

The Forward Backward Asymmetry in Top Production

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*On behalf of the CDF and D0
Collaborations at the Tevatron*

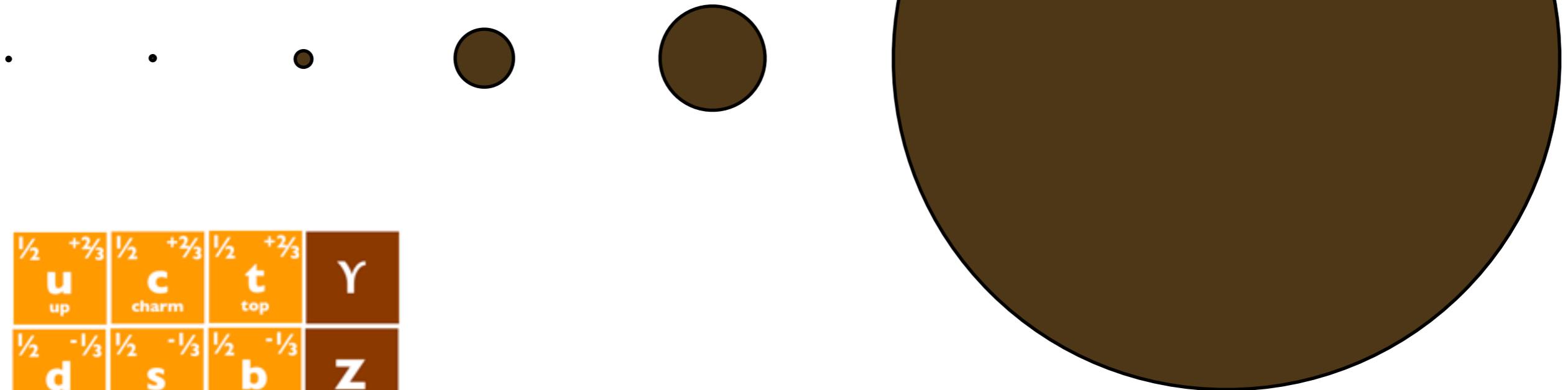
FPCP 2011

Kibbutz Maale Hachamisha, Israel

top

173 GeV

up **down** **strange** **charm** **bottom**
3 MeV 7 MeV 110 MeV 1.3 GeV 4.3 GeV



$\frac{1}{2}$ $+\frac{2}{3}$ u up	$\frac{1}{2}$ $+\frac{2}{3}$ c charm	$\frac{1}{2}$ $+\frac{2}{3}$ t top	Y
$\frac{1}{2}$ $-\frac{1}{3}$ d down	$\frac{1}{2}$ $-\frac{1}{3}$ s strange	$\frac{1}{2}$ $-\frac{1}{3}$ b bottom	Z
ν_e	ν_μ	ν_τ	W
e	μ	τ	g

Area \propto Mass

Coupling to Higgs

Top Mass

$$y_t = \sqrt{2} \cdot \frac{m_t}{v}$$

Higgs Vacuum Expectation

Average Energy in the Higgs Field

Coupling to Higgs

173 GeV

$$y_t = \sqrt{2} \cdot \frac{m_t}{v}$$

243 GeV

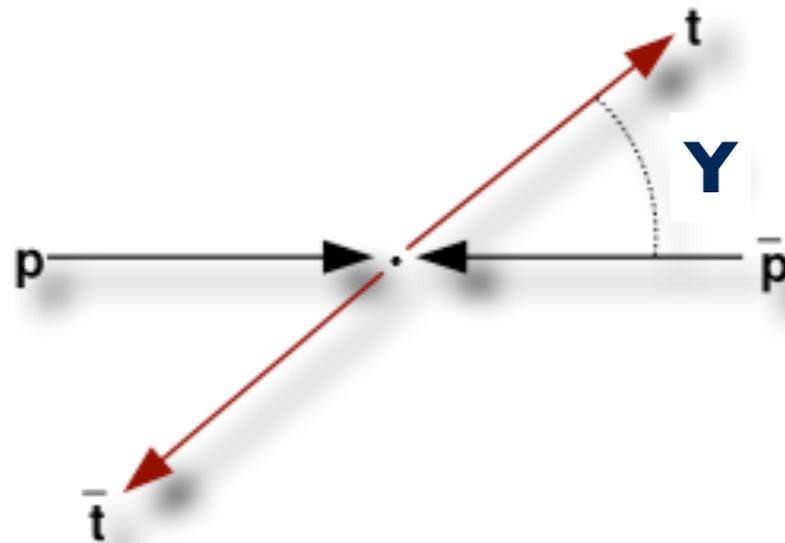
Coupling to Higgs

173 GeV

$$y_t = \sqrt{2} \cdot \frac{m_t}{v} \approx 1.0$$

243 GeV

Top Quark Forward Backward Asymmetry

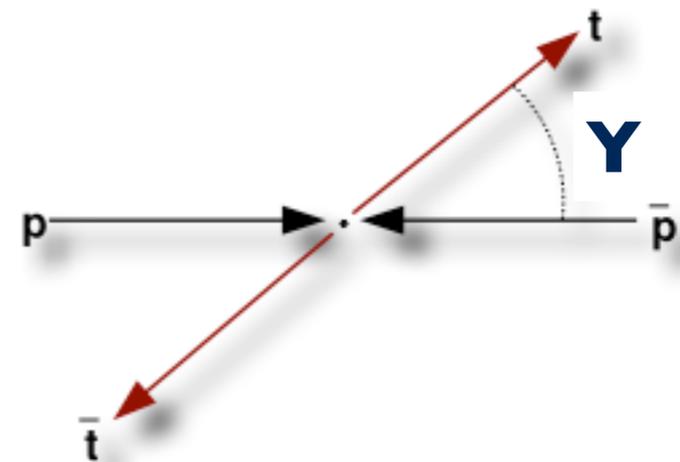


$$A_{\text{FB}} = \frac{F - B}{F + B}$$

Why Measure It?

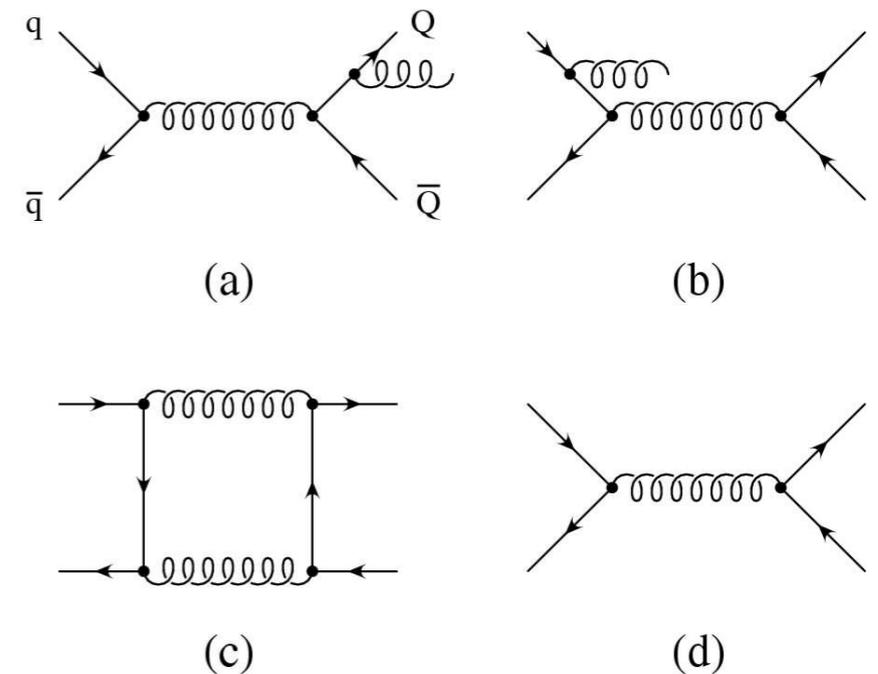
- **Test of discrete symmetries of the strong interaction**
- **NLO QCD predicts small (~6%) asymmetry from $q\bar{q} \rightarrow t\bar{t}$**
- **New physics can show up: Big Gluons with axial vector coupling**

$$A_{\text{FB}} = \frac{N_{Y>0} - N_{Y<0}}{N_{Y>0} + N_{Y<0}}$$



Why Measure It?

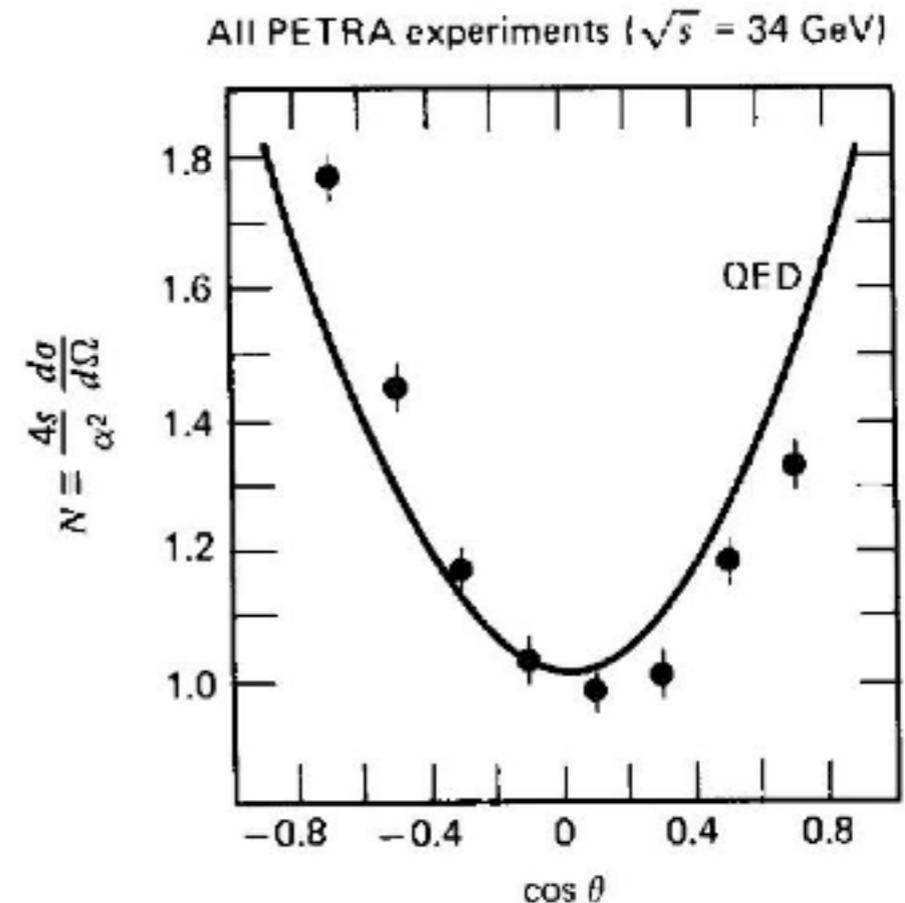
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**Kuhn, Rodrigo
PRL 81,89 (1998)**

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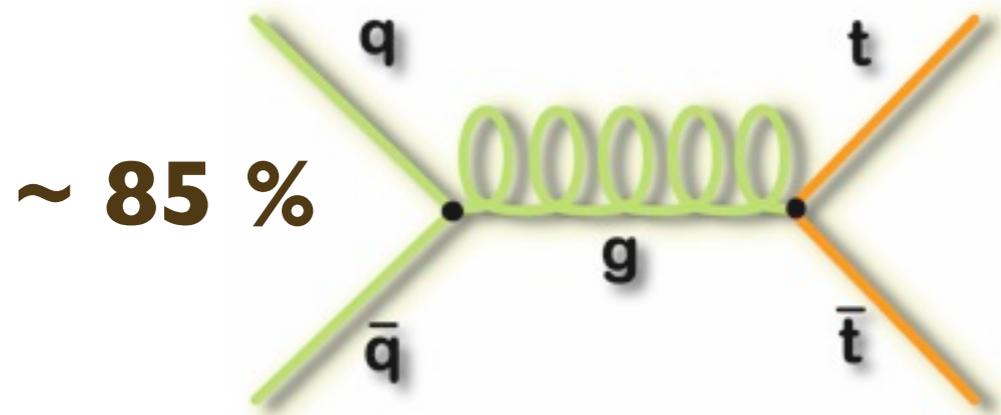


Method

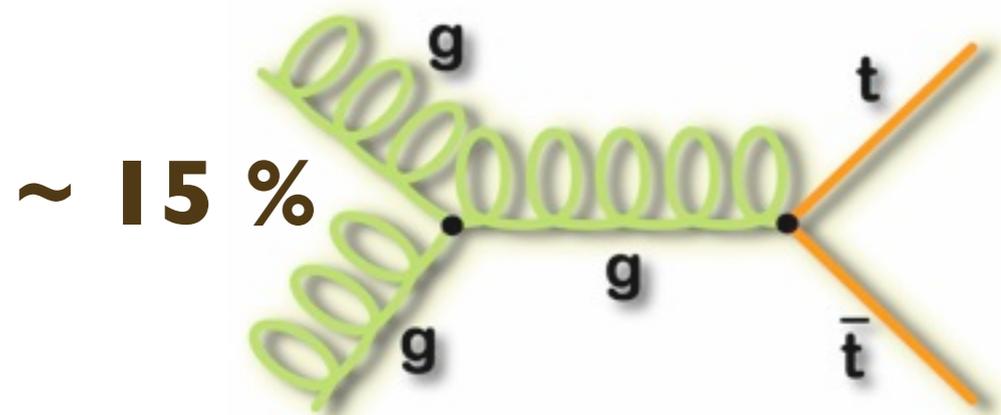
- **Extract $t\bar{t}$ events from data collected at CDF**
- **Reconstruct the production angle of top in these events**
- **Correct for any distortion from the detector, background processes, and the method of reconstructing the angle**
- **Measure A_{FB}**

