

**Measurement of Forward-Backward  
Asymmetry in Top Quark Pair Production  
in  $p\bar{p}$  Collisions at 1.96 TeV**

**Glenn Strycker**

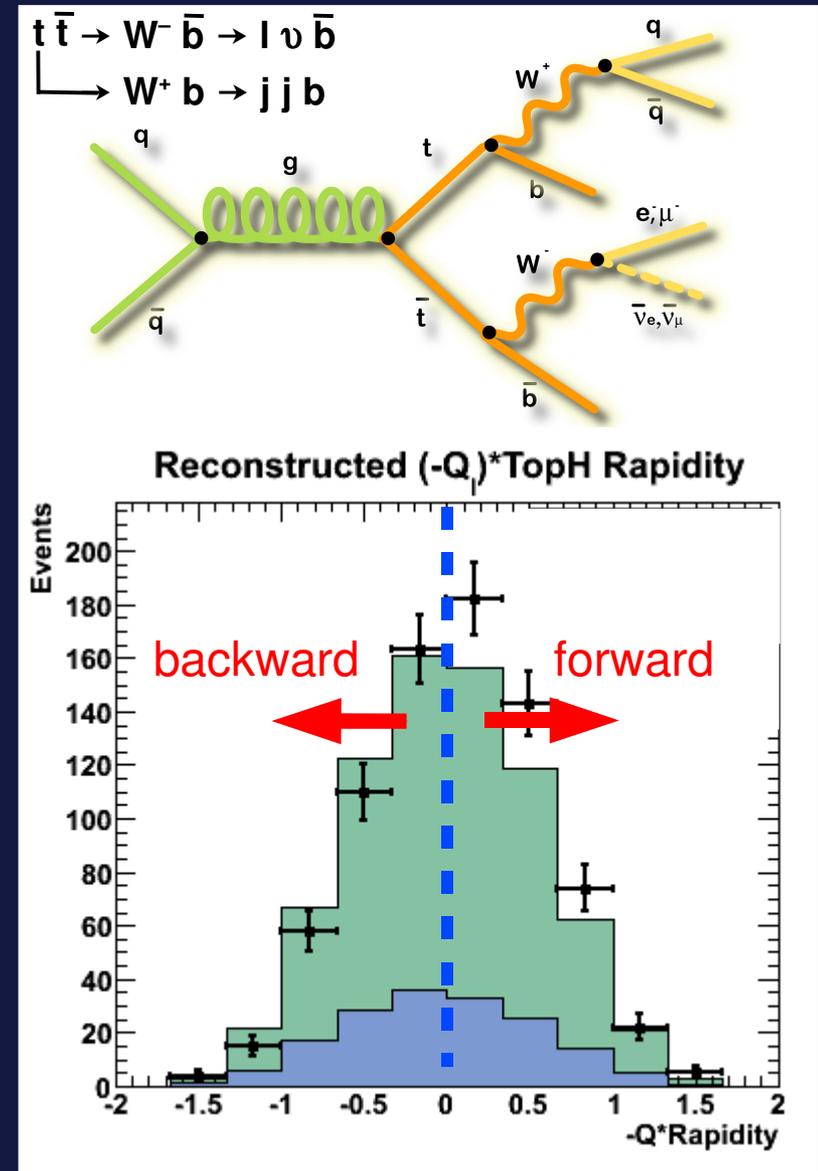
**University of Michigan**

**On behalf of the CDF Collaboration**





- Hadronic top decay is more accurately reconstructed, so we will measure  $y_{had}$
- Get hadronic top charge from lepton
- Invoke CP invariance and multiply hadronic-only distribution by  $-1 \cdot \text{lepton charge}$  to find equivalent top rapidity in each event
- Measure  $A_{fb}$  using  $-Q_{lep} \cdot y_{had}$  in the lab frame, count forward and backward events
- Correct  $A_{fb}$  back to parton level



- Previously, using  $-Q_{lep} \cdot \cos(\theta_{had})$ , we measured  $A_{fb}^{lab} = 0.17 \pm 0.08$  using  $1.9 \text{ fb}^{-1}$  of data
- D-zero measured a detector-level  $A_{fb} = 0.12 \pm 0.08 \pm 0.01$  using  $0.9 \text{ fb}^{-1}$  of data

