



1 **Updated Measurement of the Single Top Quark Production Cross**  
2 **Section in the Missing Transverse Energy plus Jets Topology in**  
3  **$p\bar{p}$  Collisions at  $\sqrt{s} = 1.96$  TeV**

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### Abstract

An updated measurement of the electroweak single top quark production cross section is presented using the full CDF data set corresponding to  $9.5 \text{ fb}^{-1}$  of integrated luminosity. The selected data sample is composed of events with an imbalance in the total transverse energy,  $b$ -tagged jets, and no identified leptons ( $\cancel{E}_T b\bar{b}$ ). A combined  $s$ - and  $t$ -channel electroweak single top quark cross section of  $3.53_{-1.16}^{+1.25}$  pb is measured and a lower limit on  $|V_{tb}|$  of 0.63 is obtained at the 95% credibility level. The total uncertainty of this measurement is 40% less than that of the previous CDF measurement, which used one quarter of the full CDF data set. These measurements are combined with previously reported CDF results obtained from events with an imbalance in total transverse momentum,  $b$ -tagged jets, and exactly one identified lepton ( $\ell\nu b\bar{b}$ ). An  $s$ - and  $t$ -channel electroweak single top quark cross section of  $3.02_{-0.48}^{+0.49}$  pb and a lower limit on  $|V_{tb}|$  of 0.84 at the 95% credibility level are obtained for the combination.

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8 The observation of electroweak single top quark production at the Tevatron was a sig-  
9 nificant achievement for the CDF and D0 experiments [1], allowing precise measurements  
10 of the cross section at a hadron collider, and the ability to place an upper limit on the  
11 Cabibbo-Kobayashi-Maskawa (CKM) [2] matrix element magnitude  $|V_{tb}|$  due to the direct  
12 coupling of the  $b$  quark with the singly-produced top quark.

13 The standard model (SM) prediction for the combined  $s$ - and  $t$ -channel electroweak single  
14 top quark production cross section has been calculated to next-to-next-to-leading order:  
15  $\sigma_{\text{SM}}^{s+t} = 3.15 \pm 0.36$  pb [3, 4], excluding the contribution from the  $tW$  production mode, which  
16 is expected to be negligible in this final state [5]. The primary sensitivity to measuring this  
17 quantity is usually obtained from events where the  $W$  from the  $t \rightarrow Wb$  process [6] decays  
18 leptonically to an  $\ell\nu$  lepton pair (where  $\ell$  represents either an electron  $e$  or muon  $\mu$ ) with a  
19 pair of jets, one of which is “ $b$ -tagged” or identified as likely having originated from a bottom  
20 quark. This sample of events (hereafter the “ $\ell\nu b\bar{b}$ ” sample) provides a distinct signature  
21 against backgrounds produced by the strong force (QCD multijet or “MJ” background),  
22 which contain no leptons.

23 A complementary method in measuring the electroweak single top quark cross section is  
24 through events in the final state that contain two or three jets and significant imbalance in the  
25 total transverse energy  $\cancel{E}_T$  [7], which results from the leptonic decay of the  $W$  boson, where  
26 the lepton has not been identified due to reconstruction or acceptance effects. Although MJ  
27 events comprise the dominant background in this final state (hereafter the “ $\cancel{E}_T b\bar{b}$ ” analysis  
28 or sample), the requirement of significant  $\cancel{E}_T$  greatly suppresses the MJ background. In  
29 addition, this search has sensitivity to events where the  $W$  boson decays via  $W^- \rightarrow \tau^- \bar{\nu}_\tau$ ,  
30 and the  $\tau^-$  decays hadronically in the form of a reconstructed jet.

31 The first CDF measurement of electroweak single top quark production in the  $\cancel{E}_T b\bar{b}$  final  
32 state was performed with a dataset corresponding to an integrated luminosity of  $2.1 \text{ fb}^{-1}$  [8].  
33 This article presents a new measurement using the full CDF data set ( $9.5 \text{ fb}^{-1}$ ). All the  
34 techniques developed in the search for  $s$ -channel electroweak single top quark production in  
35 the  $\cancel{E}_T b\bar{b}$  sample [9] are exploited in this update. The strategy for this analysis is described in  
36 Ref. [9]. Important aspects of the analysis methodology are restated here for completeness.  
37 The results of this analysis and those of the most recent  $\ell\nu b\bar{b}$  analysis [10] are then combined  
38 to obtain a more precise measurement of the electroweak single top cross section and to place  
39 a lower limit on the CKM matrix element magnitude  $|V_{tb}|$ .

