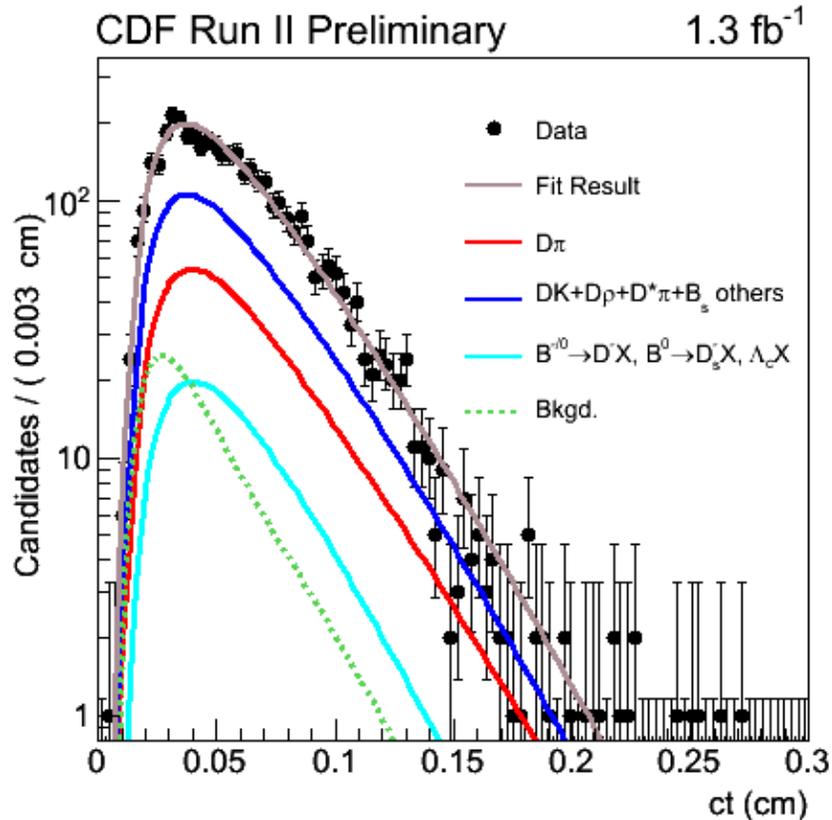
$B^0 \rightarrow D^-(K^+\pi^-\pi^-)\pi^+$

$B^0 \rightarrow D^{*-}(D^0(K^+\pi^-)\pi^-)\pi^+$

$B^+ \rightarrow D^0(K^+\pi^-)\pi^+$

**agree well with PDG**

# $B_s$ Lifetime in $B_s \rightarrow D_s^+(\phi\pi)\pi^- X$



ALEPH (1996)

$$1.54^{+0.14}_{-0.13} \pm 0.04$$

OPAL (1998)

$$1.5^{+0.16}_{-0.15} \pm 0.04$$

CDF (1999)

$$1.36 \pm 0.09^{+0.06}_{-0.05}$$

DELPHI (2000)

$$1.42^{+0.14}_{-0.13} \pm 0.03$$

D0 (2006)