Selection

- Measurement is performed using semi-leptonic top pair decays
- 3.2 fb<sup>-1</sup> of CDF data
- $\geq 4$  jets ( $E_t > 20$  GeV and  $|\eta| < 2$ )
- $\geq 1$  b-tagged jet
- 1 electron ( $E_t > 20$  GeV and  $|\eta| < 1$ ) –or–  
1 muon ( $P_t > 20$  GeV/c and  $|\eta| < 1$ )
- Missing Transverse Energy  $> 20$  GeV

Backgrounds

- Use the techniques for estimating tagged backgrounds in the W+jets sample to determine semi-leptonic ttbar background

Process	
W+HF Jets	$86.56 \pm 27.40$
Mistags (W+LF)	$27.43 \pm 7.70$
Non-W (QCD)	$33.44 \pm 28.06$
Single Top	$7.82 \pm 0.50$
WW/WZ/ZZ	$7.57 \pm 0.74$
Z+Jets	$4.78 \pm 0.59$
Top	$569.08 \pm 78.81$
Total Prediction	$736.64 \pm 89.22$

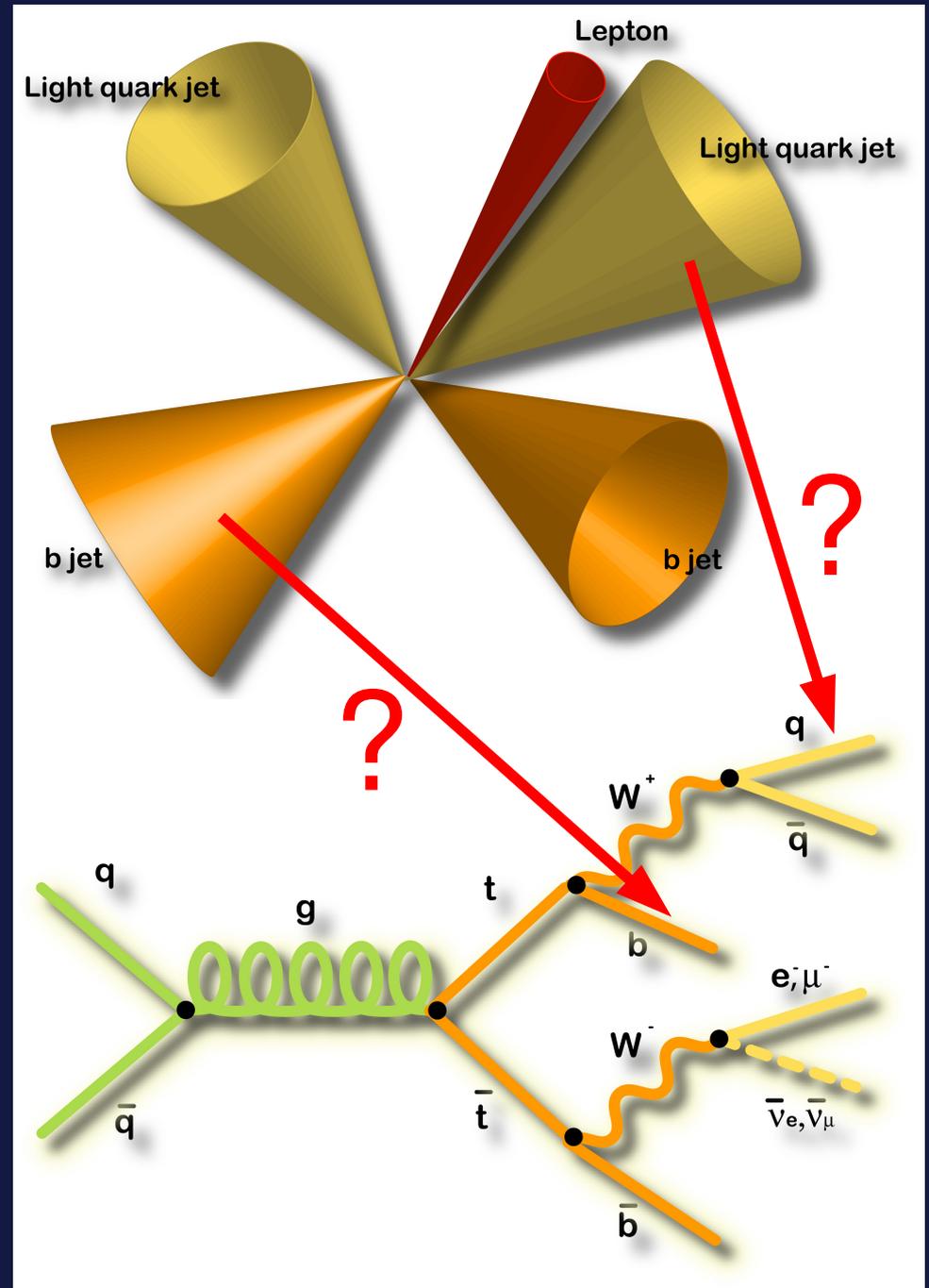
776 Candidate Events

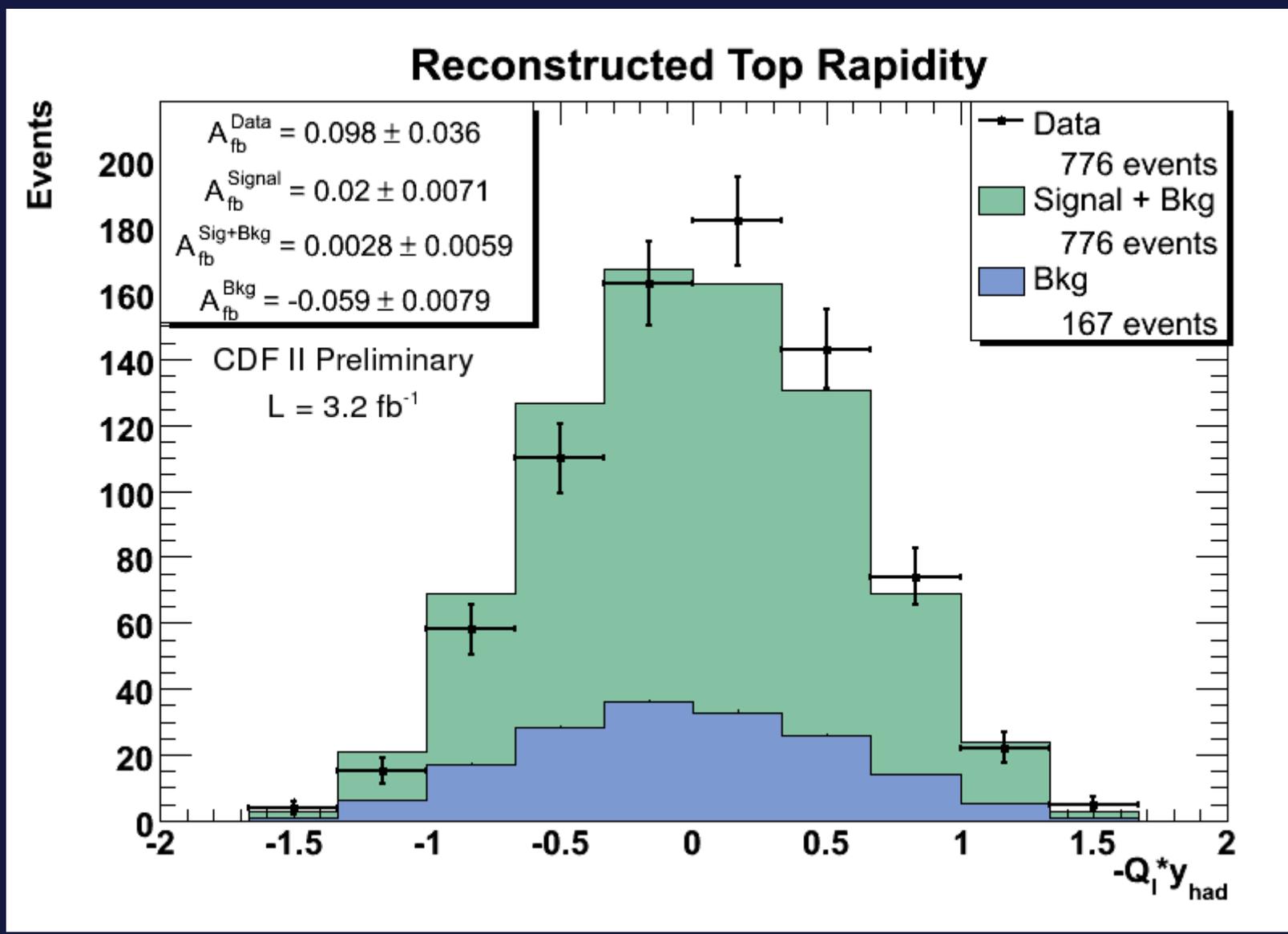
$167 \pm 34$  Predicted Background

## Reconstruction

- Match jets to b, bbar, up, down
- Constrain fit W mass to 80.4 GeV/c<sup>2</sup>
- Constrain fit for a 175.0 GeV/c<sup>2</sup> Top
- Float momenta of jets within known resolution
- Use combination with lowest  $\chi^2$