40 Events are selected in which the calorimeter missing transverse energy  $\cancel{E}_T(\text{cal})$  satisfies  
 41 a minimum online trigger threshold of at least 45 GeV, or 35 GeV when at least two jets  
 42 are present. In the offline analysis, events are accepted in which the reconstructed missing  
 43 transverse energy  $\cancel{E}_T$  is at least 35 GeV. Raw jet energies are corrected to account for  
 44 irregularities in calorimeter response, energy lost outside the jet cone, and underlying event  
 45 dynamics [11]. The jet energy scale and resolution, as well as the  $\cancel{E}_T$  resolution, are further  
 46 improved by incorporating corrections based on track-momentum measurements [12].

47 Each event is required to have at least two leading- $E_T$  jets with transverse energies,  $E_T^{j1}$   
 48 and  $E_T^{j2}$ , that satisfy  $25 < E_T^{j1} < 200$  GeV and  $20 < E_T^{j2} < 120$  GeV, respectively.  
 49 Additionally, both leading- $E_T$  jets are required to be reconstructed within the silicon detector  
 50 acceptance, corresponding to pseudorapidity requirements of  $|\eta| < 2$  for both jets, with one of  
 51 them satisfying  $|\eta| < 0.9$ . Events with three jets are considered if the third-most energetic  
 52 jet satisfies  $15 < E_T^{j3} < 100$  GeV and  $|\eta| < 2.4$ , while event with four or more jets  
 53 are rejected. To discriminate against MJ background, the angular separation between the  
 54 leading- $E_T$  jets must satisfy  $\Delta R > 0.8$ . Events that satisfy these requirements are labeled  
 55 “pre-tagged” events.

56 To suppress light-flavor MJ background, at least one of the leading- $E_T$  jets is required to  
 57 be  $b$ -tagged, which is achieved using the HOBIT algorithm [13]. The HOBIT algorithm assigns  
 58 each jet a value between 0 and 1; jets with a HOBIT value between 0.72 (0.95) and 0.95 (1)  
 59 are considered to be loosely (tightly) tagged. As two  $b$  quarks are present in the electroweak  
 60 single top final state, events are separated into three categories based on how many jets  
 61 are successfully identified as having originated from a  $b$  quark: events with only one tightly  
 62 tagged jet and no other tag (1T), events with two tightly tagged jets (TT), and events with  
 63 one tightly tagged jet and one loosely tagged jet (TL). Events are further classified according  
 64 to the total number of jets, leading to six event subsamples that are analyzed separately to  
 65 enhance sensitivity and to help separate  $s$ -channel electroweak single top quark production,  
 66 enhanced in the double tagging categories, from the  $t$ -channel production, which is enhanced  
 67 in the single tagging categories.

68 All events that satisfy the above kinematic and  $b$ -tagging criteria are separated into two  
 69 samples. Events that contain no identified leptons comprise the preselection sample, which  
 70 includes events in the signal region, which is defined below. Events that contain at least  
 71 one identified charged electron or muon comprise the electroweak sample, which is used to

72 validate the background modeling derived for this analysis.

73 Most physics processes are modeled using Monte Carlo simulation programs. The elec-  
74 troweak single top samples are modeled using the POWHEG generator [14]. Backgrounds  
75 from  $V$ +jets (where  $V$  represents a  $W$  or  $Z$  boson) and  $W + c$  processes are modeled using  
76 ALPGEN [15] with showering simulated by PYTHIA [16]. Events from diboson ( $VV$ ), strongly  
77 produced  $t\bar{t}$  (assuming a top-quark mass of 172.5 GeV), and associated Higgs boson produc-  
78 tion with a  $W$  or  $Z$  boson ( $VH$ ) are simulated using PYTHIA. Two remaining backgrounds  
79 include contributions from events with falsely-tagged jets (“electroweak mistags”) and MJ  
80 events.

81 The electroweak mistag samples are modeled by weighting  $V$ +jets and diboson-simulated  
82 events by mistag probabilities, derived from dedicated data samples [17]. The dominant  
83 background in the  $\cancel{E}_T b\bar{b}$  sample, however, originates from the MJ background. To model this  
84 background, the same data-driven method described in Ref. [18] is used: the MJ background  
85 is derived by weighting each pretagged data event by a tag-rate probability derived from a  
86 MJ-dominated data sample.