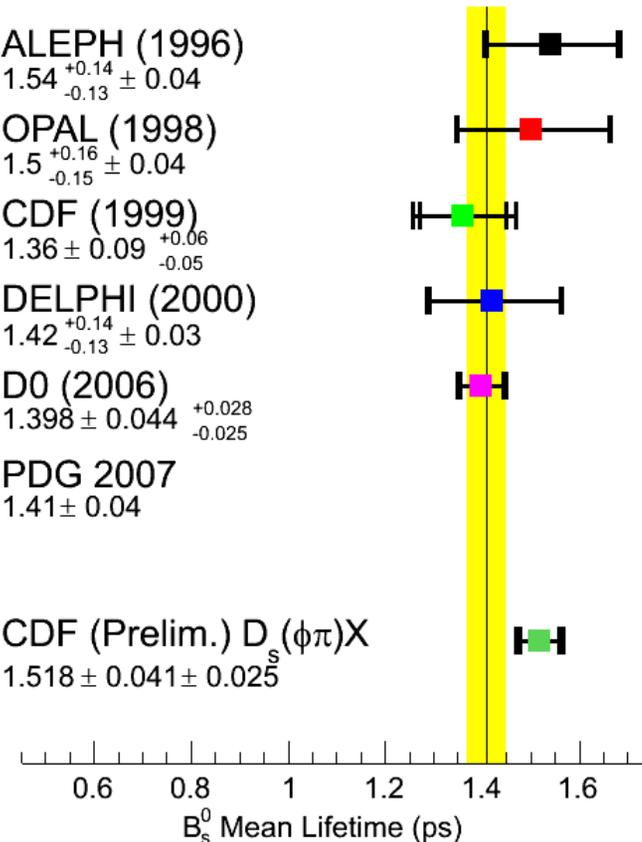
$$1.398 \pm 0.044^{+0.028}_{-0.025}$$

PDG 2007

$$1.41 \pm 0.04$$

CDF (Prelim.)  $D_s(\phi\pi)X$

$$1.518 \pm 0.041 \pm 0.025$$



Flavor-specific

$$\tau(B_s) = 1.518 \pm 0.041 (\text{stat}) \pm 0.025 (\text{syst}) \text{ ps}$$

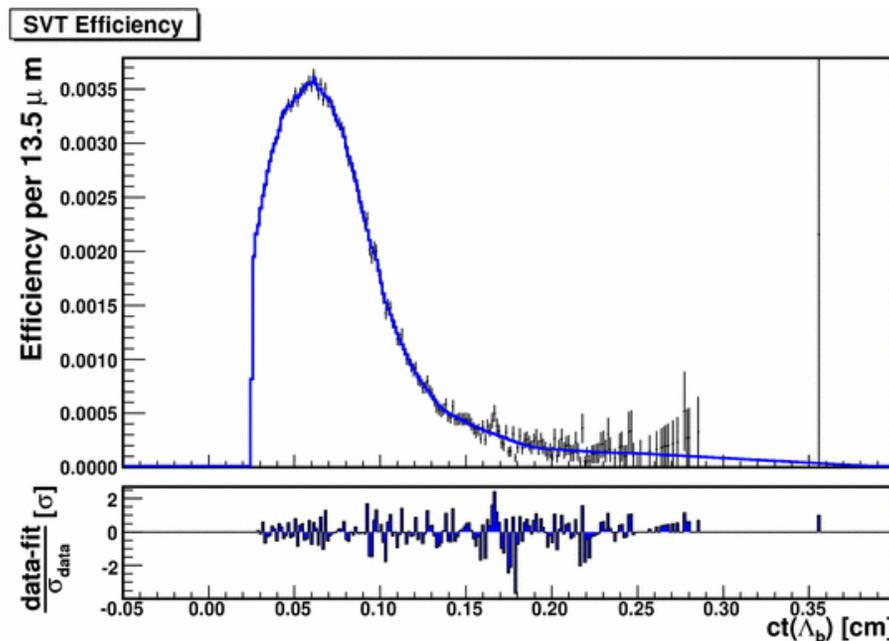
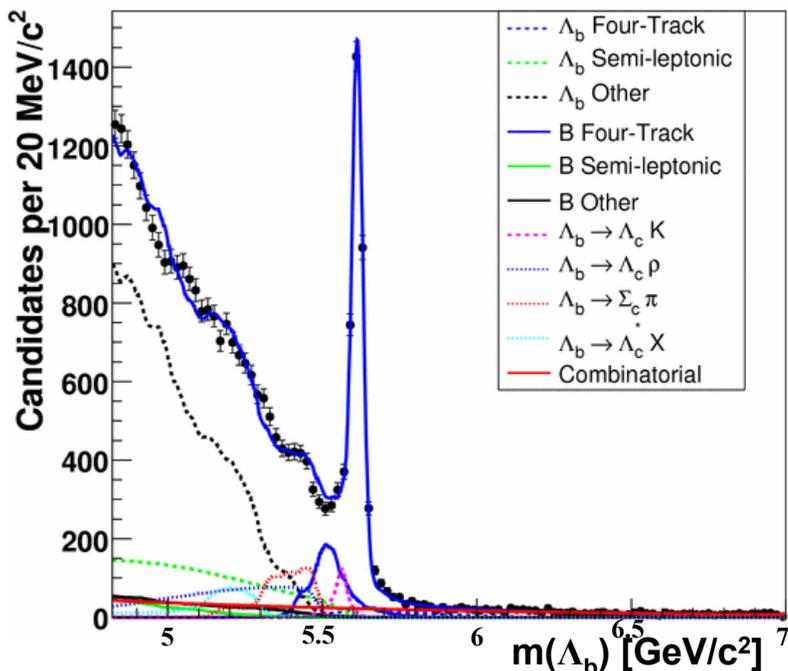
**World best measurement!**