Production & Decay

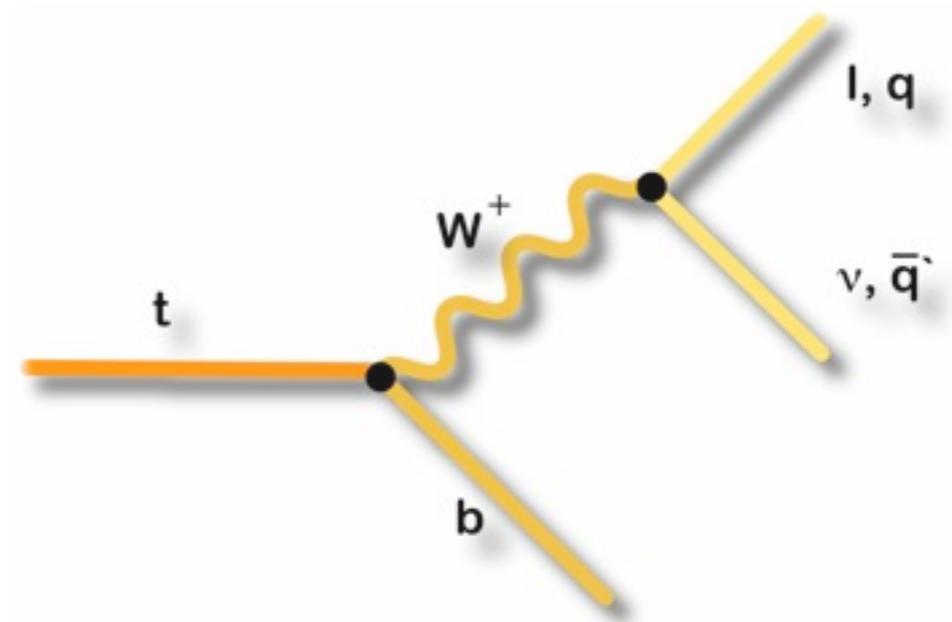
Production



$$\sigma_{tt}^{\text{SM}} = 7.5 \text{ pb}$$

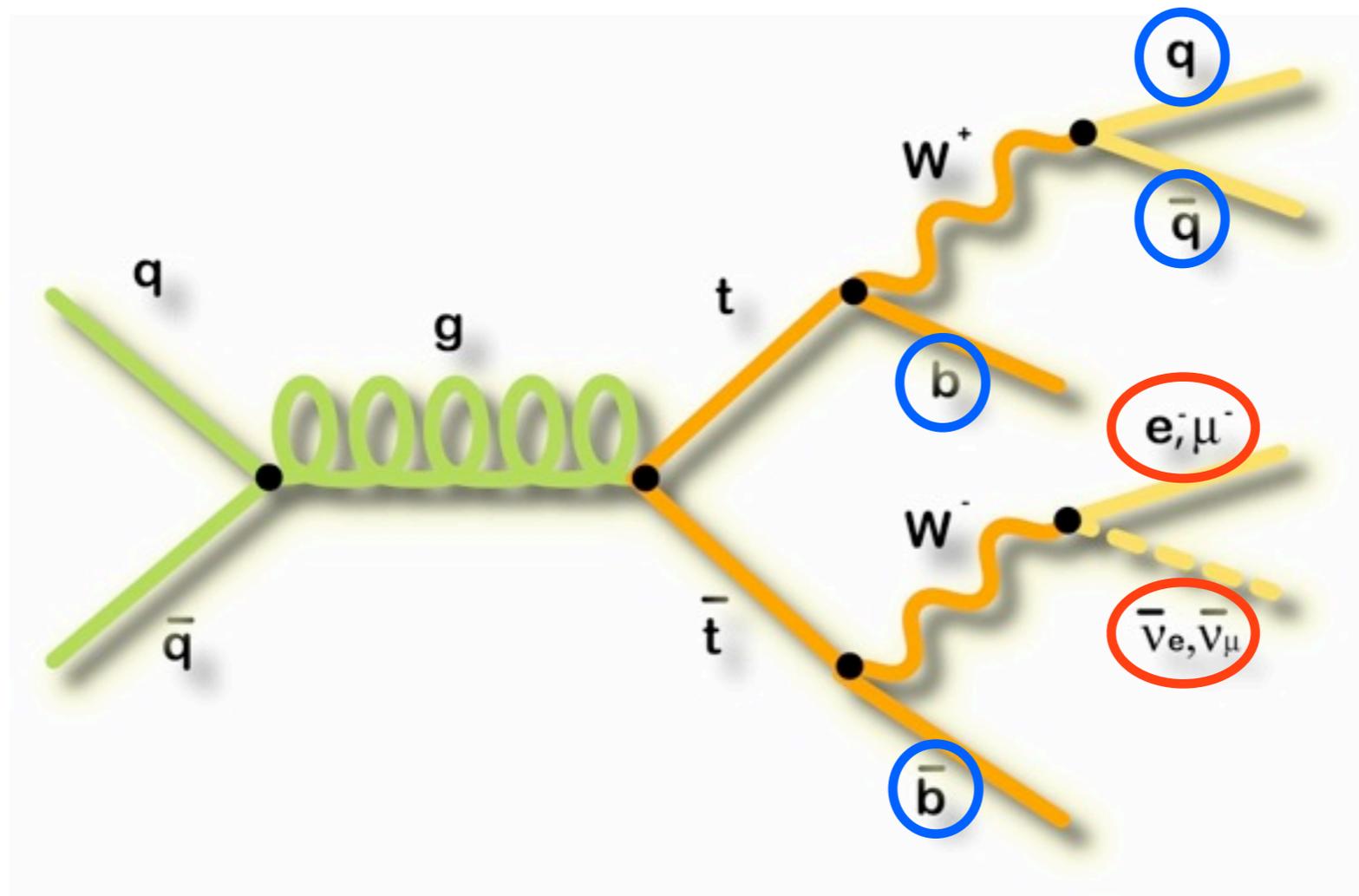


Decay



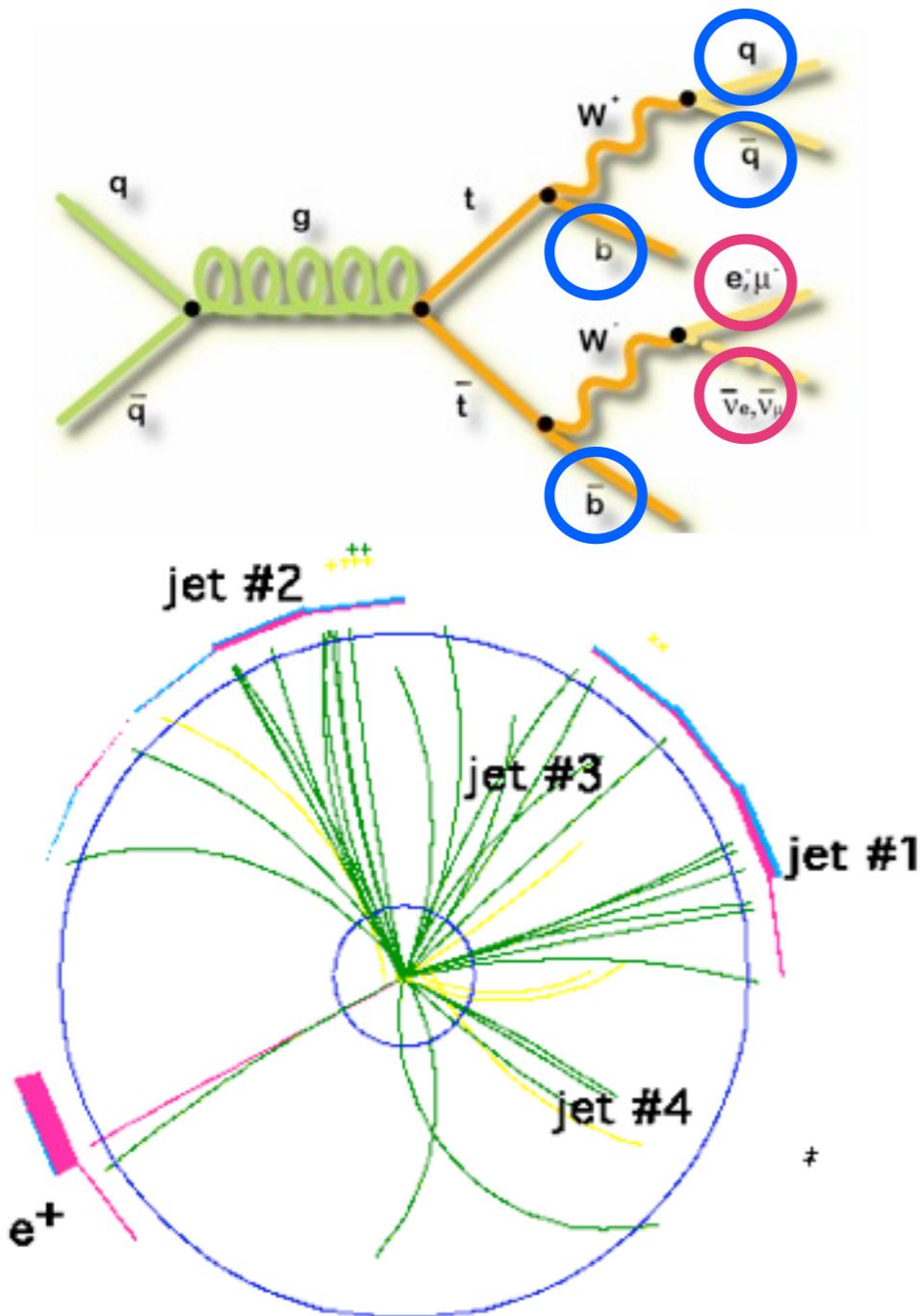
~ 100 %

Production & Decay



One Lepton, One Neutrino, and 4 Quarks

Finding Top



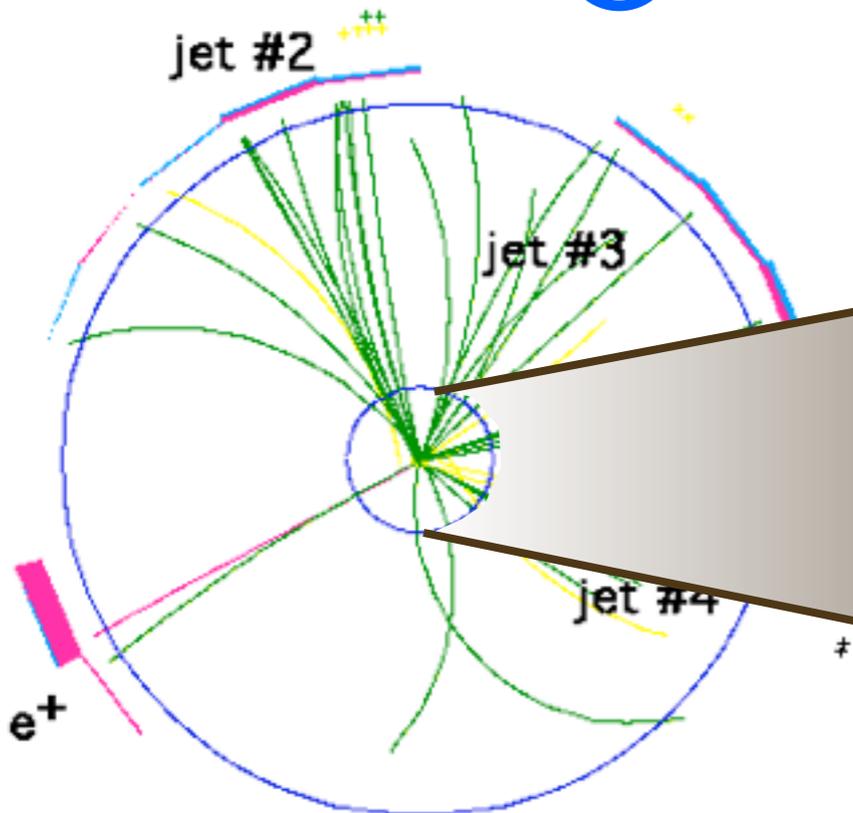
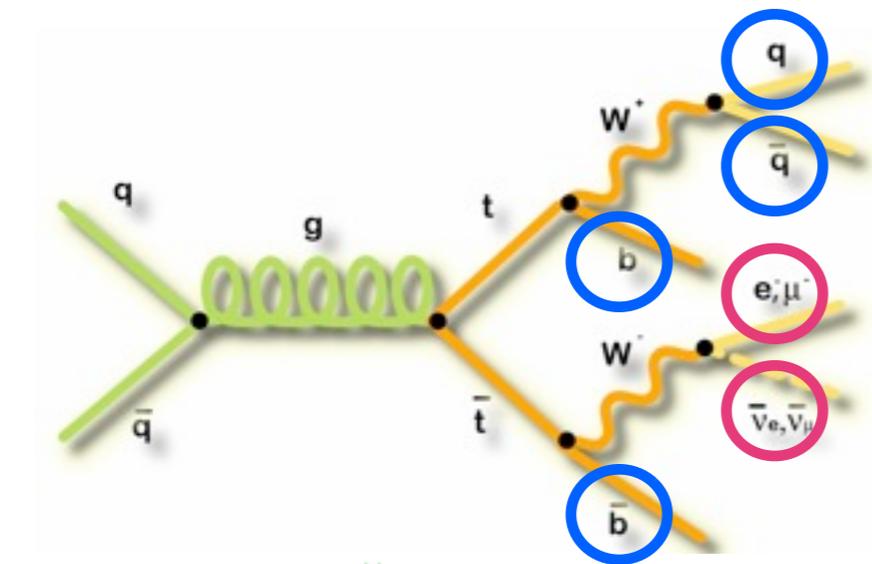
1 Electron or Muon ($E_T \geq 20 \text{ GeV}$, $|\eta| < 1.1$)

Large “Missing” Energy ($E_T \geq 20 \text{ GeV}$)

≥ 4 Jets ($E_T \geq 20 \text{ GeV}$, $|\eta| < 2.0$)

At least 1 Jet with displaced secondary vertex (Evidence of a ‘b’-jet)

Finding Top

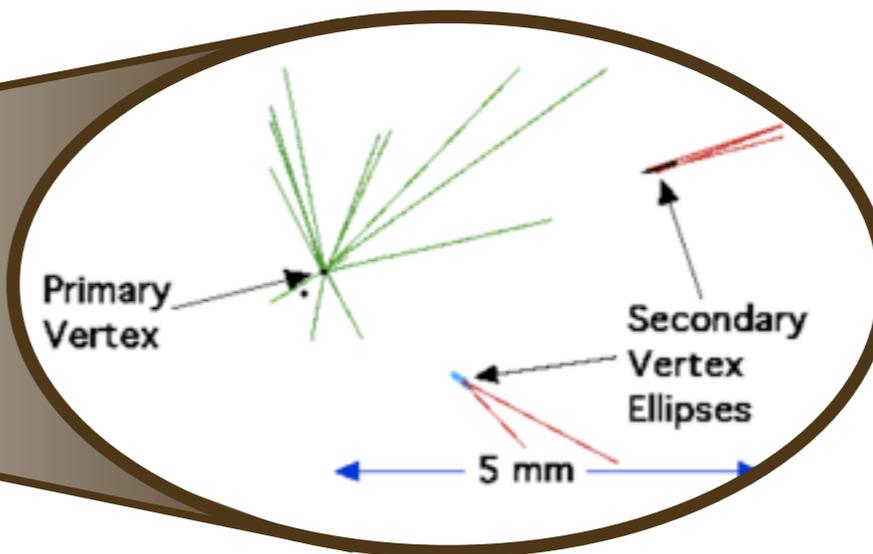


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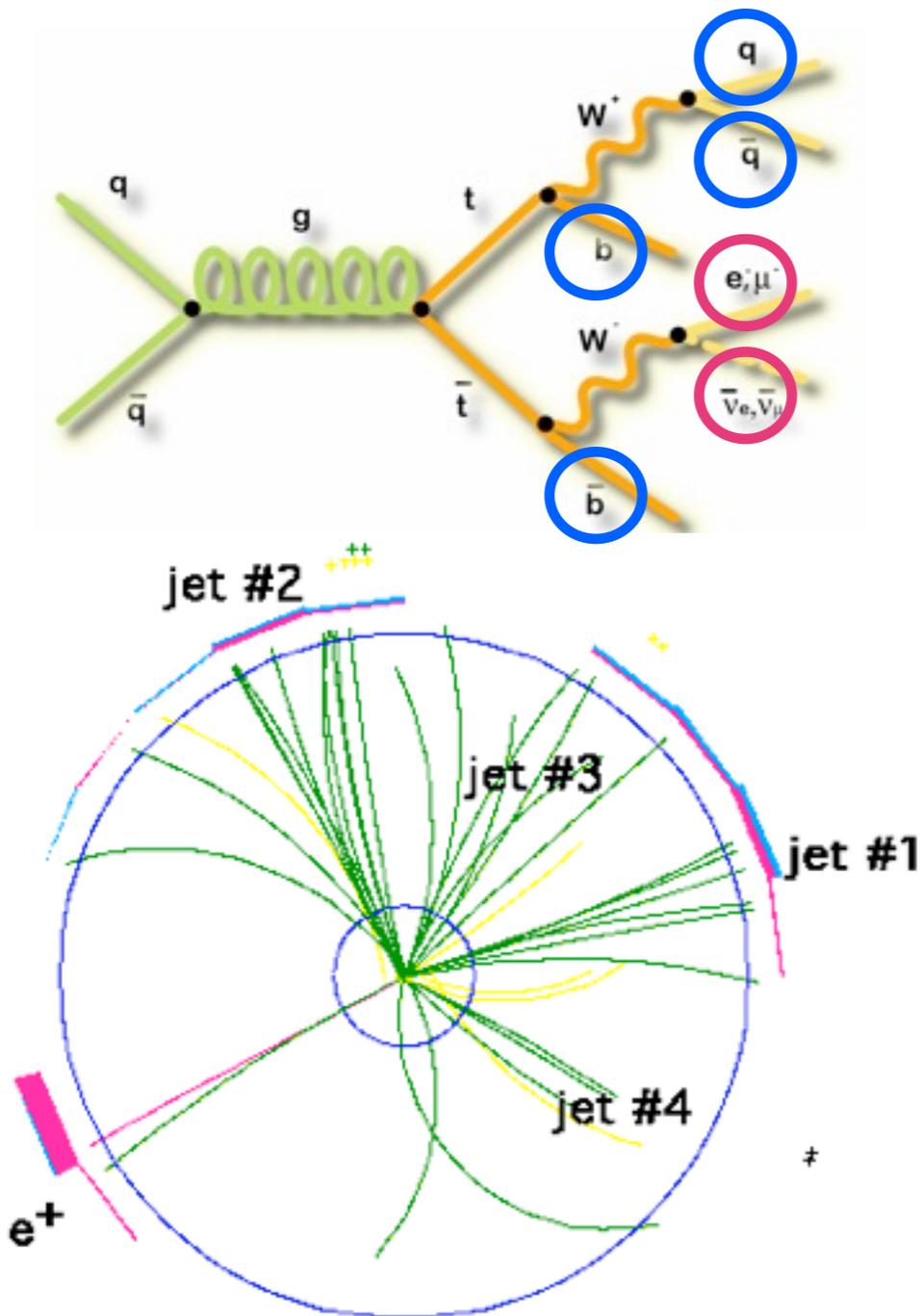
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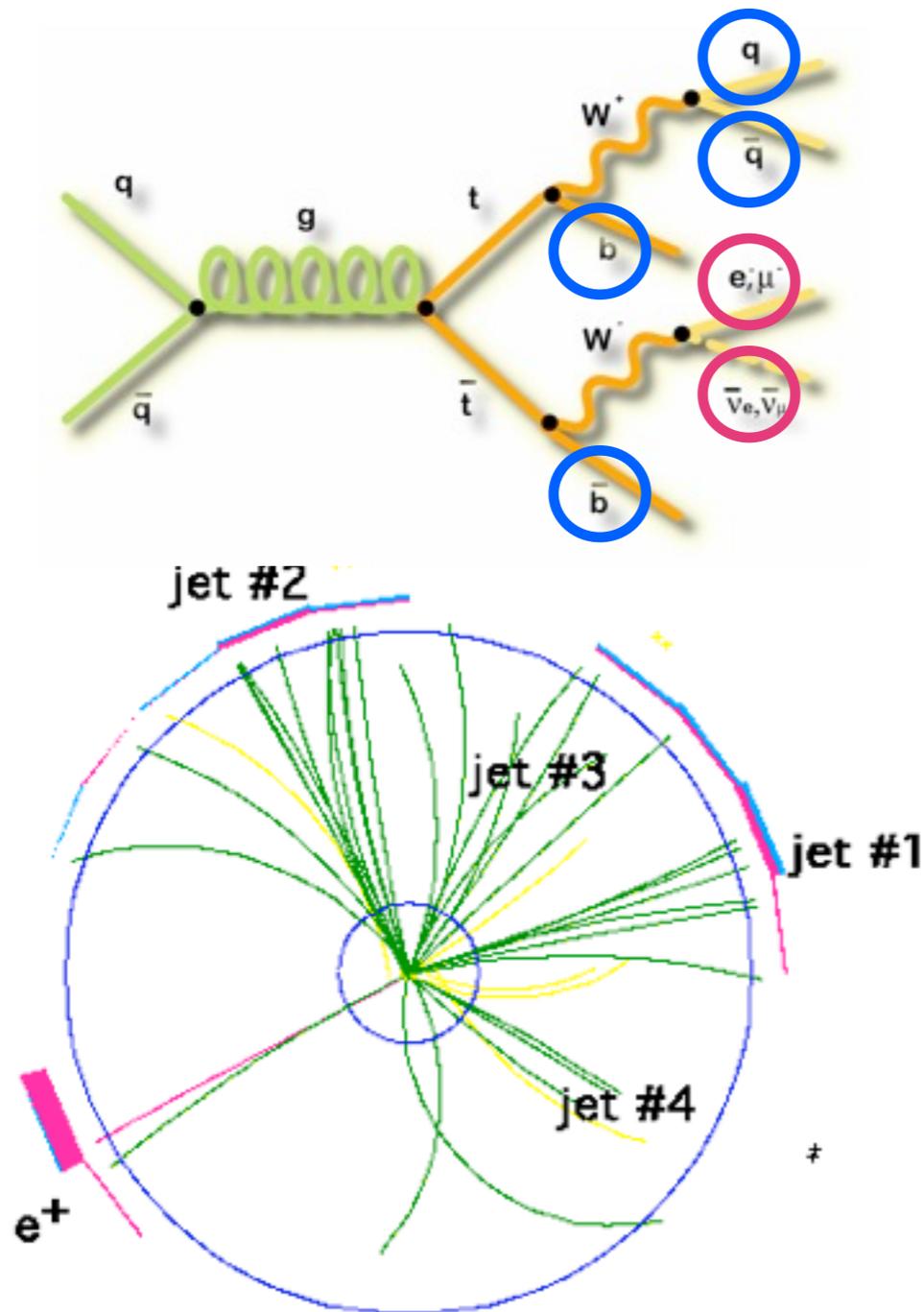
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At least 1 Jet with displaced secondary vertex (Evidence of a 'b'-jet)