87 At this stage of the analysis, placing simple requirements on kinematic event properties is  
88 not sufficient to separate the electroweak single top signal from the background. A series of  
89 multivariate discriminants that take advantage of nontrivial variable correlations are there-  
90 fore employed to optimize suppressing the MJ background and to separate the electroweak  
91 single top signal from the remaining backgrounds.

92 The dominant background in the preselection sample corresponds to that of MJ events.  
93 To discriminate against this background, the same  $\text{NN}_{\text{QCD}}$  multivariate discriminant that  
94 was developed in the  $\cancel{E}_T b\bar{b}$   $s$ -channel electroweak single top search [9] is used. The  $\text{NN}_{\text{QCD}}$   
95 algorithm was trained including several kinematic, angular, and topological variables whose  
96 shapes are different between MJ backgrounds and single top signal.

97 All events that satisfy a minimum  $\text{NN}_{\text{QCD}}$  threshold requirement populate the signal  
98 region, in which the dominant backgrounds are from MJ production,  $V$ +heavy-flavor jets  
99 events, and  $t\bar{t}$  events. Events that do not meet the minimal  $\text{NN}_{\text{QCD}}$  threshold are used  
100 to validate the background prediction with the data. From this validation, multiplicative  
101 correction factors ranging from 0.7 to 0.9 are derived for each of the 1T, TL and TT MJ  
102 predictions. These corrections are applied to the appropriate MJ background normalization  
103 so that the data and the total predicted background normalizations are in agreement.

104 For all events contained in the signal region, two additional discriminants are developed  
 105 that further exploit the differences in kinematic properties between (a) the signal and the  
 106  $V$ +jets background and (b) the signal and  $t\bar{t}$  background processes. The first discriminant  
 107  $\text{NN}_{V\text{jets}}$  is trained using simulated  $t$ -channel electroweak single top quark events for the  
 108 signal sample and MJ-modeled events that satisfy the requirement on  $\text{NN}_{\text{QCD}}$ , for the back-  
 109 ground sample. The second discriminant  $\text{NN}_{t\bar{t}}$ , is trained to separate  $t$ -channel electroweak  
 110 single top quark from  $t\bar{t}$  production, again using simulated  $t$ -channel electroweak single top  
 111 quark events for the signal but simulated  $t\bar{t}$  for the background. The values of these two  
 112 discriminants (both supporting values between 0 and 1) are then combined in quadrature  
 113 resulting in an overall discriminant called  $\text{NN}_{\text{sig}}^t$ , analogous to the strategy adopted to derive  
 114 the final discriminant in the  $\cancel{E}_T b\bar{b}$   $s$ -channel single top search [9].

115 The  $s$ -channel optimized  $\text{NN}_{\text{sig}}$  discriminant as used in the  $\cancel{E}_T b\bar{b}$   $s$ -channel electroweak  
 116 single top search [9] and the  $\text{NN}_{\text{sig}}^t$  discriminant of this analysis are combined to obtain  
 117 an  $\text{NN}_{\text{sig}}^{s+t}$  final discriminant, used to simultaneously separate both  $s$ - and  $t$ -channel signal  
 118 processes from the remaining background. For events with  $\text{NN}_{\text{sig}}$  outputs larger than 0.6,  
 119  $\text{NN}_{\text{sig}}^{s+t}$  is defined to be equal to the  $\text{NN}_{\text{sig}}$  output. For those events that do not satisfy the  
 120 requirement on  $\text{NN}_{\text{sig}}$ ,  $\text{NN}_{\text{sig}}^{s+t}$  is defined as the  $\text{NN}_{\text{sig}}^t$  output multiplied by 0.6. Figure 1  
 121 shows the predicted and observed shapes of  $\text{NN}_{\text{sig}}^{s+t}$  output variable for each of the six event  
 122 subsamples used in this analysis.

123 Several sources of systematic uncertainty are taken into account in this analysis. Uncer-  
 124 tainties on assumed cross section values range from 5%-6% on  $t\bar{t}$ ,  $VV$  (6%),  $VH$  (5%),  $W+c$   
 125 (23%) cross sections [19–22]. Other systematic uncertainties arise from the normalization  
 126 of the  $V$ -plus-heavy-flavor (30%) and of the MJ (3%-7%) background contributions. All  
 127 samples whose normalizations are not constrained according to the data are subject to a  
 128 luminosity uncertainty of 6% [23]. Furthermore, uncertainties are assigned due to the effi-  
 129 ciencies of the lepton vetoes (2%). We also assign a normalization uncertainty of 2% due  
 130 to variations in the assumed parton distribution functions. To account for differences in the  
 131 trigger efficiency in data and simulation, a 2% rate uncertainty is assigned.