# $\Lambda_b$ Lifetime in $\Lambda_b \rightarrow \Lambda_c \pi$

- ⊕ 1 fb<sup>-1</sup> data, 2900 events
- ⊕ Signal region:  
5.565 < m( $\Lambda_b$ ) < 5.670 GeV/c<sup>2</sup>
- ⊕ Lifetime analysis developed w/ data fit blinded.

- ⊕ Trigger efficiency curve from MC simulation
- ⊕ Two step fit: mass, lifetime
- ⊕ Fit checked with MC samples with input lifetimes between 325 - 500  $\mu$ m.

CDF II Preliminary, L = 1.1 fb<sup>-1</sup>



# $\Lambda_b$ Lifetime in $\Lambda_b \rightarrow \Lambda_c \pi$

⊕ We measure:

$$\tau(\Lambda_b) = 1.410 \pm 0.046 \text{ (stat)} \pm 0.029 \text{ (syst)} \text{ ps}$$

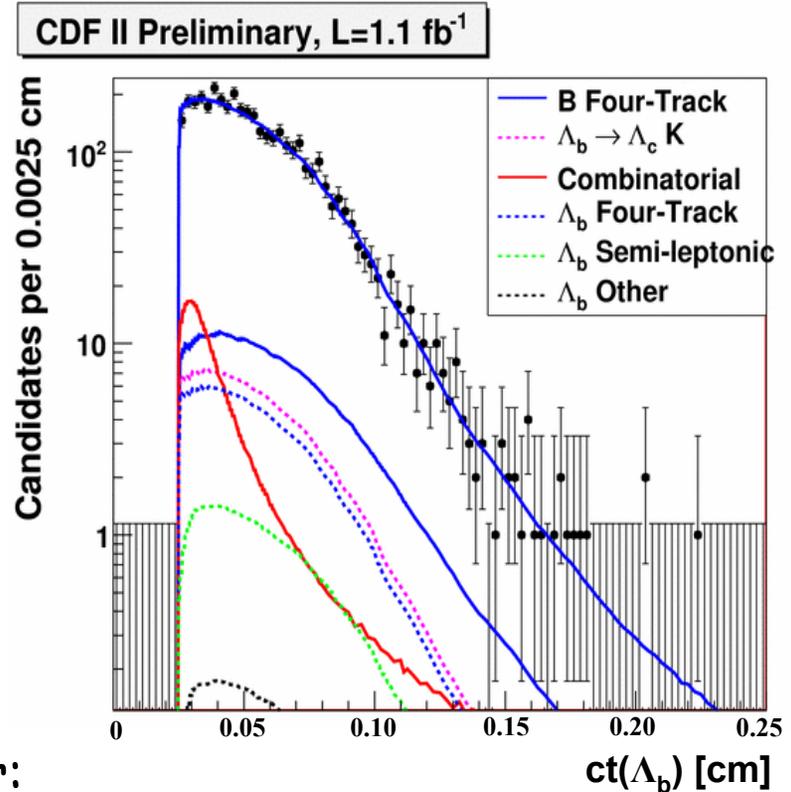
**World best measurement!**

⊕ Using world average  $B^0$  lifetime:

$$\frac{\tau(\Lambda_b)}{\tau(B^0)} = 0.922 \pm 0.039 \text{ (stat + syst)}$$

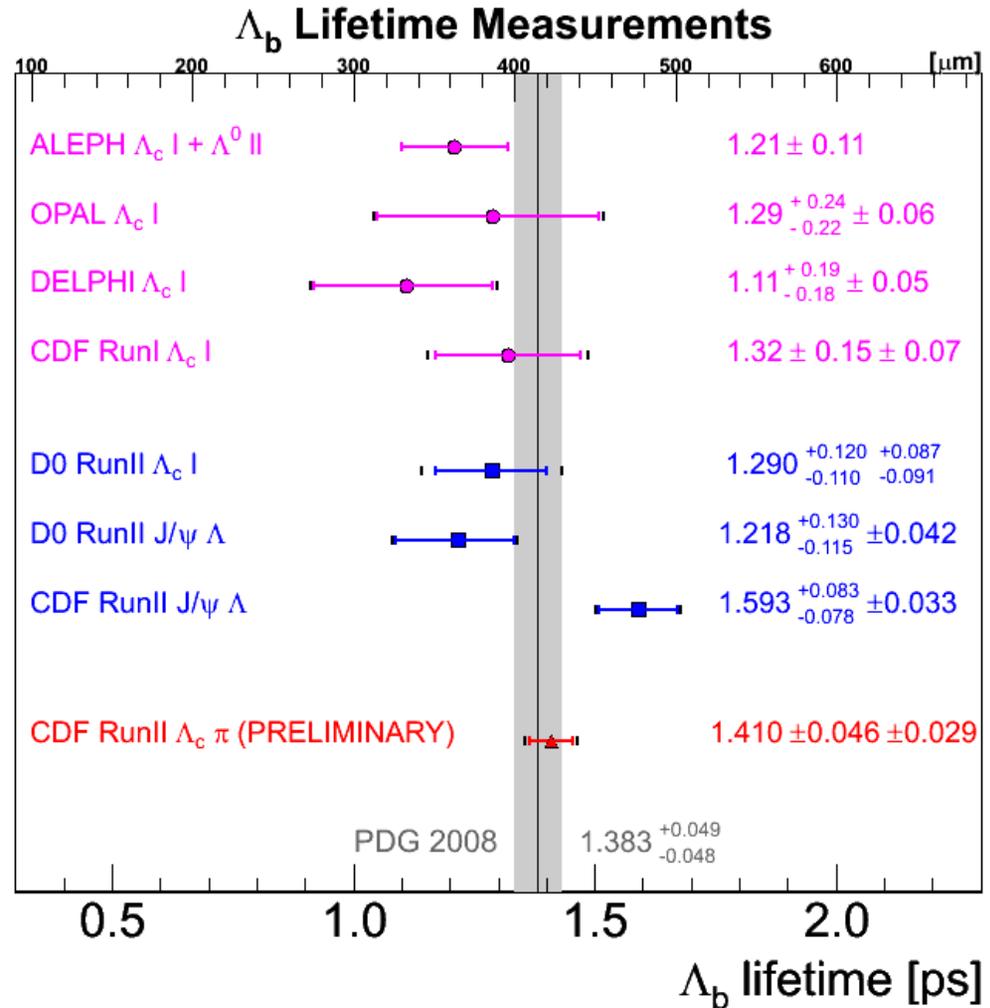
⊕ Leading sources of systematic error:

- ⊕ Displaced vertex trigger modeling: 71.6%
- ⊕  $\Lambda_c$  Dalitz structure: 42.0%
- ⊕ Combinatoric ct template: 32.9%