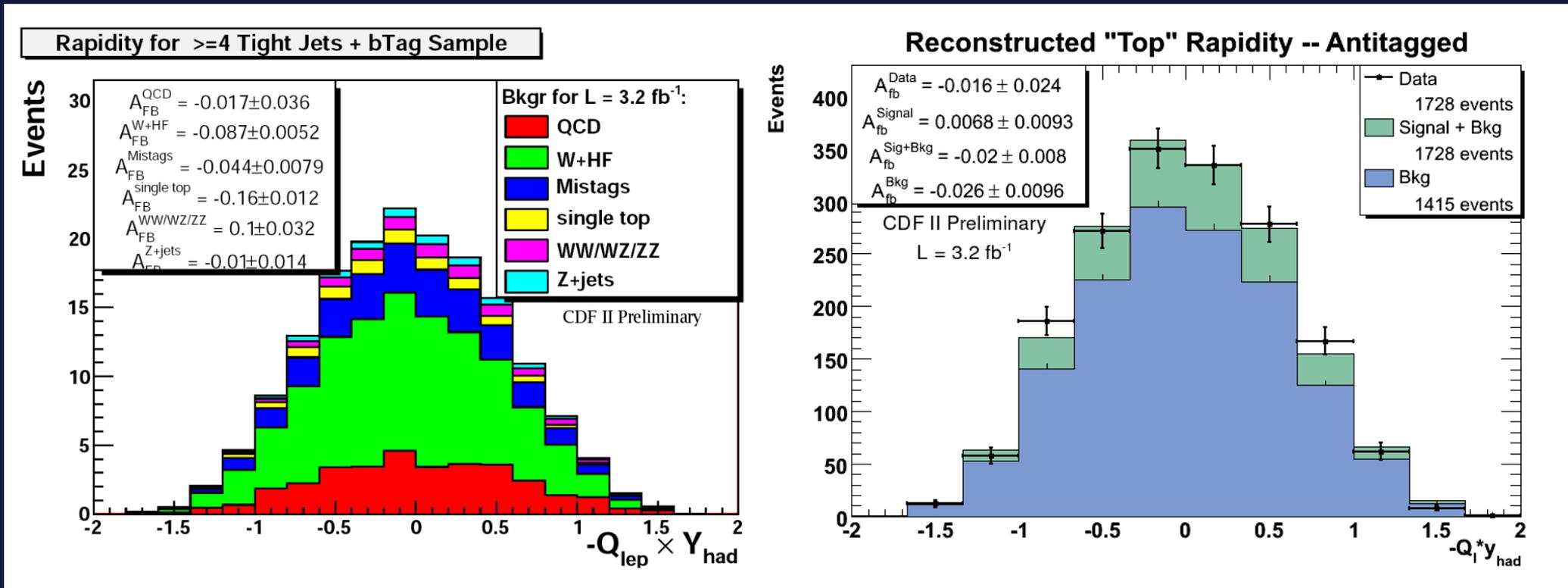
$$\chi^2 = \sum_{lep, jets} \frac{(p_t^{i, meas} - p_t^{i, fit})^2}{\sigma_i^2} + \sum_{j=x,y} \frac{(p_j^{UE, meas} - p_j^{UE, fit})^2}{\sigma_j^2} + \frac{(M_{jj} - M_W)^2}{\Gamma_W^2} + \frac{(M_{lv} - M_W)^2}{\Gamma_W^2} + \frac{(M_{bjj} - M_{top})^2}{\Gamma_t^2} + \frac{(M_{blv} - M_{top})^2}{\Gamma_t^2}$$