**1300 Events (5.3 fb^{-1})
20 % Background**

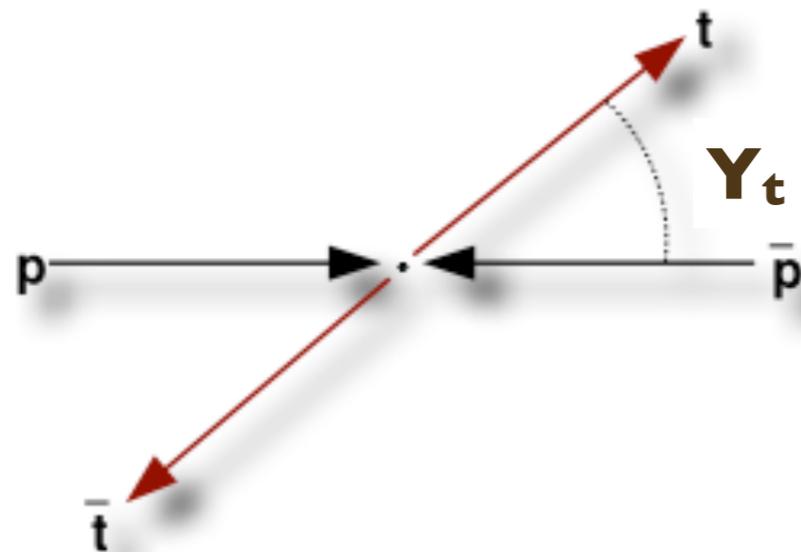
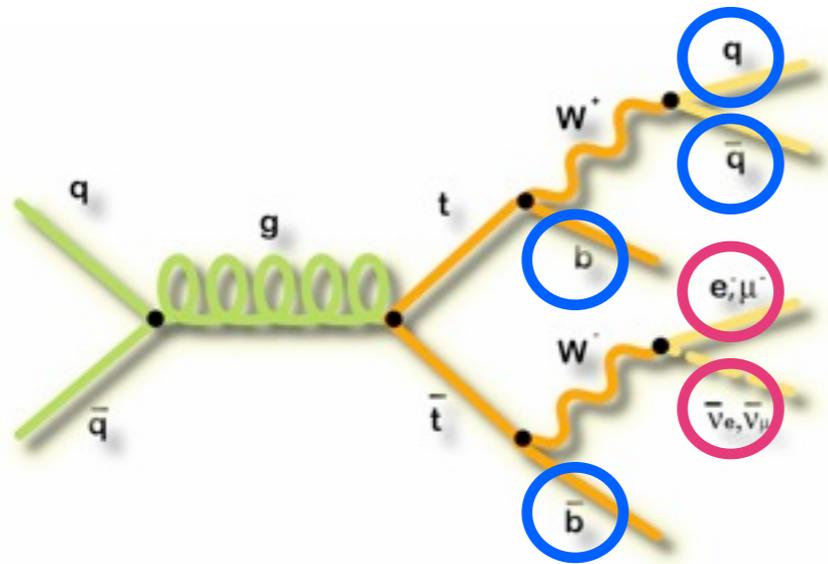
Reconstructing the Top Direction



- **Reconstruct the top direction from the observables in the detector**
- **Algorithm used to match jets to partons \rightarrow just add 4-vectors to get top direction**
- **We use the rapidity difference (ΔY) of $t \rightarrow l\nu b$ and $t \rightarrow jjb$, which is proportional to Y_t in $t\bar{t}$ frame**

$$Y_t \propto Q_{\text{lepton}} \cdot \Delta Y$$

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$$Y_t \propto Q_{\text{lepton}} \cdot \Delta Y$$

Measurement

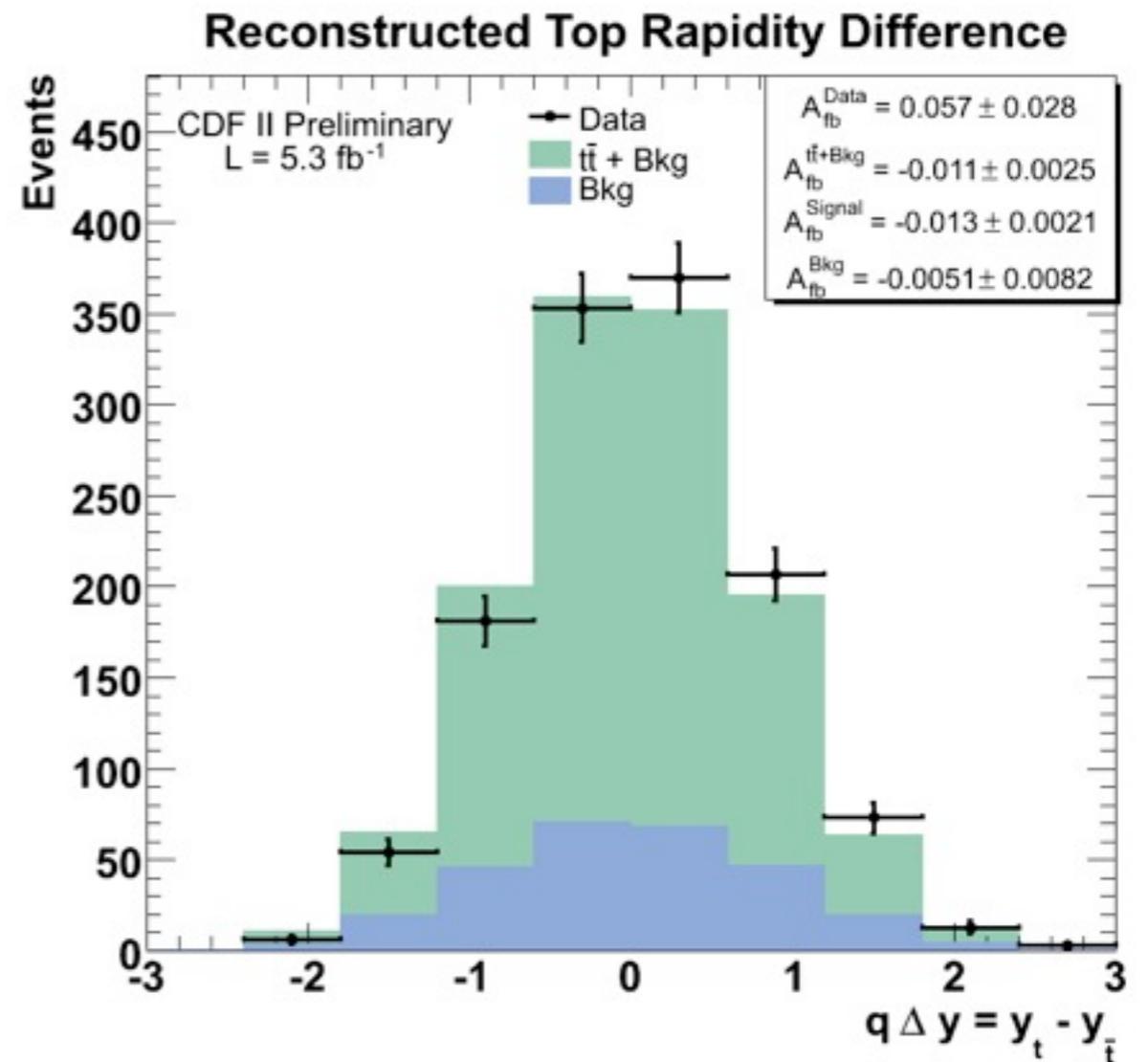
$$A_{FB} = 16 \pm 7_{\text{stat}} \pm 2_{\text{syst}} \%$$

5.3 fb^{-1}

Directly comparable to SM

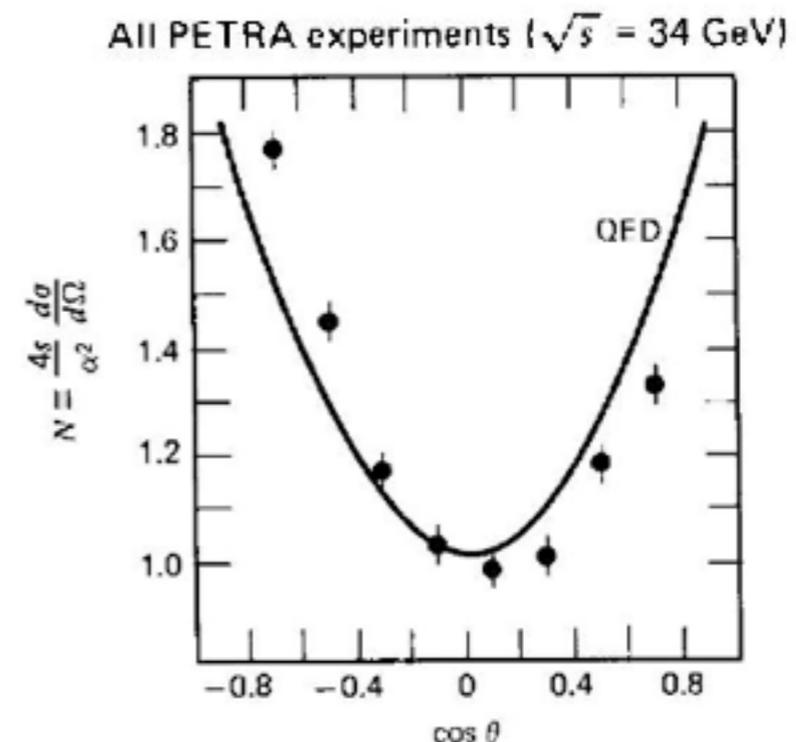
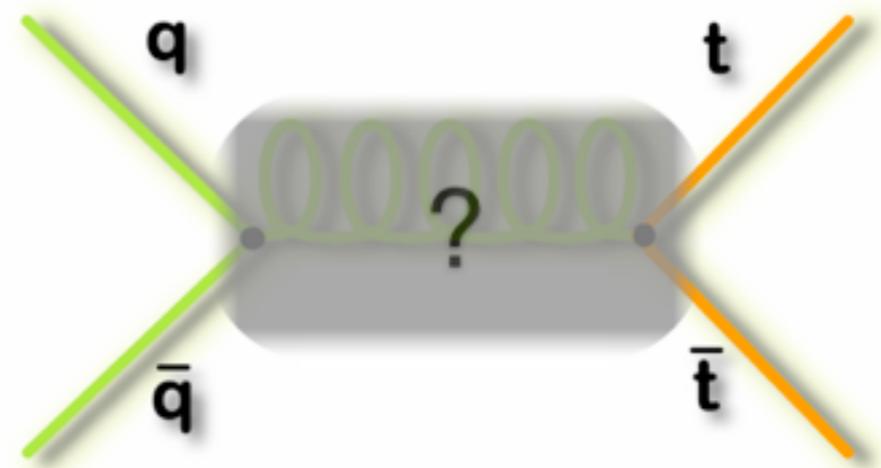
$$A_{FB}^{\text{Theory}} = 6 \pm 1 \%$$

Kuhn, Rodrigo PRL 81,89 (1998)