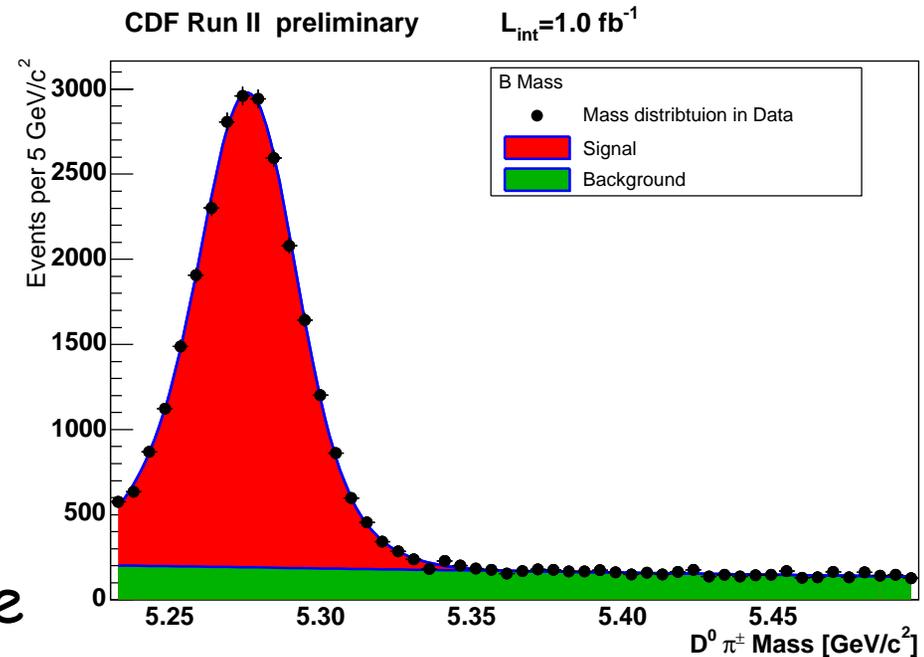
# $\Lambda_b$ Lifetime in $\Lambda_b \rightarrow \Lambda_c \pi$

⊕ Good agreement with world average and theory (lifetime ratio).