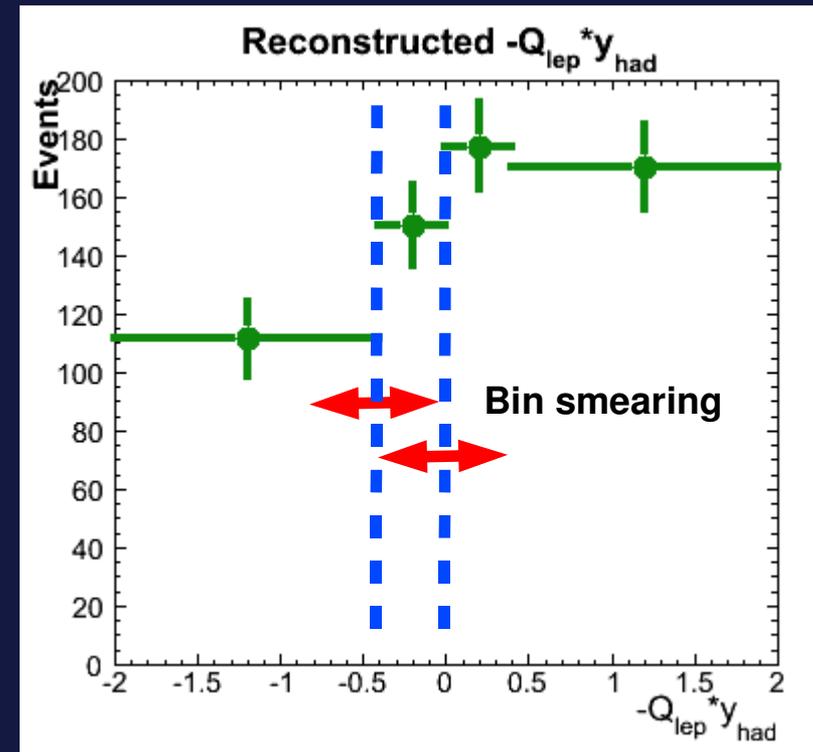
Signal MC is MC@NLO, normalized so signal+background = number of data events

- Background has a known asymmetry that modifies the top  $A_{fb}$  measurement
- We subtract backgrounds from our data
- Check anti-tagged data and MC for consistency and cross-section



- We subtract off this total background from the data shape, 167 events out of 776 data events, which has  $A_{fb} = -0.059 \pm 0.0079$
- Negative values mostly due to electroweak processes (W+HF)

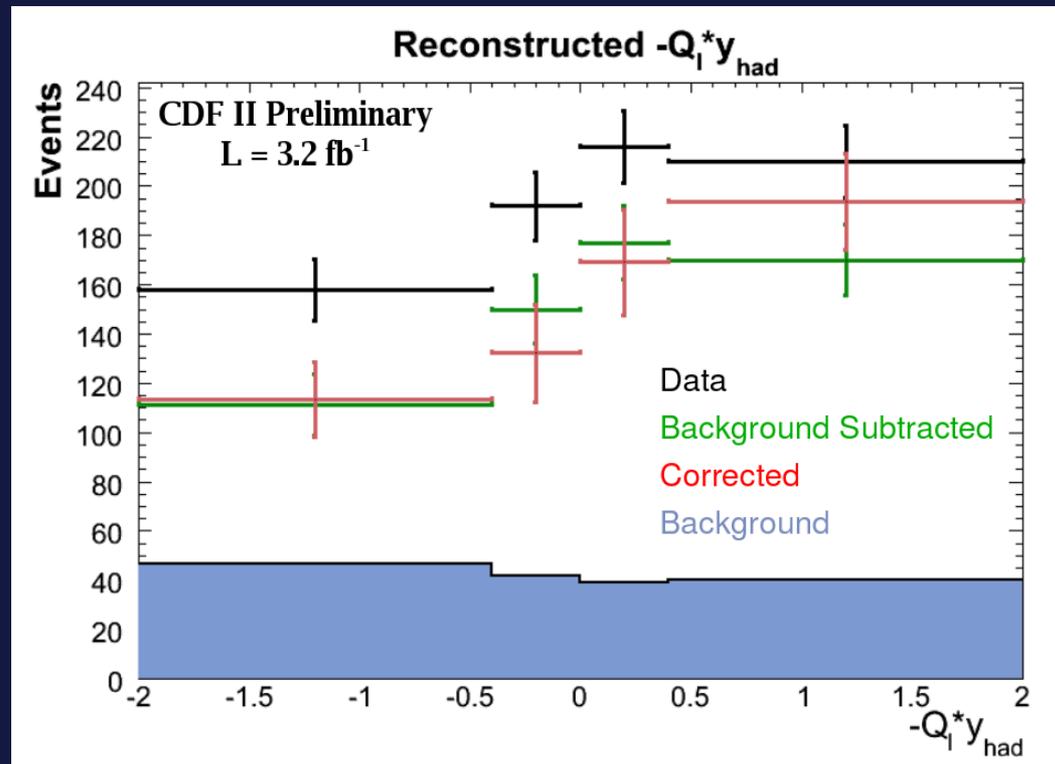
- We optimize for number of bins and bin spacing
- Reconstruction of the event causes smearing between bins. We use a matrix unfolding technique to correct for this effect.
- Acceptance efficiencies also bias our sample, so an analogous correction is made using an acceptance matrix