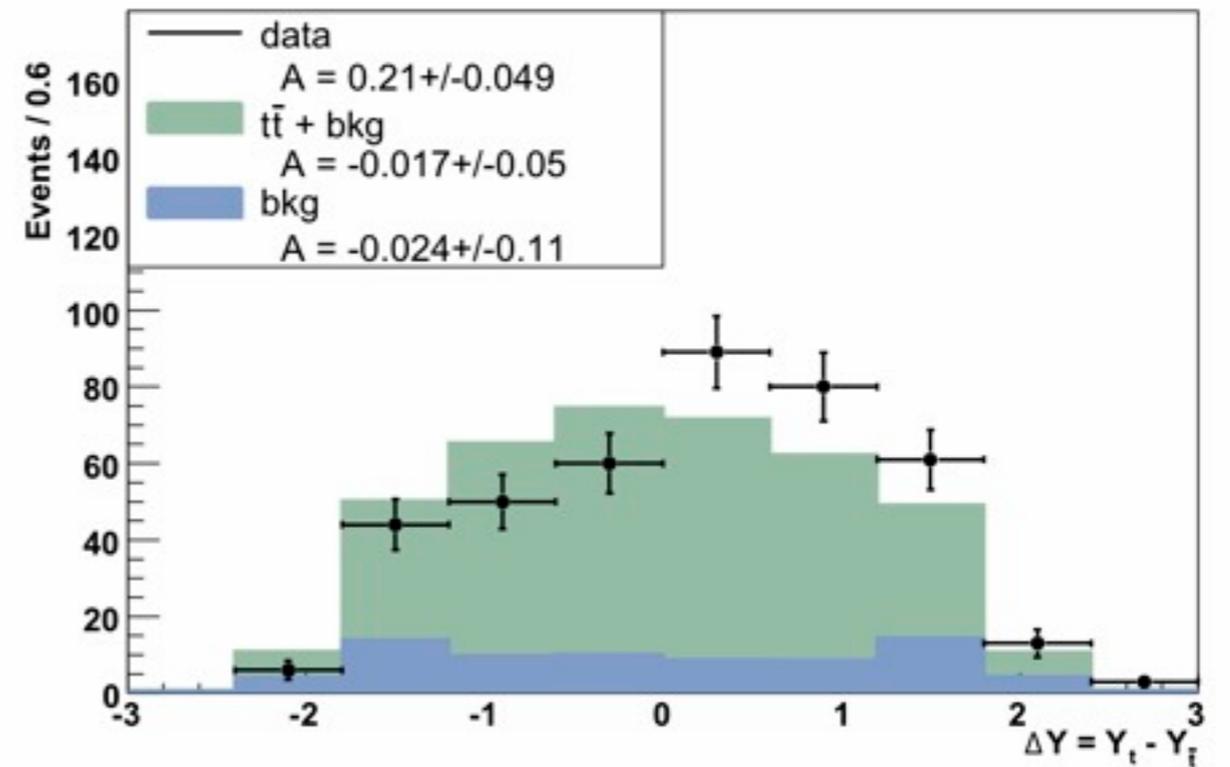
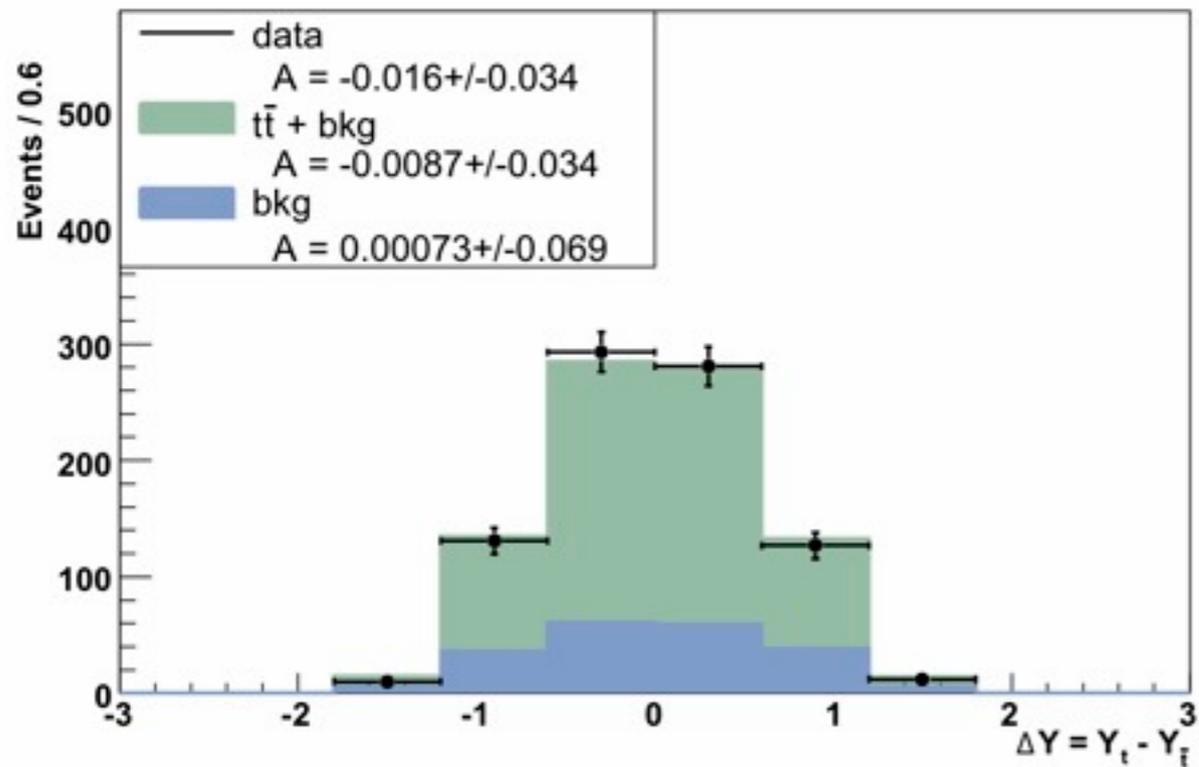


$M_{t\bar{t}}$ Dependence

- A_{FB} could increase at higher energy due to new production mechanisms
- Study the asymmetry vs. the mass of the $t\bar{t}$ system ($M_{t\bar{t}}$)
- Simply divide sample into high/low $M_{t\bar{t}}$
- Use 450 GeV \rightarrow based on MC studies



$M_{t\bar{t}}$ Dependence



	Inclusive	$M < 450 \text{ GeV}$	$M > 450 \text{ GeV}$
Data	$5.7 \pm 2.8 \%$	$-1 \pm 3 \%$	$21 \pm 5 \%$
SM MC	$2 \pm 0.4 \%$	$1 \pm 0.6 \%$	$3 \pm 0.7 \%$

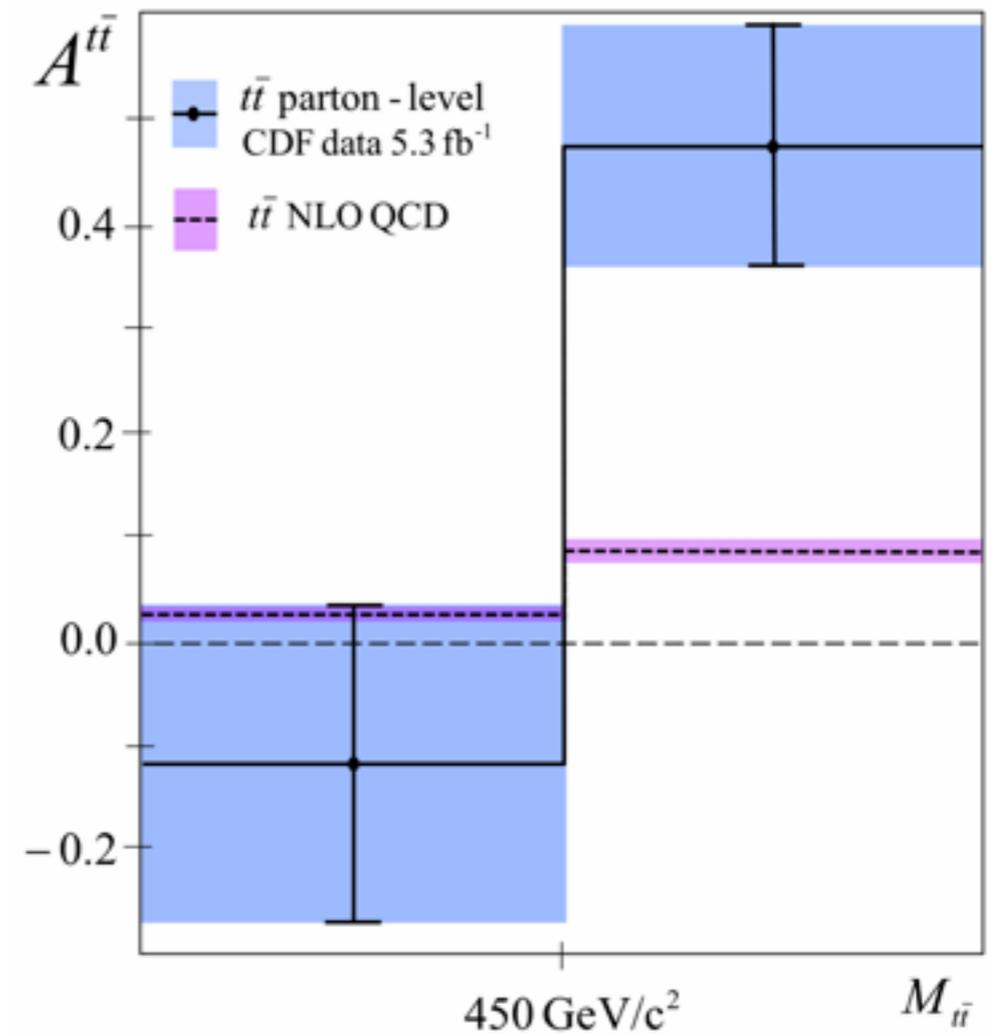
$M_{t\bar{t}}$ Dependence

- **Unfold $M_{t\bar{t}}$ dependence back to parton level**

$$A_{\text{FB}} = 48 \pm 11_{\text{stat+syst}} \%$$

5.3 fb⁻¹

$$A_{\text{FB}}^{\text{Theory}} = 9 \pm 1 \%$$

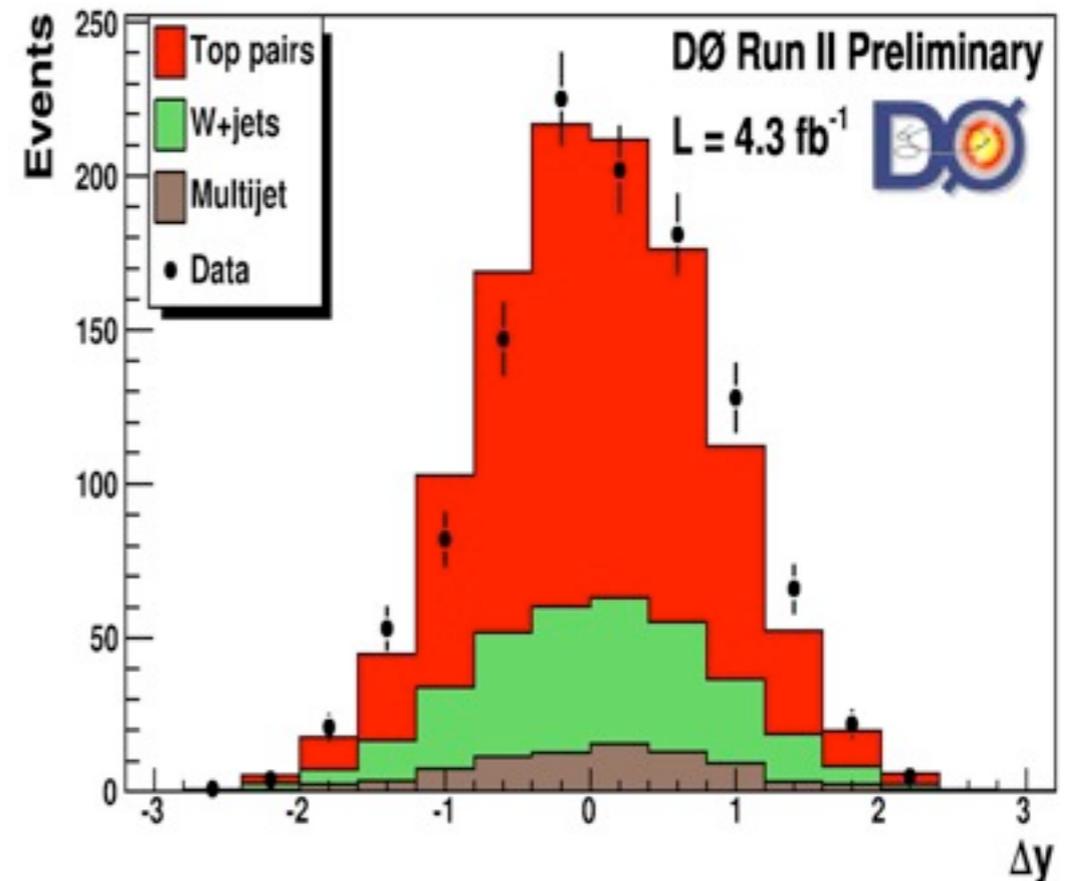


Other Signs?

-  collaboration has also performed this measurement
-  compares the result to the SM as seen by the detector (only corrects for backgrounds)

$$A_{\text{FB}}^{\text{data-bkg}} = 8 \pm 4_{\text{stat+sys}} \%$$

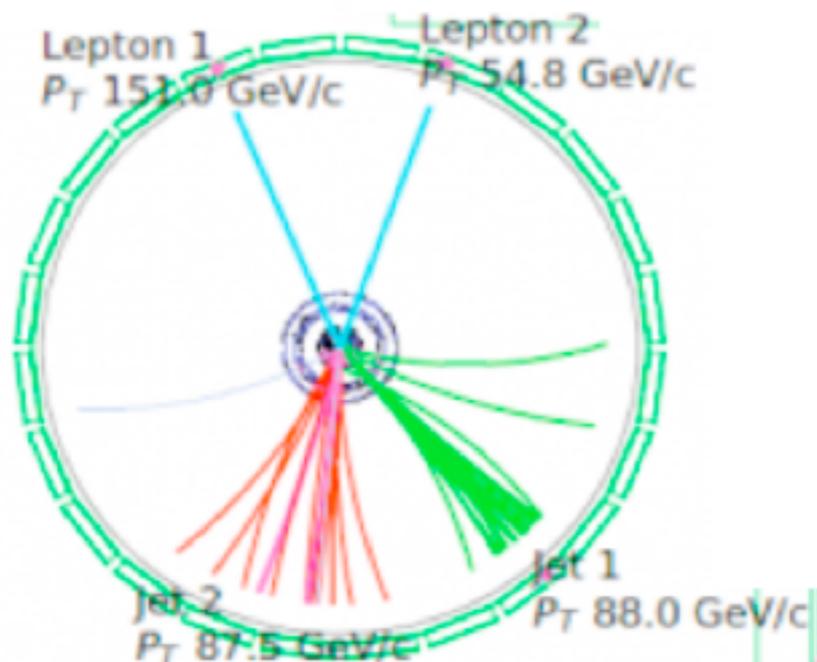
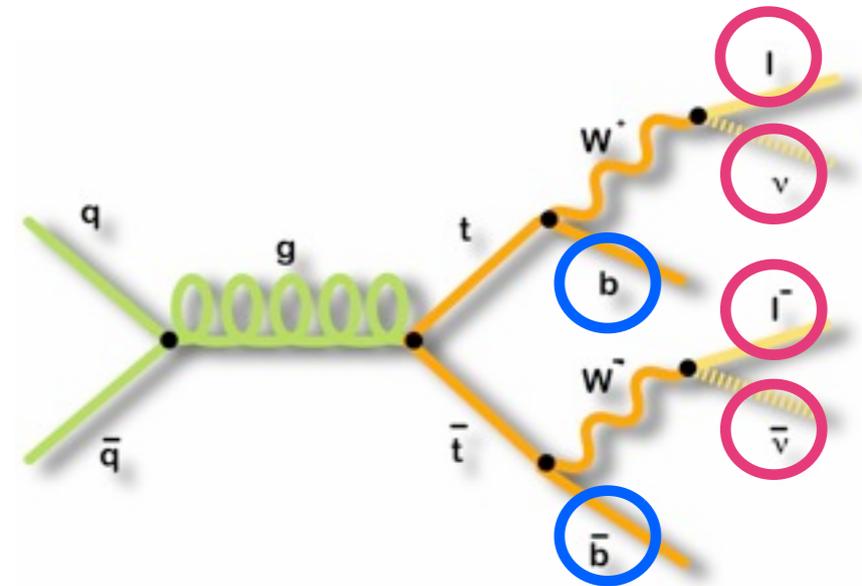
$$A_{\text{FB}}^{\text{mc@nlo}} = 1^{+2.0}_{-1.0} \%$$



$$A_{\text{FB}}^{\text{CDF}} = 7.5 \pm 3.7 \%$$

A_{FB} in Dileptons

- **Alternative channel to previous measurement in single lepton+jets events**
- **Independent events using different reconstruction algorithm**



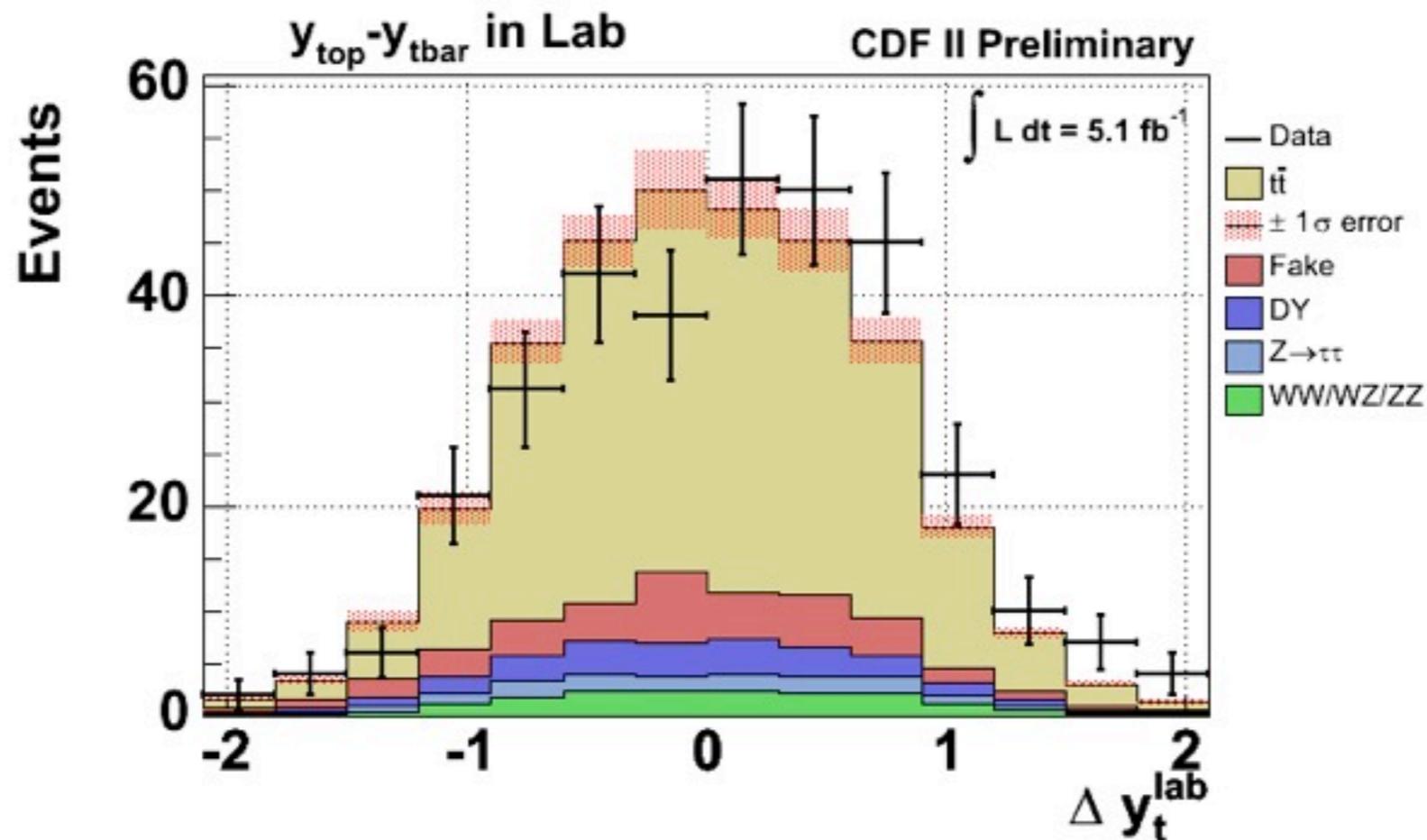
2 Leptons ($E_T \geq 20 \text{ GeV}$, $|\eta| < 1.1$)