# B<sup>+</sup> Lifetime in D<sup>0</sup> π<sup>+</sup> Decays

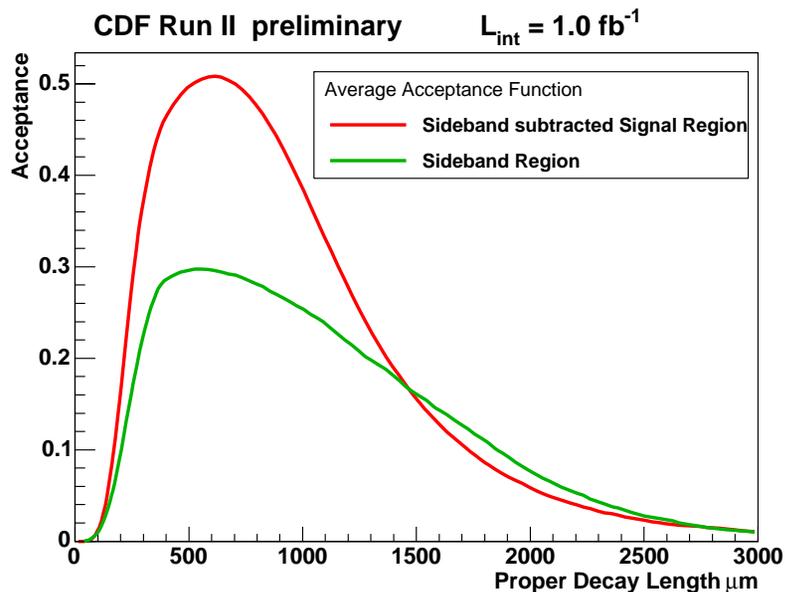
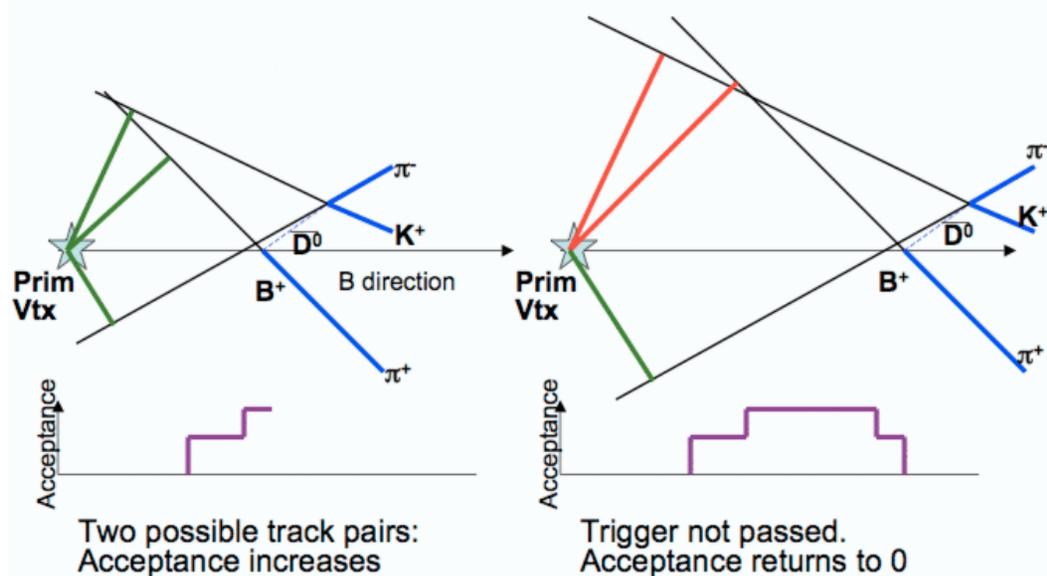
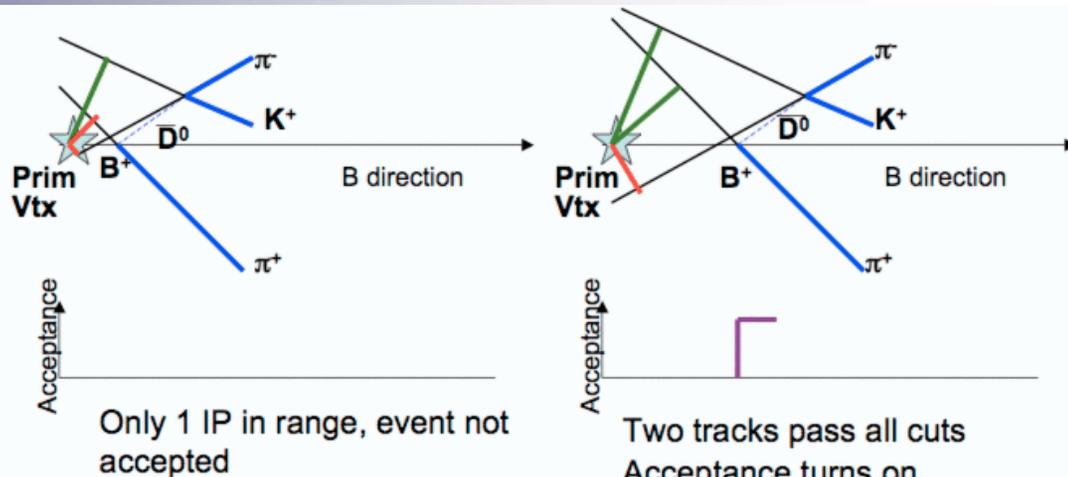
- ⊕ Proof of principle measurement employing a **data driven method** to correct for trigger bias.
- ⊕ Uses **decay kinematics** to correct bias on an event-by-event basis.
- ⊕ Method applicable to future experiments which use impact parameter based triggers.
- ⊕ Systematic error due to MC modeling is completely avoided.