$$S_{ij} = N_{\text{recon}}^{ij} / N_{\text{truth}}^i$$

$$A_{ij} = N_{\text{sel}}^i / N_{\text{gen}}^i$$

$$N_{\text{corrected}} = A^{-1} \cdot S^{-1} \cdot N_{\text{bkg-sub}}$$



**Raw**

$$A_{fb} = 9.8 \pm 3.6\%$$

**Bkg-sub**

$$A_{fb} = 14.1 \pm 4.6\%$$

**Final Corrected**

$$A_{fb} = 19.3 \pm 6.5\%$$

Vary simulated data by  $\pm\sigma$  and calculate  $A_{fb}$  difference with known sample

	Calc. Uncert.
Background Shape	0.011
Background Size	0.018
ISR/FSR	0.008
JES	0.002
PDF	0.001
MC Generator	0.003
Shape / Unfolding	0.006
Total Uncertainty	0.024

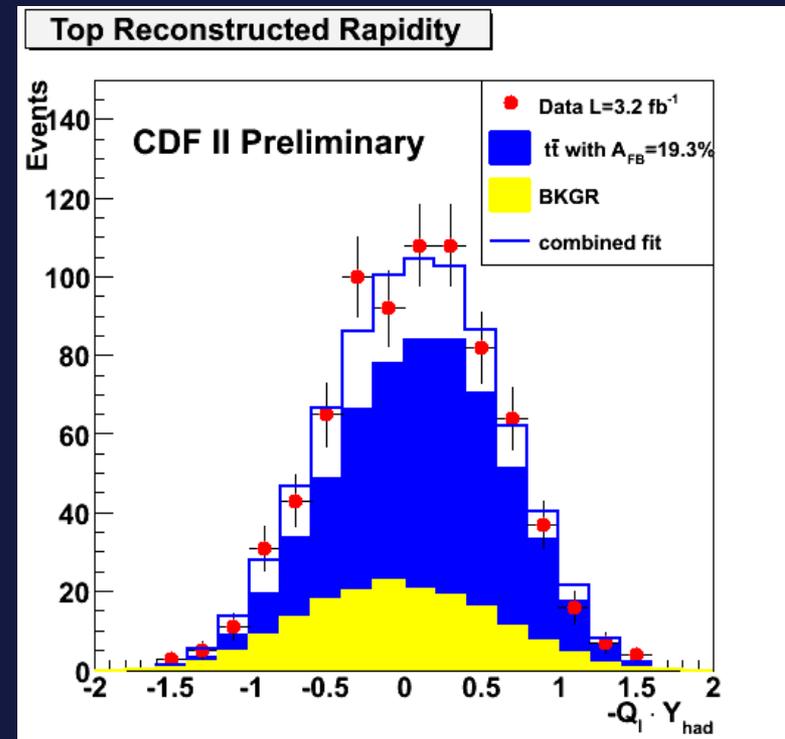
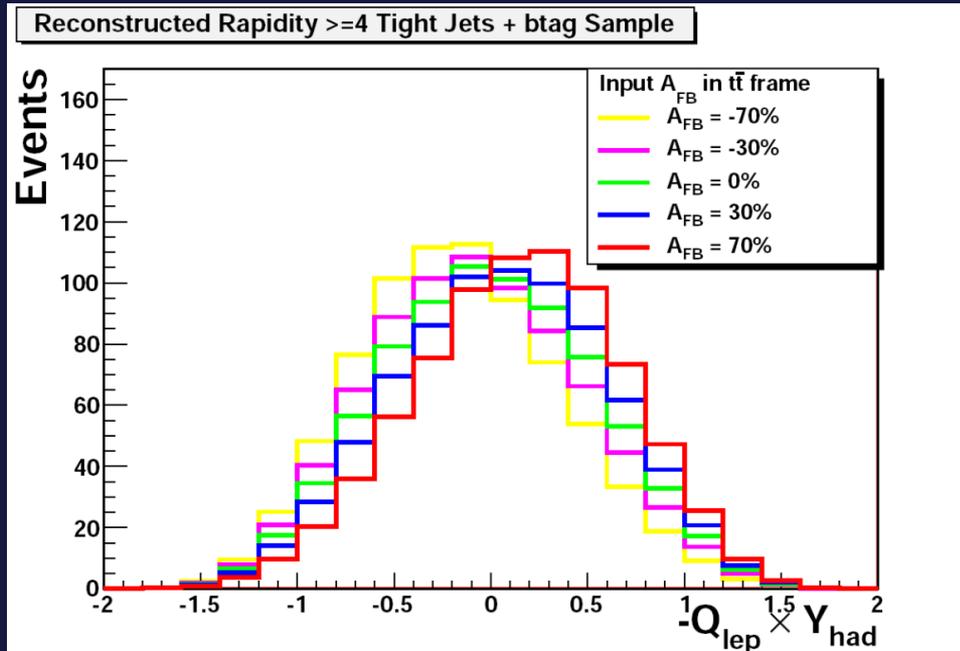
**Final Corrected  $A_{fb} = 19.3 \pm 6.5 \pm 2.4\%$**