Large “Missing” Energy ($E_T \geq 50 \text{ GeV}$)

≥ 2 Jets ($E_T \geq 15 \text{ GeV}$, $|\eta| < 2.5$)

ΣE_T (jets, leptons) $> 200 \text{ GeV}$

A_{FB} in Dileptons



$$A_{\text{FB}} = 42 \pm 15_{\text{stat}} \pm 5_{\text{syst}} \%$$

5.1 fb⁻¹

$$A_{\text{FB}}^{\text{Theory}} = 6 \pm 1 \%$$

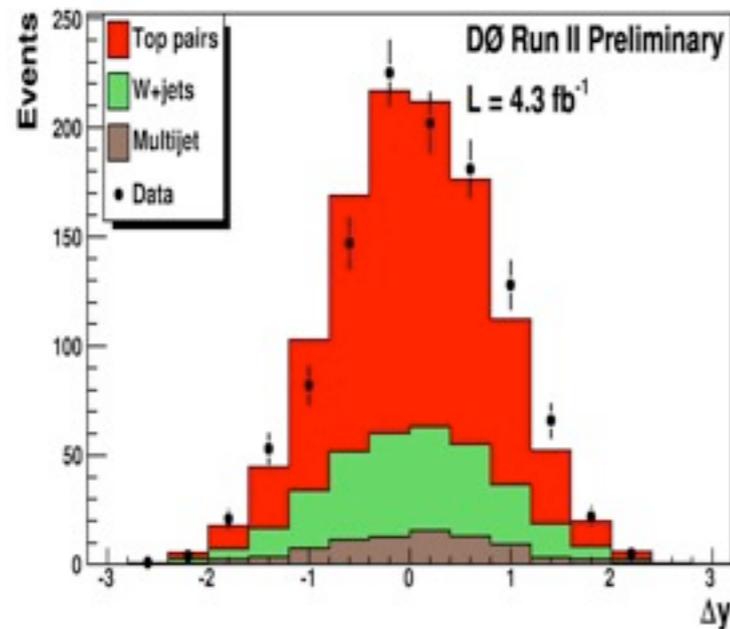
$$A_{\text{FB}}^{\text{l+Jets}} = 16 \pm 7 \%$$

Summary of Results

Inclusive Asymmetry

$$A_{FB} = 8 \pm 4 \%$$

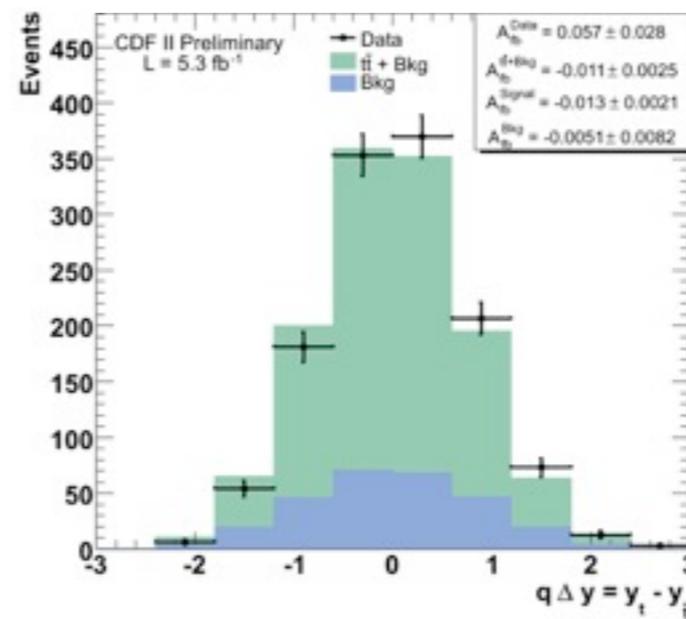
$$\sim 2 \sigma \quad (4 \text{ fb}^{-1})$$



$$A_{FB}^{sm} \sim 1 \%$$

$$A_{FB} = 16 \pm 7 \%$$

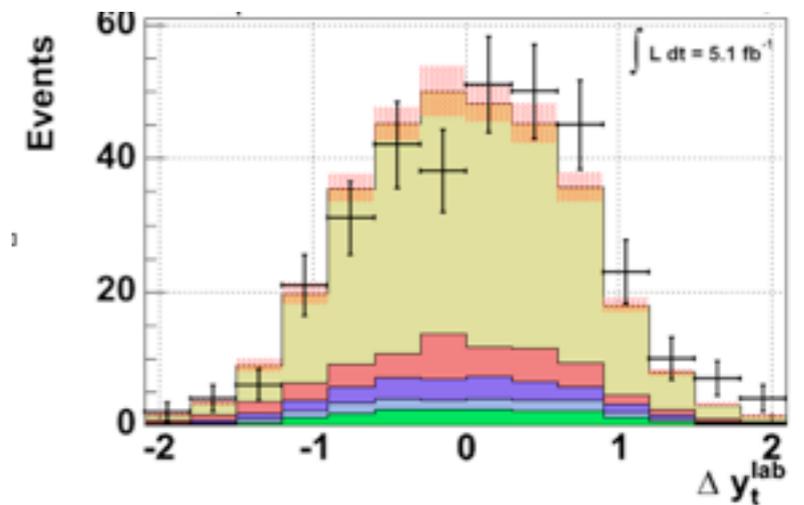
$$\sim 2 \sigma \quad (5 \text{ fb}^{-1})$$



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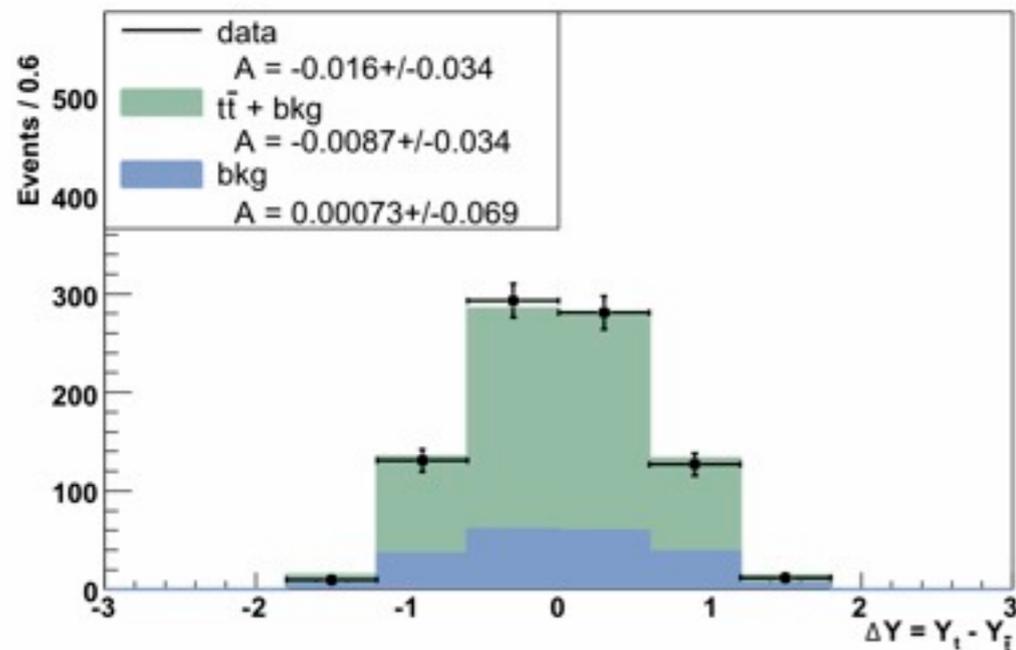
$$A_{FB} = 42 \pm 16 \%$$

$$\sim 2.7 \sigma \quad (5 \text{ fb}^{-1})$$



$$A_{FB}^{sm} \sim 6 \%$$

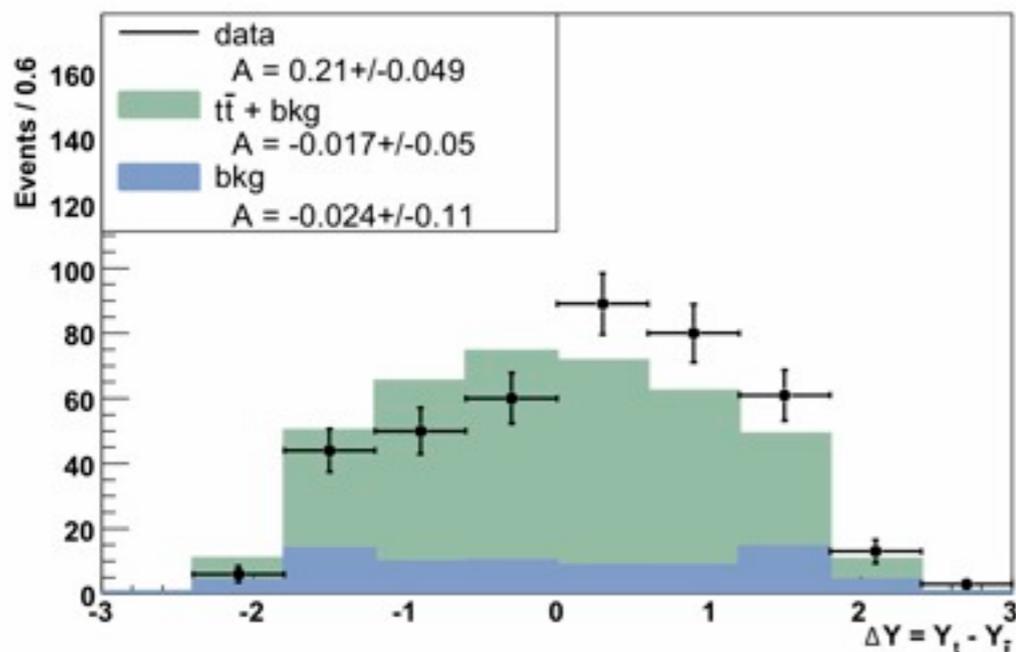
Summary of Results



For $M_{t\bar{t}} > 450 \text{ GeV}$

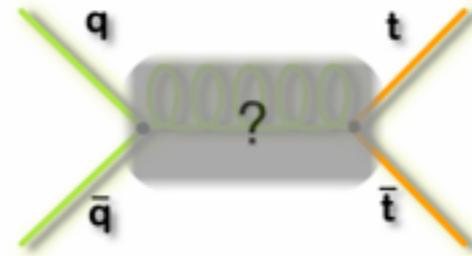
$A_{\text{FB}} = 48 \pm 11_{\text{stat+syst}} \%$