132 Possible mismodeling in the  $b$ -tagging efficiency is taken into account by applying scale  
 133 factors to the simulation to correct its  $b$ -tagging efficiency to that of data. The scale factors  
 134 vary depending on the tag category (all are on the order of unity), and the associated uncer-  
 135 tainties range from 8%-16% [13]. Mistag rate uncertainties (20%-30%) are also included [13].

TABLE I: Numbers of predicted and observed events in the two-jet signal region in the subsample with exactly one tightly tagged jet (1T), one tightly and one loosely tagged jet (TL) and two tightly tagged jets (TT). The uncertainties in the predicted numbers of events are due to the theoretical cross section uncertainties and to the uncertainties on signal and background modeling. Both the uncertainties and the central values are those returned by the fit to the data with theory constraints.

Category	1T	TL	TT
$t\bar{t}$	$243 \pm 24$	$85 \pm 9$	$92 \pm 8$
Diboson	$285 \pm 2$	$51 \pm 1$	$37 \pm 1$
$VH$	$17 \pm 1$	$7 \pm 1$	$8 \pm 1$
$V$ +jets	$6528 \pm 2048$	$694 \pm 216$	$220 \pm 69$
MJ	$8322 \pm 180$	$928 \pm 59$	$300 \pm 32$
$t$ -ch single top	$160 \pm 31$	$11 \pm 2$	$9 \pm 12$
$s$ -ch single top	$86 \pm 48$	$42 \pm 23$	$46 \pm 25$
Total prediction	$15557 \pm 2056$	$1733 \pm 224$	$663 \pm 76$
Observed	15312	1743	686

TABLE II: Numbers of predicted and observed events in the three-jet signal region in the subsample with exactly one tightly tagged jet (1T), one tightly and one loosely tagged jet (TL) and two tightly tagged jets (TT). The uncertainties in the predicted numbers of events are due to the theoretical cross section uncertainties and to the uncertainties on signal and background modeling. Both the uncertainties and the central values are those returned by the fit to the data with theory constraints.

Category	1T	TL	TT
$t\bar{t}$	$597 \pm 60$	$117.5 \pm 13$	$110 \pm 10$
Diboson	$108 \pm 1$	$15.7 \pm 0$	$9 \pm 0$
$VH$	$6 \pm 1$	$1.9 \pm 0$	$2 \pm 0$
$V$ +jets	$1610 \pm 505$	$164.5 \pm 51$	$50 \pm 16$
MJ	$1818 \pm 49$	$187.5 \pm 14$	$56 \pm 8$
$t$ -ch single top	$82 \pm 16$	$8 \pm 2$	$7 \pm 1$
$s$ -ch single top	$46 \pm 25$	$15 \pm 8$	$16 \pm 9$
Total prediction	$4220 \pm 511$	$495 \pm 55$	$234 \pm 20$
Observed	4198	490	237

136      Uncertainties in the jet energy scale [11] are included by correlating the uncertainties  
137 in the predicted yields of signals and backgrounds (of the order of 1%-6%) with the corre-  
138 sponding distortions in the predicted kinematic distributions arising from jet energy scale  
139 shifts in all samples except the MJ background, which is entirely data-determined. An addi-  
140 tional shape systematic uncertainty is incorporated for the MJ model, accounting for shape