Vary simulated data by  $\pm\sigma$  and calculate  $A_{fb}$  difference with known sample

	Calc. Uncert.
Background Shape	0.011
Background Size	0.018
ISR/FSR	0.008
JES	0.002
PDF	0.001
MC Generator	0.003
Shape / Unfolding	0.006
Total Uncertainty	0.024

$$\text{Final Corrected } A_{fb} = 19.3 \pm 6.5 \pm 2.4\%$$

Statistical error dominates total error



The simplest form of an asymmetry is  $1+A \cdot \cos(\theta_{t\bar{t}})$

- Use Pythia MC (initial  $A_{fb}=0$ ) and reweight by  $1+A \cdot \cos(\theta_{t\bar{t}})$  in the rest frame
- Propagate reweights to lab frame and rapidity variable to make a template
- Set up binned likelihood fit to data rapidity distribution using signal (templates) plus background contribution (Gaussian-constrained to background parameters)
- The good fit to the data supports the linear hypothesis

- Previous results ( $1.9 \text{ fb}^{-1}$ ):

$$A_{\text{fb}} \cos(\theta) \text{ method: } A_{\text{fb}}^{\text{lab}} = 17 \pm 8\%$$

- Current results ( $3.2 \text{ fb}^{-1}$ ):

$$A_{\text{fb}}^{-Q^*y_{\text{hadtop}}} \text{ method: } A_{\text{fb}}^{\text{lab}} = 19.3 \pm 6.5 \pm 2.4\%$$

- Are measured values are higher than the 5% SM prediction, but consistent within  $\sim 2$  sigma
- Template technique shows data is consistent with linear hypothesis  $1 + A \cdot \cos(\theta_{\text{tt}})$



# Backup Slides



Process	=4 jets	>=5 Jets	>=4 jets
W+HF Jets	$-0.095 \pm 0.0078$	$-0.078 \pm 0.007$	$-0.087 \pm 0.0052$
Mistags (W+LF)	$-0.038 \pm 0.012$	$-0.05 \pm 0.01$	$-0.044 \pm 0.0079$
Non-W (QCD)	$-0.044 \pm 0.06$	$-0.002 \pm 0.044$	$-0.017 \pm 0.036$
Single Top	$-0.18 \pm 0.016$	$-0.12 \pm 0.018$	$-0.16 \pm 0.012$
WW/WZ/ZZ	$0.078 \pm 0.046$	$0.13 \pm 0.045$	$0.1 \pm 0.032$
Z+Jets	$-0.016 \pm 0.021$	$-0.0041 \pm 0.018$	$-0.01 \pm 0.014$
Total Prediction	$-0.07 \pm 0.012$	$-0.045 \pm 0.012$	$-0.059 \pm 0.0079$