5.3 fb^{-1}

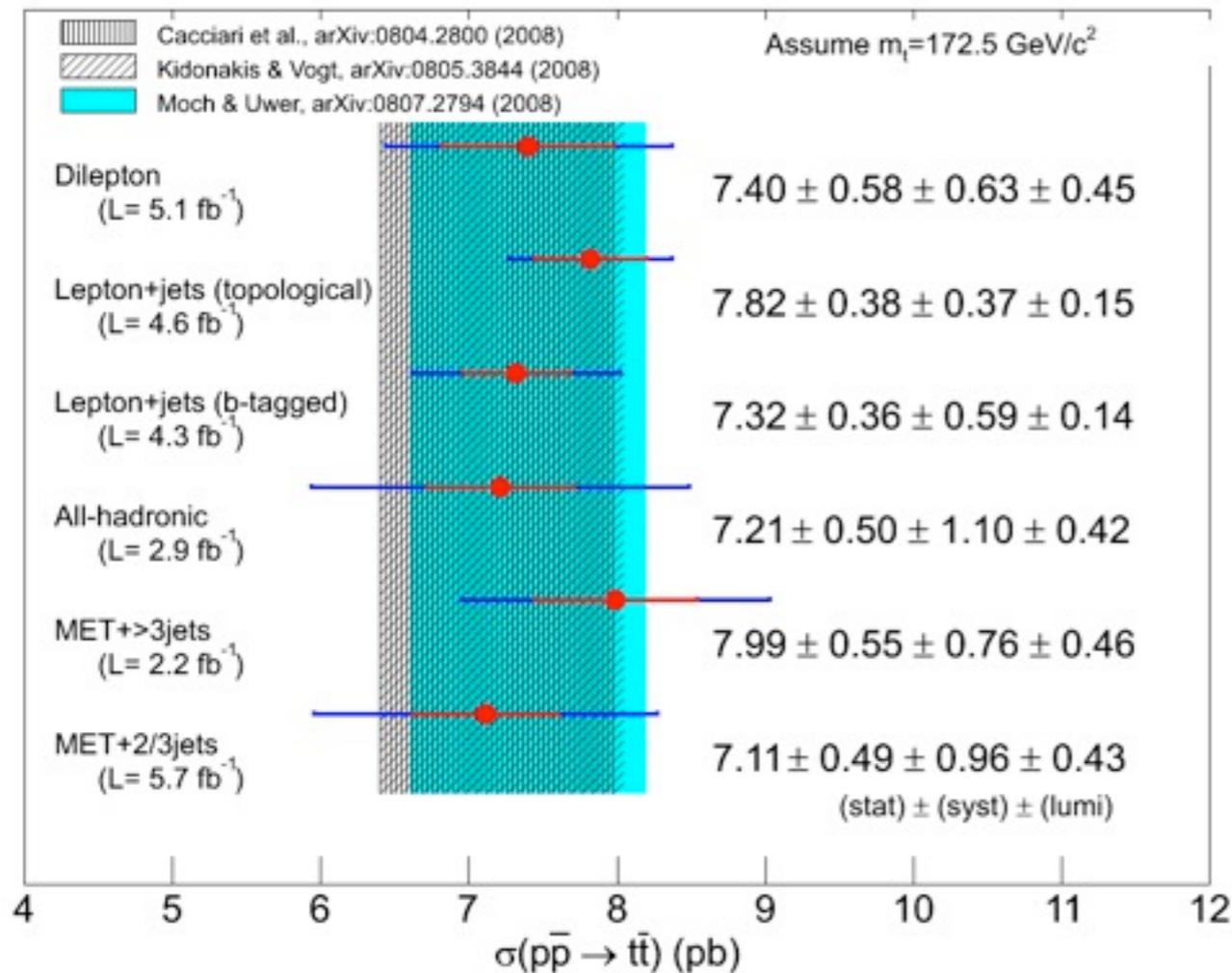


$A_{\text{FB}}^{\text{Theory}} = 9 \pm 1 \%$

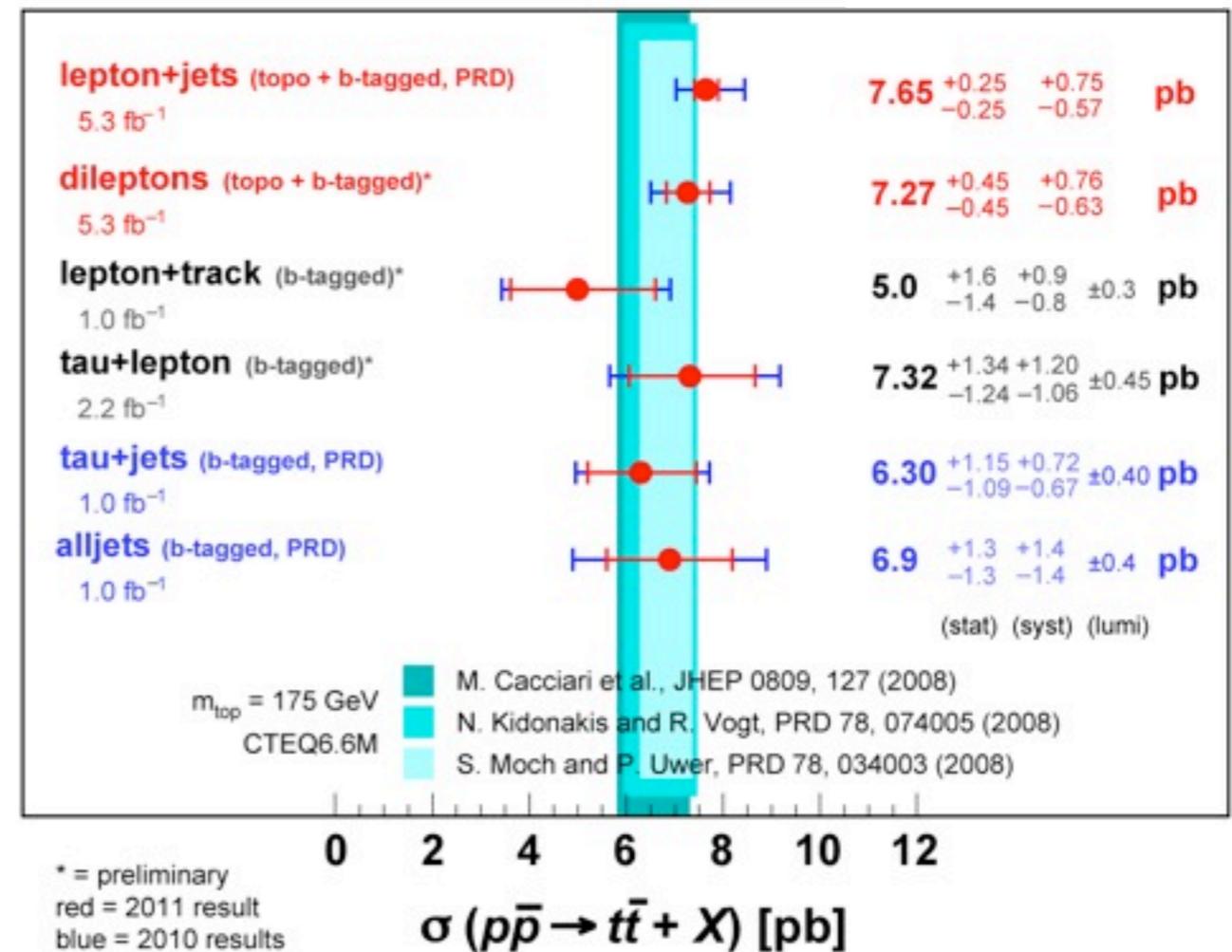
Rate of Top Production



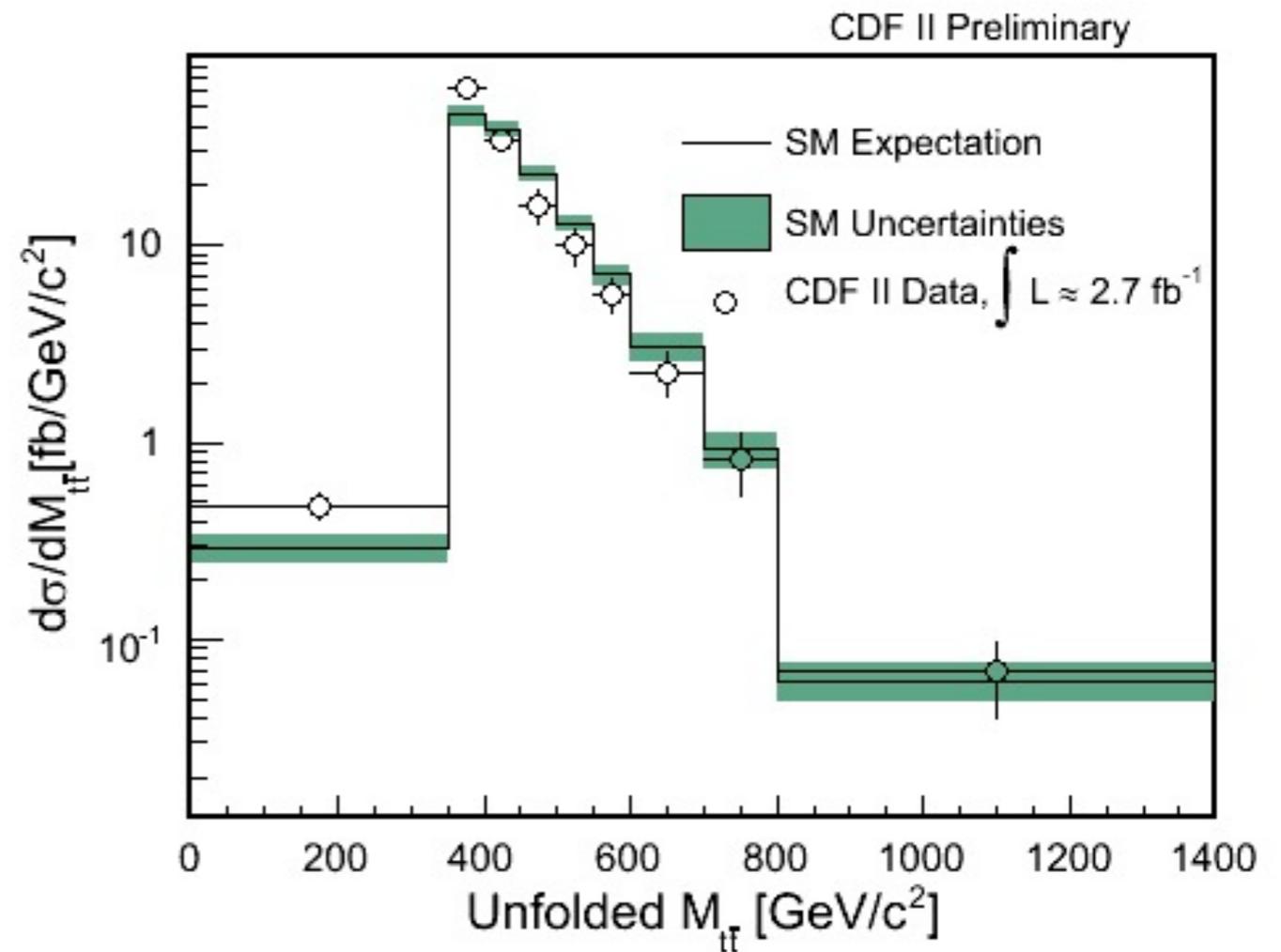
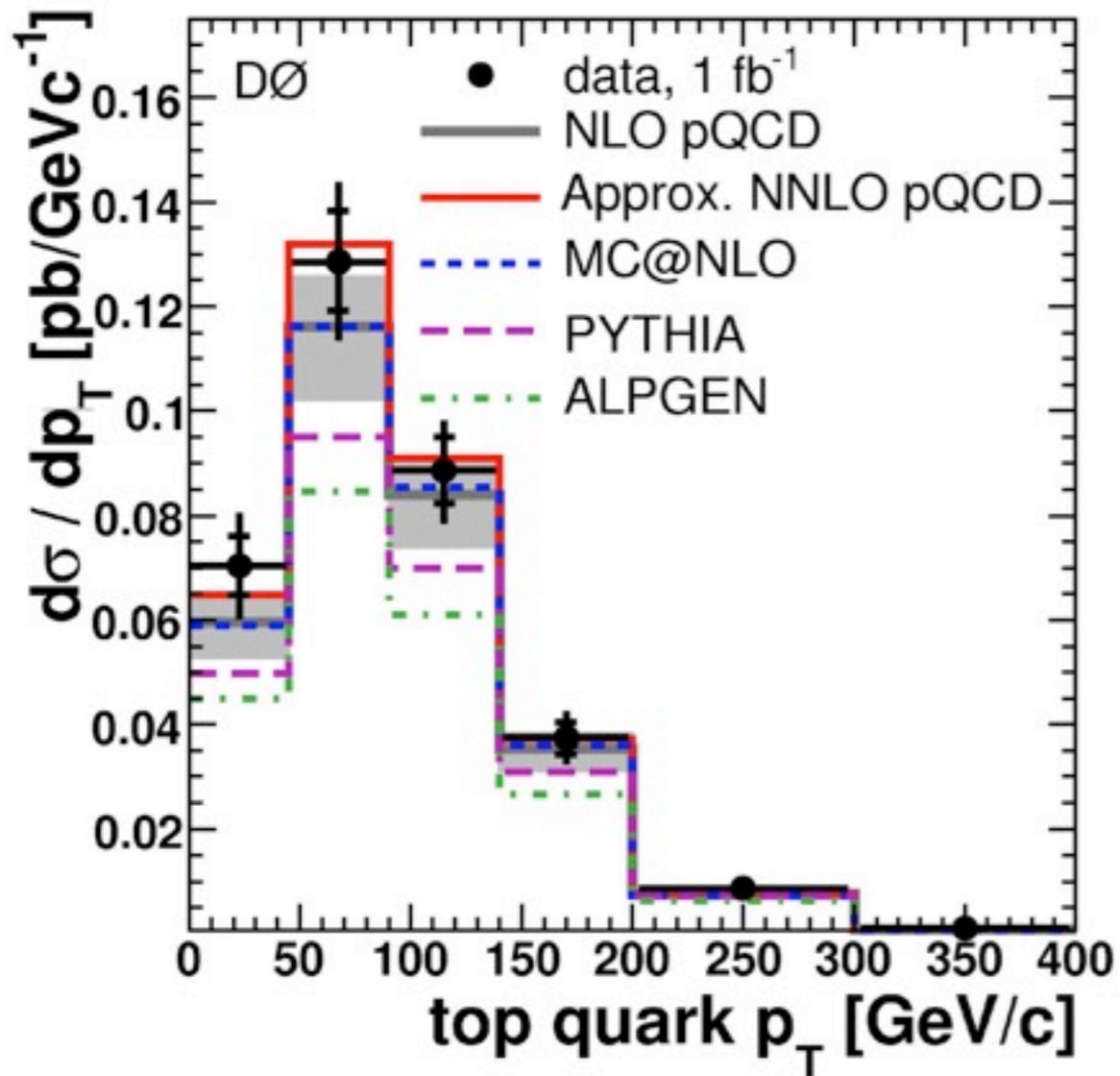
CDF Run II



D0 Run II



Top Kinematics



Boosted Top

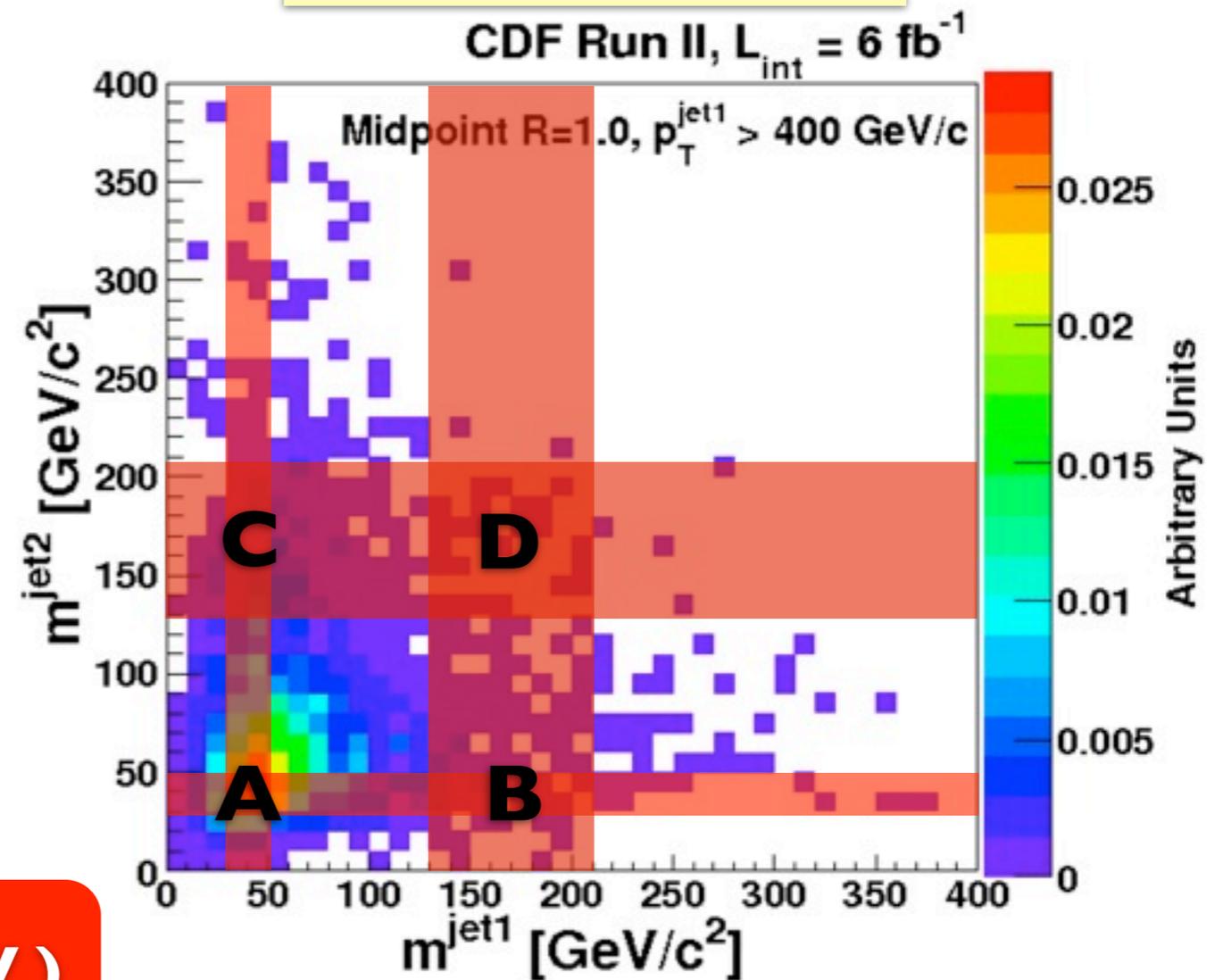
- Look for top events at very high P_t ($P_t > 400 \text{ GeV}$)

$$\sigma_{tt}^{\text{sm}} \sim 4 \text{ fb}$$

- Decay products merge together due to boost
- Use mass of top 'jets' to distinguish events
- Expect 44 ± 16 events, observe 58