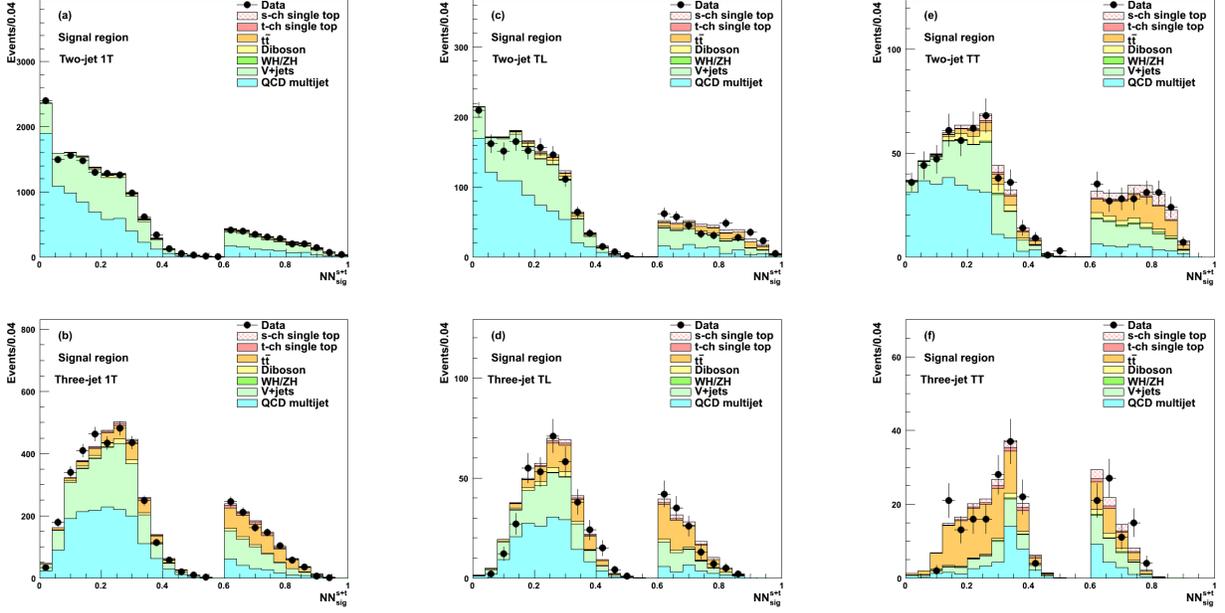


FIG. 1: Predicted and observed  $NN_{\text{sig}}^{s+t}$  distributions in the signal region, for the (a) 1T two-jet, (b) 1T three-jet, (c) TL two-jet, (d) TL three-jet, (e) TT two-jet, (f) and TT three-jet subsamples.

141 variations in the MJ prediction.

142 To measure the electroweak single top production cross section, a combined likelihood  
 143 is formed, which is the product of Poisson probabilities for each bin of the six  $NN_{\text{sig}}^{s+t}$  dis-  
 144 criminants shown in Fig. 1. To account for systematic uncertainties, a Bayesian technique  
 145 is used, in which each independent source of systematic uncertainty is assigned a nuisance  
 146 parameter with a Gaussian prior probability distribution. The impact of each nuisance pa-  
 147 rameter is propagated to the predictions of the signal and background yields in each bin  
 148 of each histogram in the analysis. A non-negative uniform prior probability distribution  
 149 is assumed for the single-top cross section, which is extracted from its posterior probab-  
 150 ility density after integrating over all nuisance parameters. After applying the measurement  
 151 procedure on data, the obtained electroweak single top quark production cross section is  
 152  $3.53_{-1.16}^{+1.25}$  pb, consistent with the SM prediction. The magnitude of  $V_{tb}$  is extracted from the  
 153 posterior probability density by  $|V_{tb}|_{\text{obs}}^2 = |V_{tb}|_{\text{SM}}^2 \sigma_{\text{obs}}^{s+t} / \sigma_{\text{SM}}^{s+t}$  assuming  $|V_{tb}|_{\text{SM}}^2$  is unity and by  
 154 fixing the  $s$ - and  $t$ -channel relative contributions to their SM prediction. Including the theo-  
 155 retical uncertainty of the signal cross section (5.8% for  $s$ -channel, 6.2% for  $t$ -channel) [3] and  
 156 assuming a uniform prior of  $0 < |V_{tb}| < 1$ , the magnitude is measured to be  $|V_{tb}| > 0.63$   
 157 at the 95% credibility level (C.L.).

158 These results are combined with the results of the most recent CDF measurement of  
 159 electroweak single top quark production in the  $\ell\nu b\bar{b}$  sample, performed with  $7.5 \text{ fb}^{-1}$  as  
 160 described in Ref. [10]. In this analysis, candidate events were selected by requiring exactly  
 161 one reconstructed charged lepton ( $e$  or  $\mu$ ) in the final state. Hence, no such events are  
 162 included in the  $\cancel{E}_T b\bar{b}$  analysis described above. Four independent subsamples are formed  
 163 based on the number of  $b$ -tagged jets using the SECVTX algorithm, and also the total  
 164 number of jets: two jets and one  $b$ -tag, two jets and two  $b$ -tags, three jets and one  $b$ -tag,  
 165 or three jets and two  $b$ -tags. Events were also divided into independent categories based on  
 166 different lepton reconstruction algorithms. To further discriminate the signal from all other  
 167 backgrounds, multivariate discriminants (NNs) were employed. These NNs were optimized  
 168 separately for each of the four event subsamples. Correlated systematic errors were treated  
 169 as described above for the  $\cancel{E}_T b\bar{b}$  analysis. Finally, a Bayesian binned-likelihood technique  
 170 was applied to the final NN output to extract an electroweak single top quark cross section  
 171 of  $3.04_{-0.53}^{+0.57}$  pb, assuming a top-quark mass of  $172.5 \text{ GeV}/c^2$ . The magnitude of  $V_{tb}$  was  
 172 estimated following the same prescription described above and constrained to be  $|V_{tb}| > 0.86$   
 173 at the 95% C.L.