$$S = \begin{bmatrix} 0.76 \pm 0.0096 & 0.13 \pm 0.0041 & 0.035 \pm 0.0022 & 0.011 \pm 0.0012 \\ 0.17 \pm 0.0046 & 0.66 \pm 0.0093 & 0.16 \pm 0.0046 & 0.042 \pm 0.0023 \\ 0.053 \pm 0.0025 & 0.17 \pm 0.0047 & 0.67 \pm 0.0095 & 0.16 \pm 0.0045 \\ 0.017 \pm 0.0014 & 0.042 \pm 0.0023 & 0.13 \pm 0.0042 & 0.79 \pm 0.01 \end{bmatrix}$$

$$A = \begin{bmatrix} 0.981 \pm 0.00483 & 0 & 0 & 0 \\ 0 & 1.09 \pm 0.00555 & 0 & 0 \\ 0 & 0 & 1.05 \pm 0.00547 & 0 \\ 0 & 0 & 0 & 0.901 \pm 0.00464 \end{bmatrix}$$

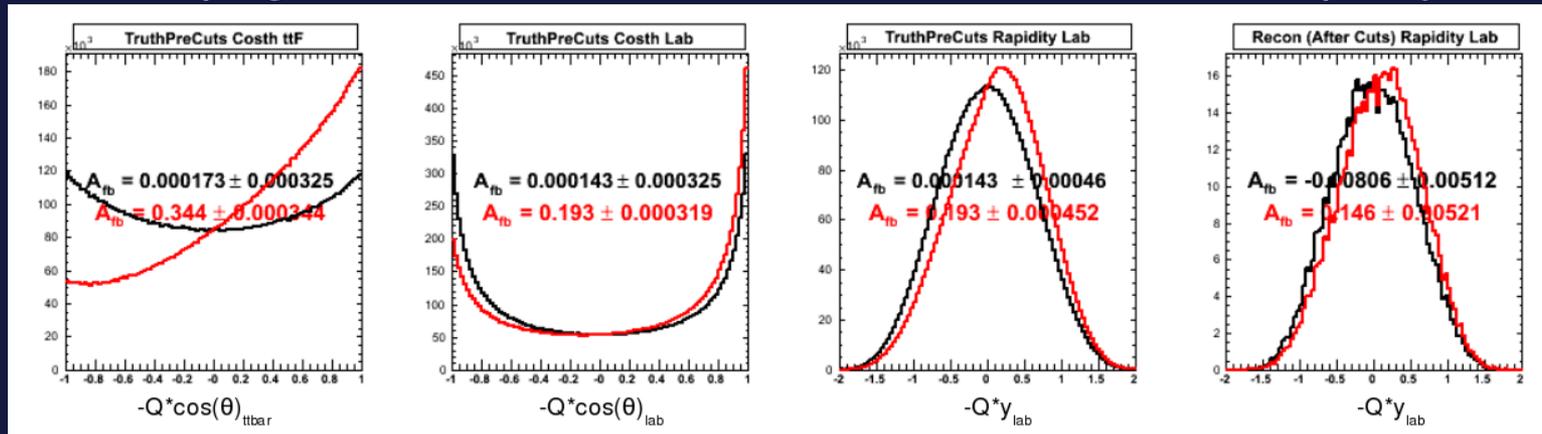
$$(A^{-1} \cdot S^{-1}) = \begin{bmatrix} 1.4 & -0.28 & -0.0061 & -0.0043 \\ -0.33 & 1.6 & -0.35 & -0.0084 \\ -0.016 & -0.38 & 1.6 & -0.29 \\ -0.0095 & -0.018 & -0.28 & 1.5 \end{bmatrix}$$

$$S_{ij} = N_{\text{recon}}^{ij} / N_{\text{truth}}^i$$

$$A_{ii} = N_{\text{sel}}^i / N_{\text{gen}}^i$$

$$N_{\text{corrected}} = A^{-1} \cdot S^{-1} \cdot N_{\text{bkg-sub}}$$

## Propagation of $A_{fb}$ from $t\bar{t}$ frame to lab frame rapidity



- We make control samples with known asymmetry by reweighting Pythia  $\text{Cos}(\theta)$  signal in the  $t\bar{t}$  frame by

$$1 + A \cdot \text{Cos}(\theta_{tt})$$

- Propagate these changes to obtain appropriate factors for reweighting  $Y_{pp}$
- Check corrected measurement vs known  $A_{fb}$  for  $\text{Cos}(\theta_{tt})$  signal