$$\sigma_{tt} < 40 \text{ fb @ 95\%CL } (p_t > 400 \text{ GeV})$$

ABCD Method



What's Next for AFB

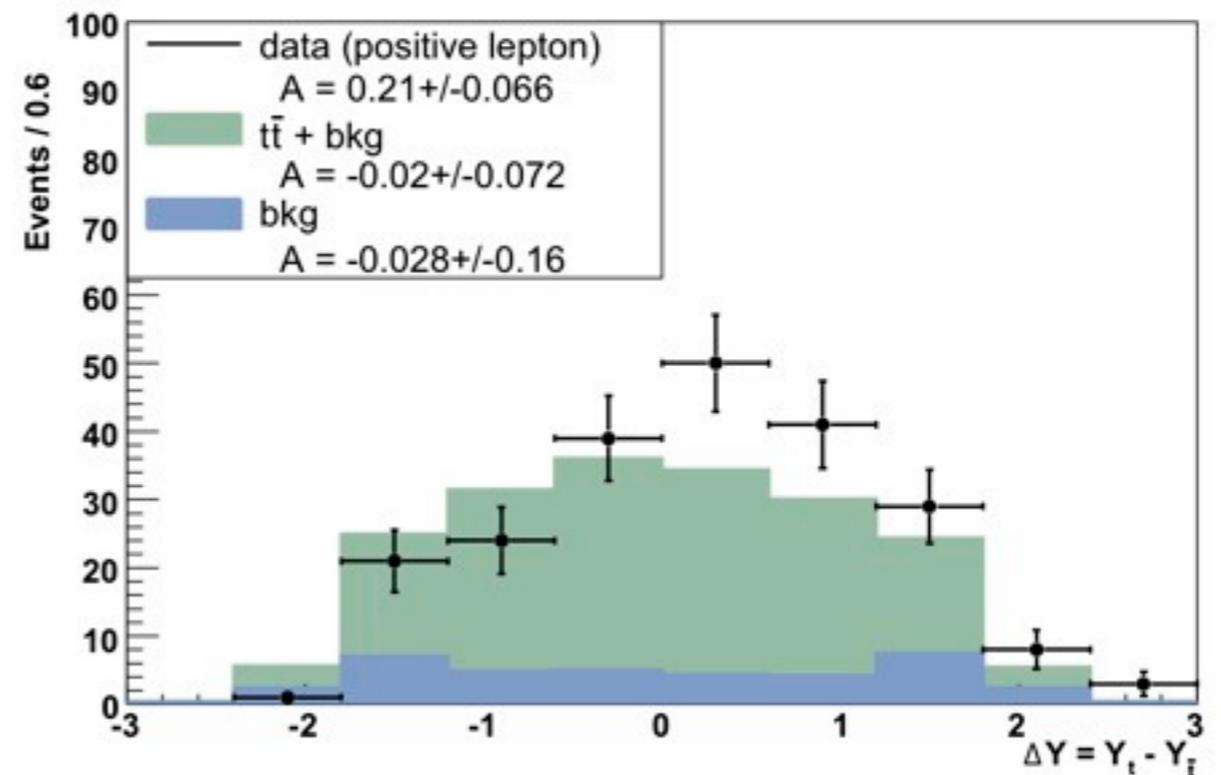
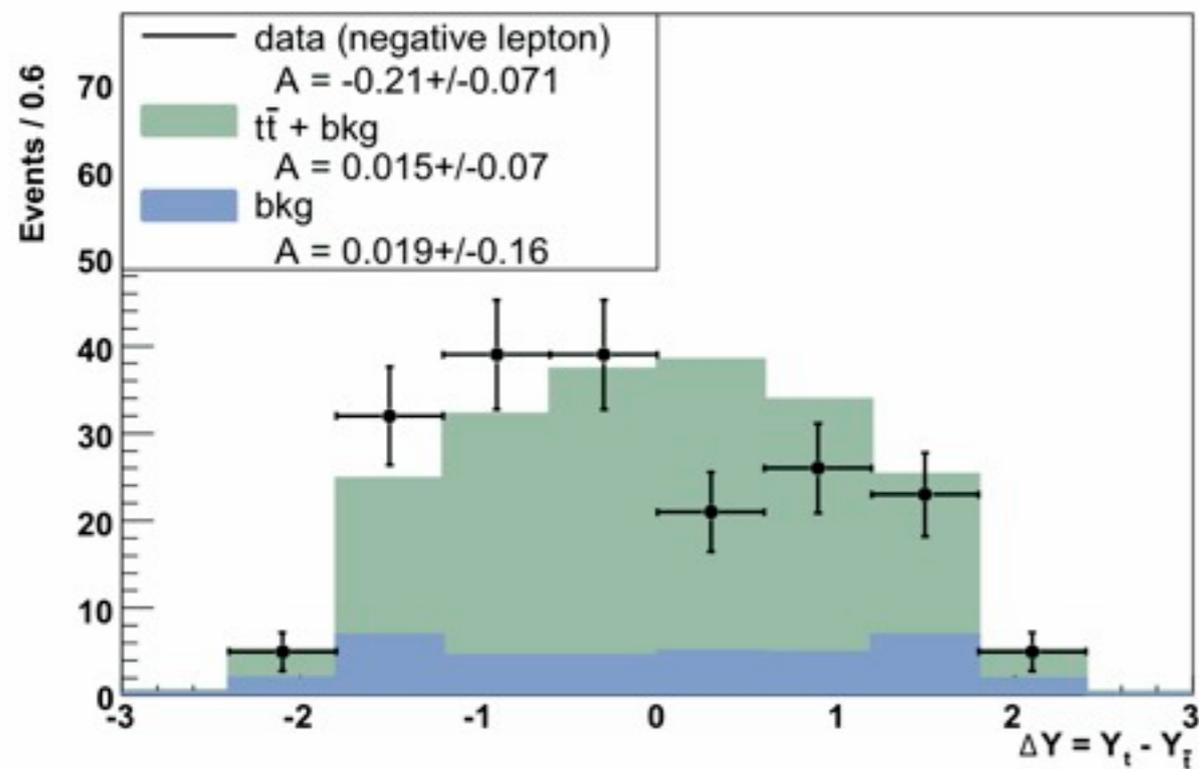
- **Time and data - really need $4-5\sigma$ before we're sure it's not statistics**
- **D0 will tell us more - comparable results, study mass dependence, combination**
- **Correlated to other observables → LHC needs to see something**

STAY TUNED!

Thanks!!!



$M_{t\bar{t}}$ Dependence



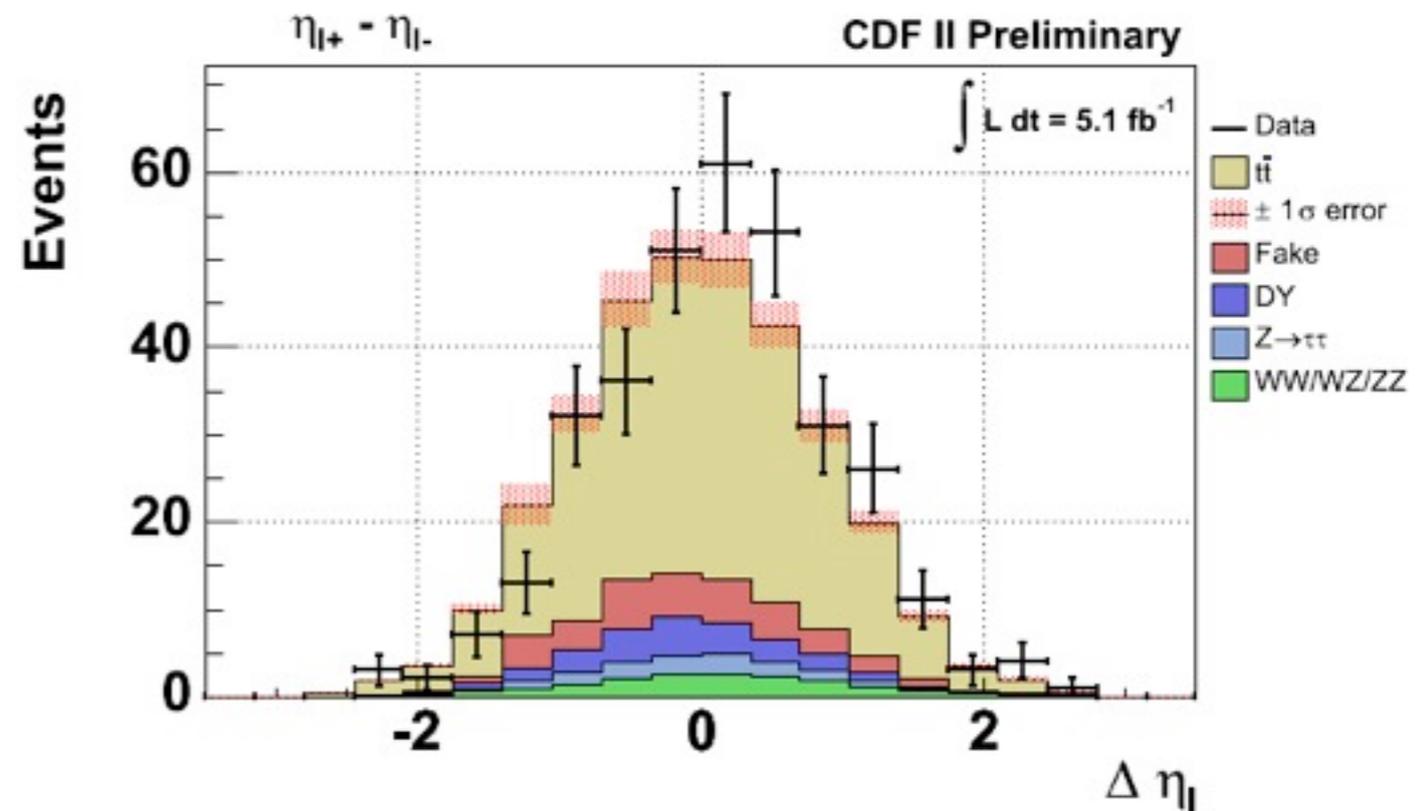
	Inclusive	$M < 450 \text{ GeV}$	$M > 450 \text{ GeV}$
AFB +	$6.7 \pm 4 \%$	$-1 \pm 5 \%$	$21 \pm 7 \%$
AFB -	$-5 \pm 4 \%$	$2 \pm 5 \%$	$-21 \pm 7 \%$

A_{FB} in Dileptons

- **Top direction correlated with two leptons**
- **Much simpler than reconstruction algorithm - though correlated**
- **Significance remains**

$$A_{\text{FB}}^{\text{II}} = 14 \pm 5_{\text{stat}} \%$$

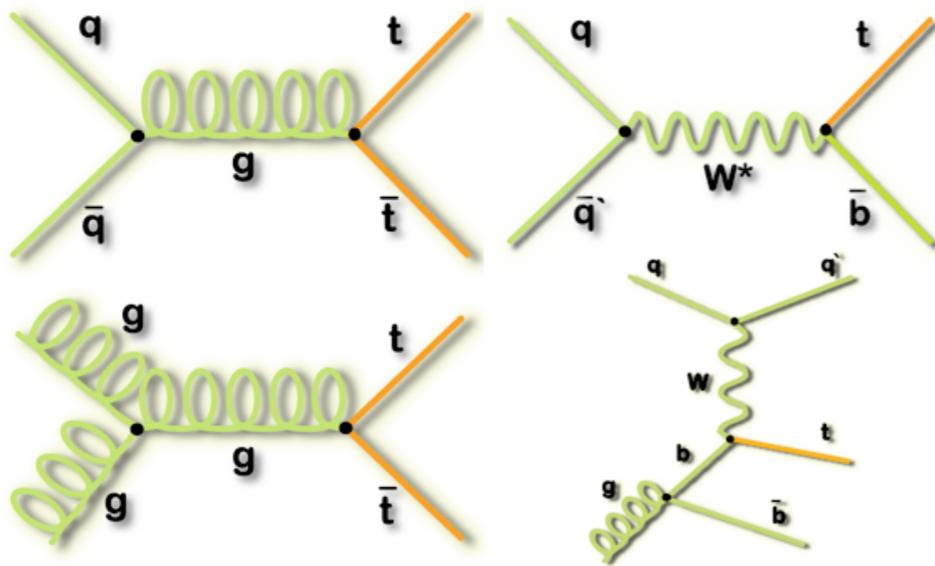
$$5.1 \text{ fb}^{-1}$$



$$A_{\text{FB}}^{\text{Pred}} = -2 \pm 2 \%$$

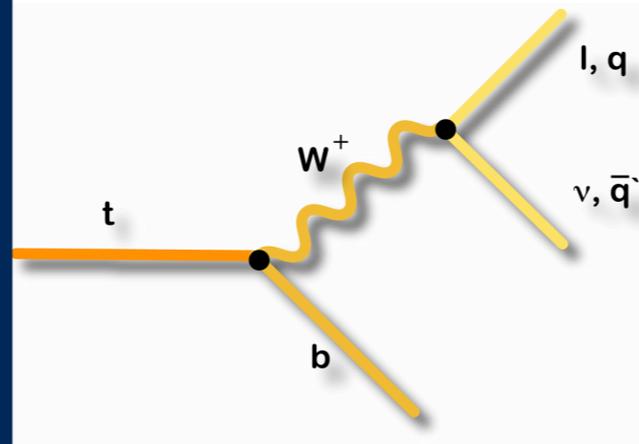
Tevatron Top Physics

How is Top Produced



- **Strong Force**
 $\sigma_{tt} \sim 7.5 \text{ pb}$
- **Electroweak**
 $\sigma_{s+t} \sim 3 \text{ pb}$

How Does Top Decay



- **V-A**
 $F_0 \sim 0.7, F_+ \sim 0$
- $V_{TB} \sim 1$

What are Top's Intrinsic Properties

$2/3$ $+2/3$ C charm	$1/2$ $+2/3$ t top
$1/2$ $-1/3$ S	$1/2$ $-1/3$ b

- **Mass**
- **Spin** $1/2$
- **Charge** $+2/3$

Tevatron Top Physics

How is Top Produced

$$\sigma_{tt} = 7.70 \quad \delta \sim 6\%$$

$$\sigma_{s+t} = 2.8 \quad \delta \sim 19\%$$

$$\sigma_t = 3.1 \quad \delta \sim 30\%$$

How Does Top Decay

$$F_0 = 0.88 \quad \delta \sim 10\%$$

$$F_+ = -0.15 \quad \delta \sim 10\%$$

$$V_{tb} = 0.88 \quad \delta \sim 9\%$$

What are Top's Intrinsic Properties

$$M_t = 173.3 \quad \delta \sim 0.6\%$$

$$\Gamma_t \sim 2.1 \quad @ 25\%CL$$

$$\kappa = 0.7 \quad sig \sim 1\sigma$$

$$q \neq -4/3 \quad @ 95\%CL$$

- Strong Force
 $\sigma_{tt} \sim 7.5 \text{ pb}$
- Electroweak
 $\sigma_{s+t} \sim 3 \text{ pb}$

- V-A
 $F_0 \sim 0.7, F_+ \sim 0$
- $V_{TB} \sim 1$

- Mass
- Spin $1/2$
- Charge $+2/3$

What you shouldn't worry about

- **Backgrounds**
 - **Too small, and the predicted asymmetry in backgrounds goes in the opposite direction**
- **Reconstruction**
 - **If it's broken, it's broken for MANY precision measurements that agree with the SM and other well-vetted techniques**
- **Unfolding**
 - **The significance of the result is present before the acceptance/reconstruction corrections - they only scale the result**

Questions...

- **Why do muons have a larger asymmetry than electrons?**
- **Why is the lab frame asymmetry stronger, yet less dependent on M_{tt} ?**
- **Why is the result in dileptons so much larger?**