174 The results of the two analyses are combined by taking the product of their likelihoods  
 175 and simultaneously varying the correlated uncertainties, following the procedure explained  
 176 above. The uncertainties associated with the theoretical cross sections of the  $t\bar{t}$ ,  $VV$ , and  $VH$   
 177 production processes, and those associated with the luminosity are taken as fully correlated  
 178 between the two analyses. The combined measurement results in an electroweak single top  
 179 quark production cross section of  $3.02_{-0.48}^{+0.49}$  pb, consistent with the SM prediction. The  $s$ -  
 180 and  $t$ -channel cross sections are also extracted separately by constraining the other opposite-  
 181 channel cross section to the SM prediction. The result is shown in Fig. 2a. From the posterior  
 182 probability density on  $|V_{tb}|^2$ , shown in Fig. 2b, a 95% C.L. lower limit of  $|V_{tb}| > 0.84$  is  
 183 obtained.

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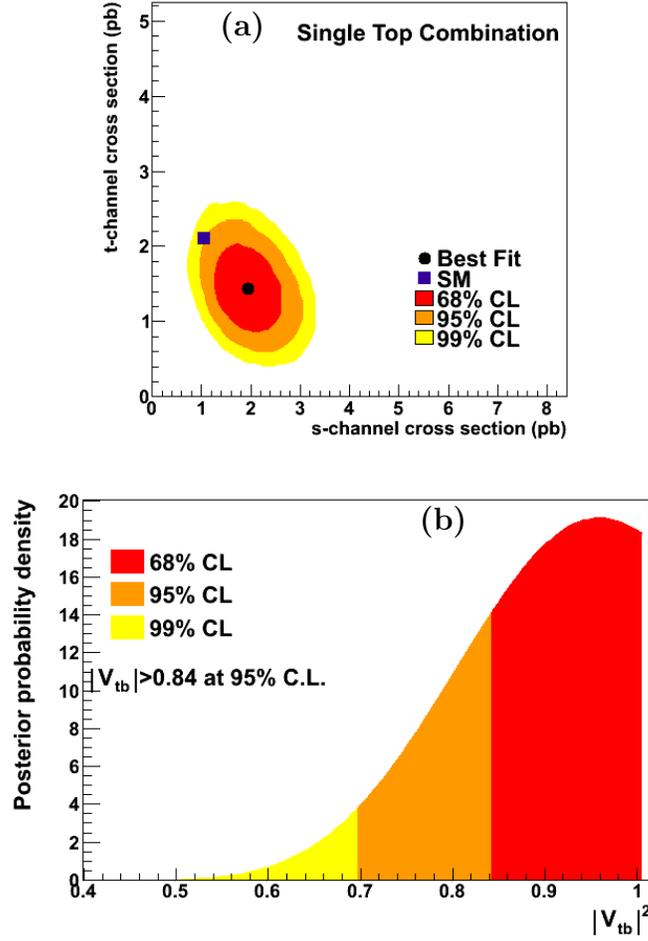


FIG. 2: CDF single-top combinations of the (a) two-dimensional posterior density of the measured  $s$ -vs.- $t$ -channel cross sections, normalized to the SM predictions, and (b) the posterior probability density on  $|V_{tb}|^2$ , assuming the SM prediction for the relative contributions between the  $s$ - and  $t$ -channel processes.

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205 towers,  $\vec{E}_T(\text{cal}) = -\sum_i E_T^i \hat{n}_i$ , where  $i$  is a calorimeter tower number with  $|\eta| < 3.6$ ,  $\hat{n}_i$   
206 is a unit vector perpendicular to the beam axis and pointing at the  $i$ th calorimeter tower.  
207 The reconstructed missing transverse energy,  $\vec{E}_T$ , is derived by subtracting from  $\vec{E}_T(\text{cal})$   
208 components of the event not registered by the calorimeter, such as jet energy adjustments.  
209  $E_T$  [ $E_T(\text{cal})$ ] is the scalar magnitude of  $\vec{E}_T$  [ $\vec{E}_T(\text{cal})$ ].
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