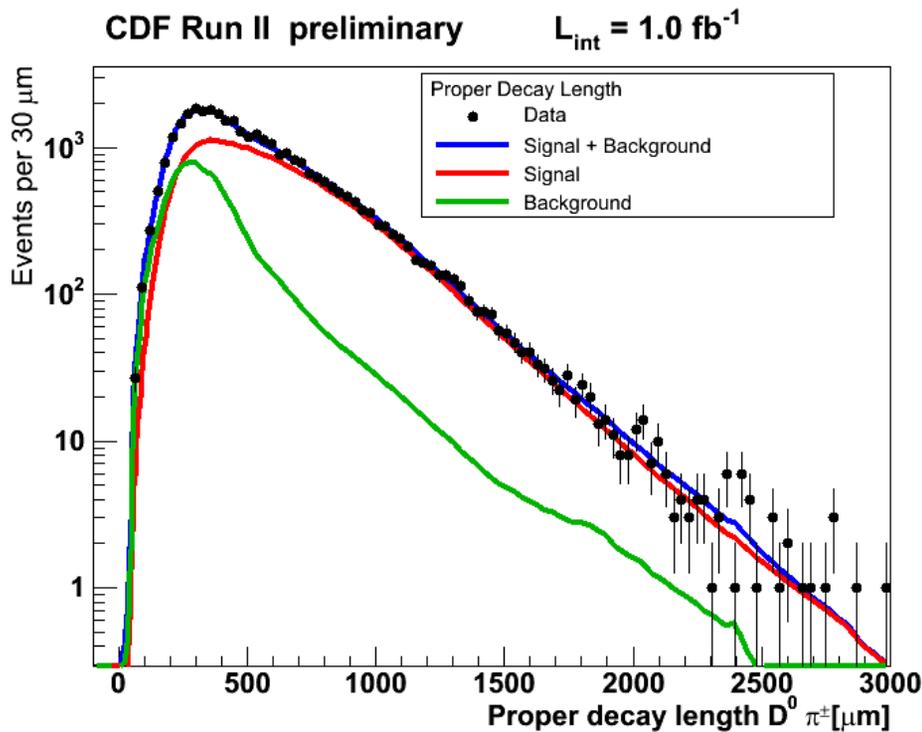
**24200 ± 200** signal  
events from **1 fb<sup>-1</sup>** data

# Data Driven Trigger Bias Correction

- Events are slid along the B direction and trigger acceptance is evaluated as a function of proper decay length



# B<sup>+</sup> Lifetime in D<sup>0</sup> π<sup>+</sup> Decays



⊕ Dominant sources of systematic error:

- ⊕ IP (68.9%),  $p_T$  (40%) dependence of track finding efficiency
- ⊕ Mass-lifetime correlation (55.6%) in background

⊕ We measure:  $\tau(B^+) = 1.662 \pm 0.023 \text{ (stat)} \pm 0.013 \text{ (syst)} \text{ ps}$

⊕ Current world average:  $1.638 \pm 0.011 \text{ ps}$

# Summary

- ⊕ With over  $3 \text{ fb}^{-1}$  accumulated data and much more to come, heavy flavor physics at CDF has entered a precision era.
- ⊕ World's best  $B_s$ ,  $B_c$  and  $\Lambda_b$  lifetime measurements from CDF are in agreement with the world averages and HQE predictions.
- ⊕ Stay tuned for more!!

<http://www-cdf.fnal.gov/physics/new/bottom/bottom.html>

# Backup-1 Data Driven Lifetime Method

⊕ Unbiased decay PDF:  $\frac{e^{-\frac{t}{\tau}}}{\tau}$

⊕ ... with high and low IP cuts:  $\frac{e^{-\frac{t}{\tau}}}{\tau(e^{-\frac{t_{min}}{\tau}} - e^{-\frac{t_{max}}{\tau}})}$

⊕ A triggered event w/ IP cuts, single track eff. and multiple track combination considered:

$$\frac{e^{-\frac{t_j}{\tau}} ([\Theta(t_{min}^1) - \Theta(t_{max}^1)]p(n_1, k_1, \epsilon_s) + \dots [\Theta(t_{min}^N) - \Theta(t_{max}^N)]p(n_N, k_N, \epsilon_s))}{\tau((e^{-\frac{t_{min}^1}{\tau}} - e^{-\frac{t_{max}^1}{\tau}}))p(n_1, k_1, \epsilon_s) + \dots p(n_N, k_N, \epsilon_s)(e^{-\frac{t_{min}^N}{\tau}} - e^{-\frac{t_{max}^N}{\tau}})}$$

⊕ where,  $k_i$  out of  $n_i$  tracks have a matching trigger track in the  $i^{\text{th}}$  of  $N$  different ways to satisfy the trigger.