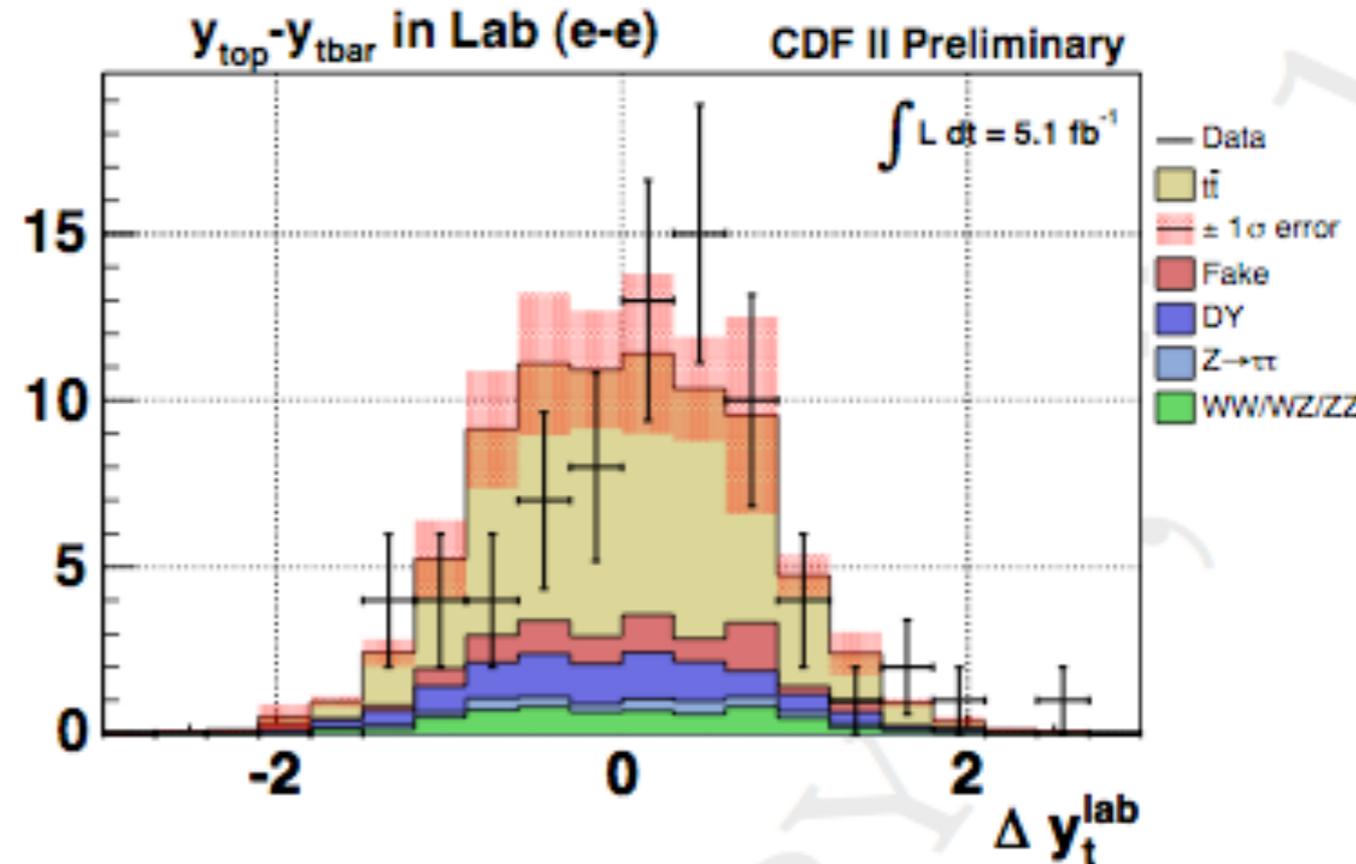
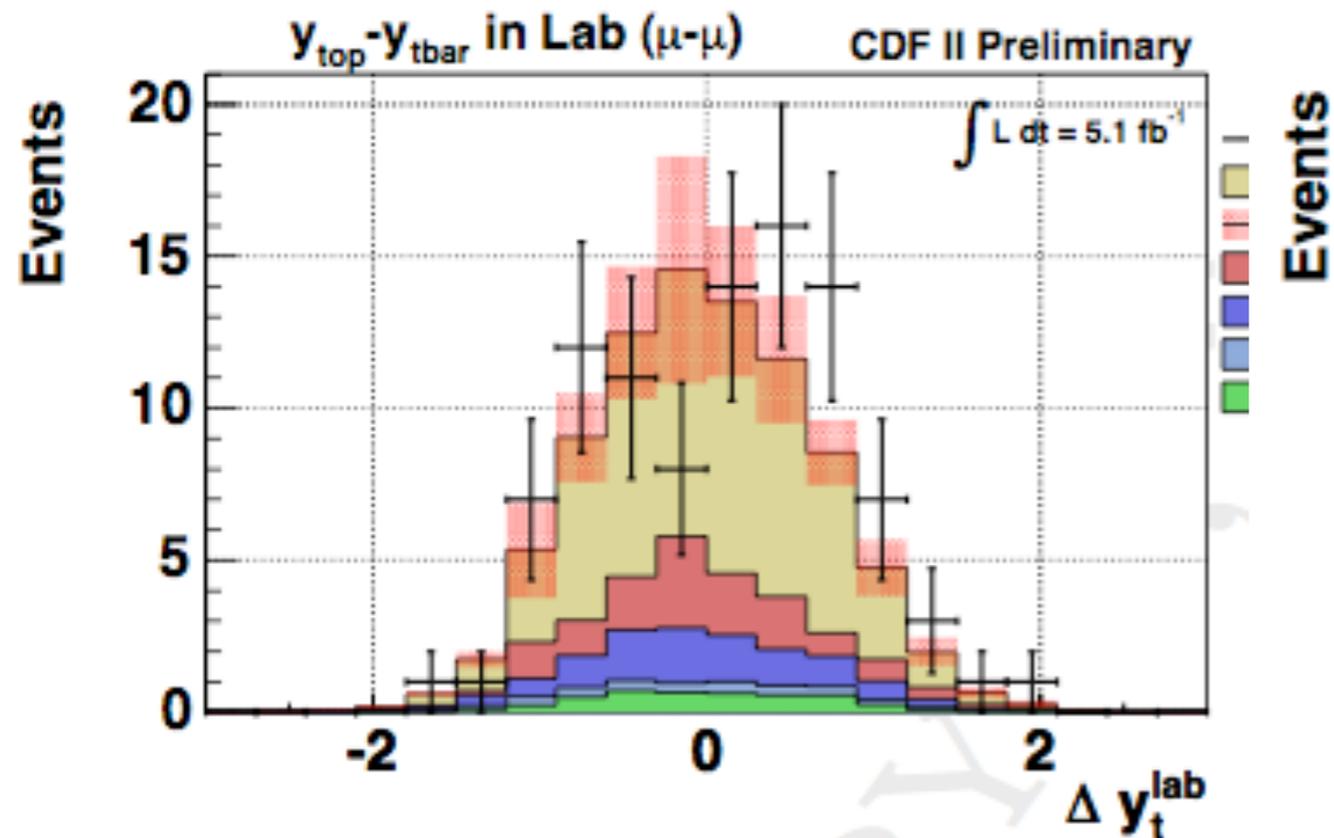
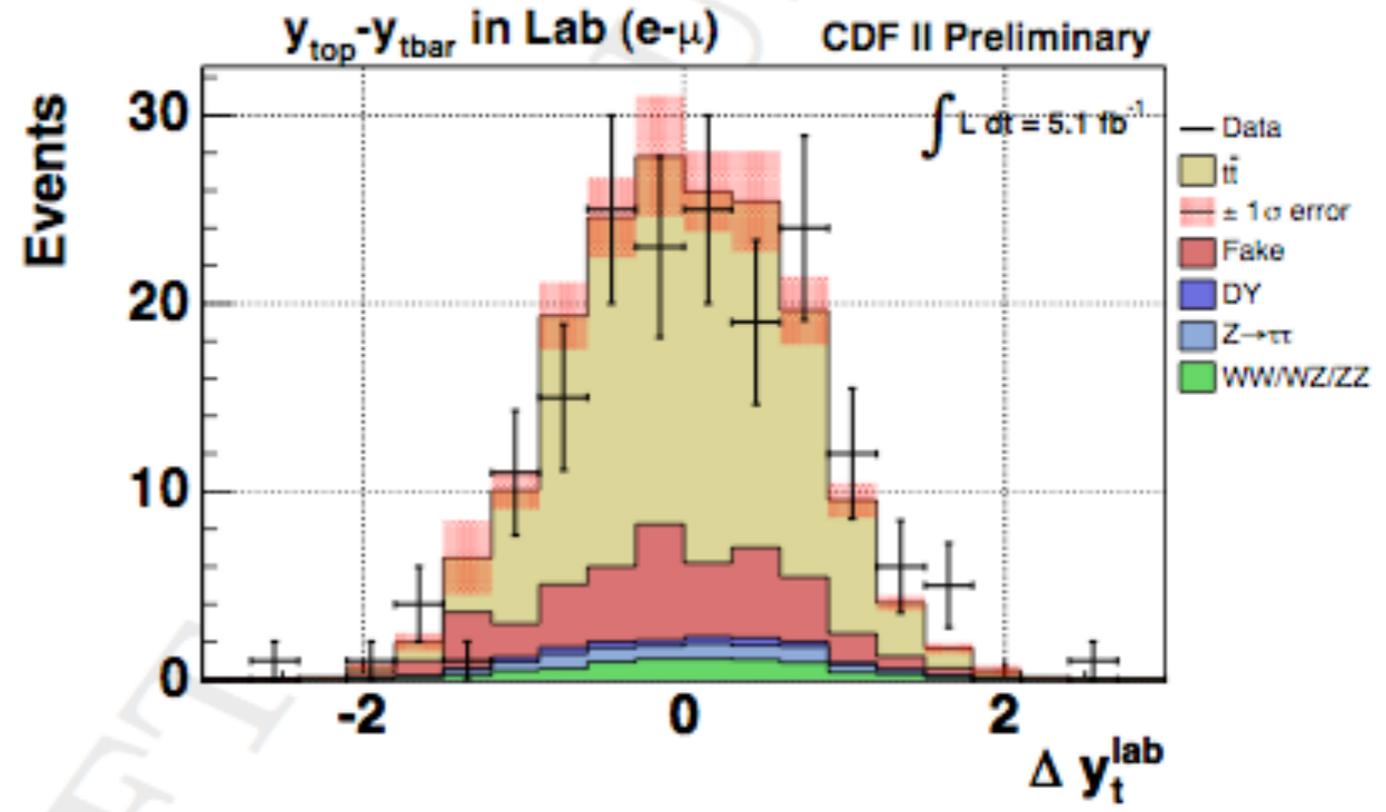
Muons vs Electrons

*** before corrections**

selection	N events	all M	$M < 450 \text{ GeV}/c^2$	$M \geq 450 \text{ GeV}/c^2$
standard	1260	0.057 ± 0.028	-0.016 ± 0.034	0.212 ± 0.049
electrons	735	0.026 ± 0.037	-0.020 ± 0.045	0.120 ± 0.063
muons	525	0.105 ± 0.043	-0.012 ± 0.054	0.348 ± 0.080
data $\chi^2 < 3.0$	338	0.030 ± 0.054	-0.033 ± 0.065	0.180 ± 0.099
data no-b-fit	1260	0.062 ± 0.028	0.006 ± 0.034	0.190 ± 0.050
data single b-tag	979	0.058 ± 0.031	-0.015 ± 0.038	0.224 ± 0.056
data double b-tag	281	0.053 ± 0.059	-0.023 ± 0.076	0.178 ± 0.095
data anti-tag	3019	0.033 ± 0.018	0.029 ± 0.021	0.044 ± 0.035
pred anti-tag	-	0.010 ± 0.007	0.013 ± 0.008	0.001 ± 0.014
pre-tag	4279	0.040 ± 0.015	0.017 ± 0.018	0.100 ± 0.029
pre-tag no-b-fit	4279	0.042 ± 0.015	0.023 ± 0.018	0.092 ± 0.029

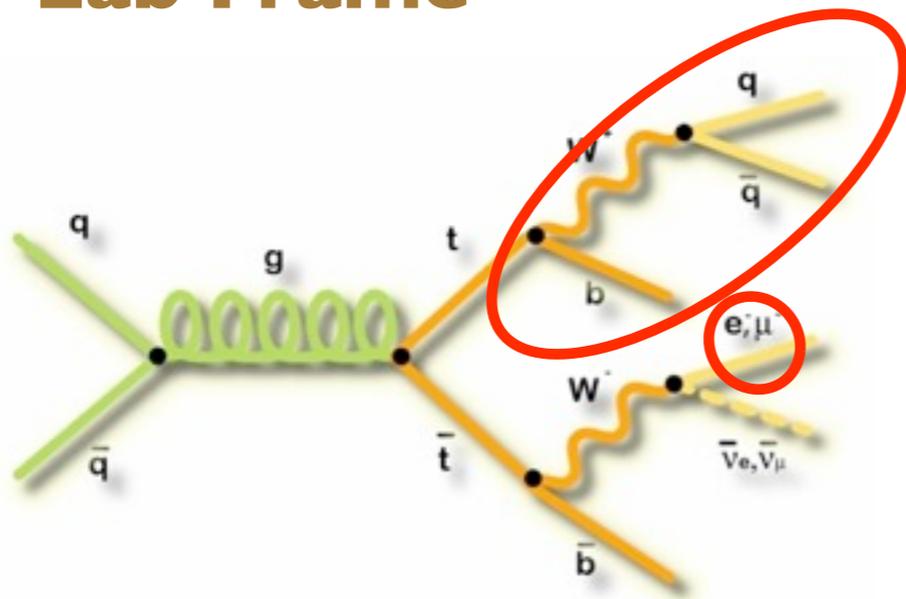
What about the di-lepton result?

Flavor	Asymmetry
Inclusive	$14 \pm 5 \%$
e-e	$27 \pm 11 \%$
e-u	$6.4 \pm 7.6 \%$
u-u	$17 \pm 10 \%$

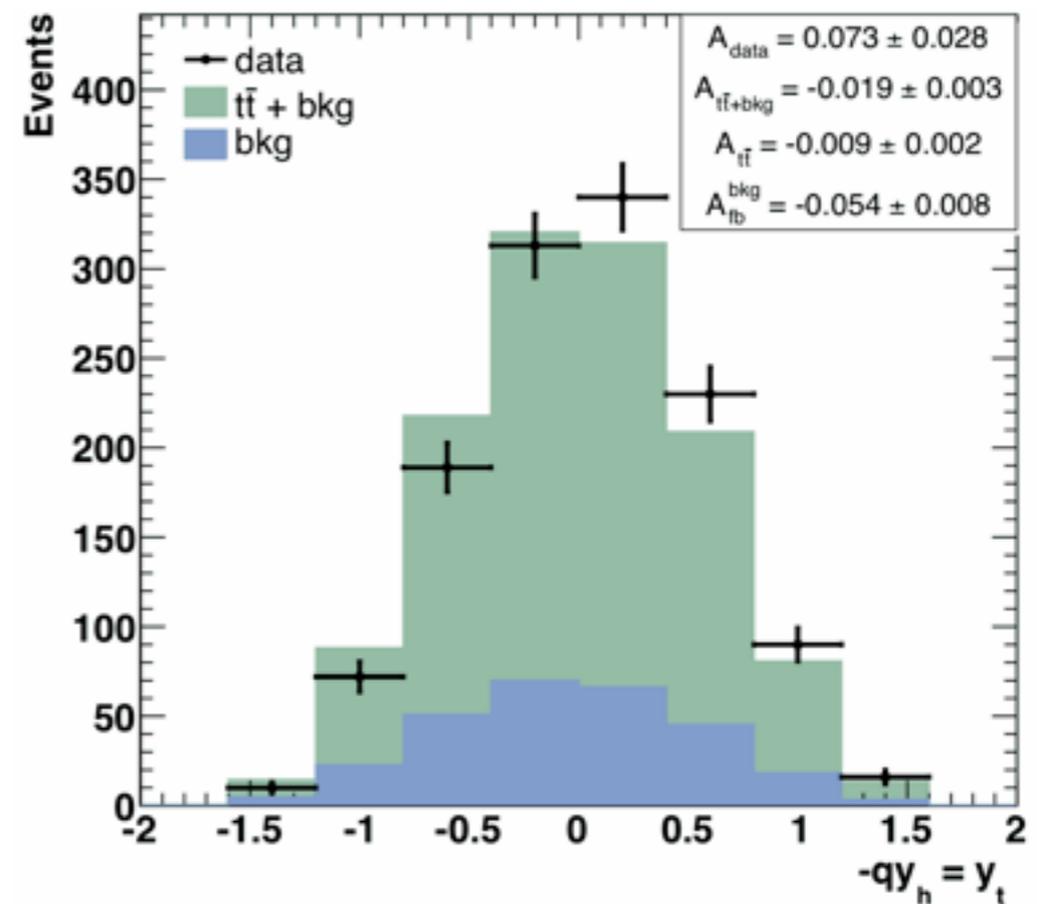


Lab Frame

- **Alternative method**
 - **Lab Frame**



- **Takes the Lepton Pt and Neutrino out of it, still depend on lepton charge**

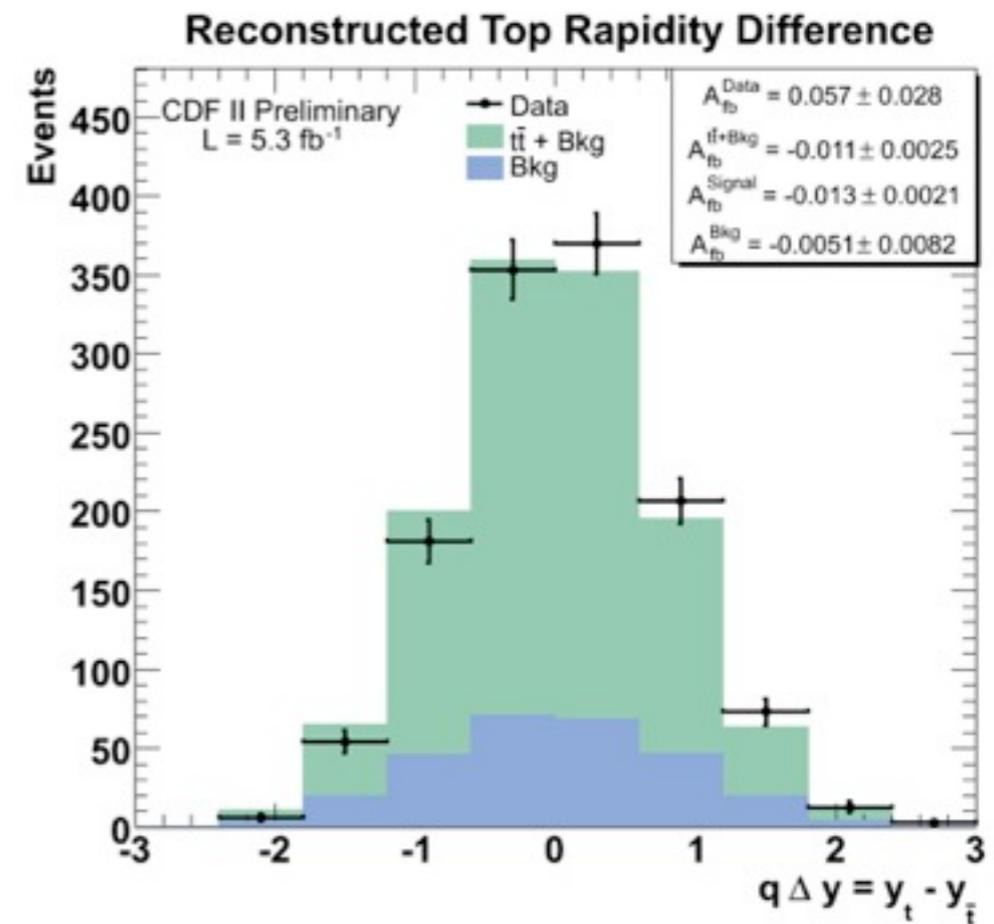
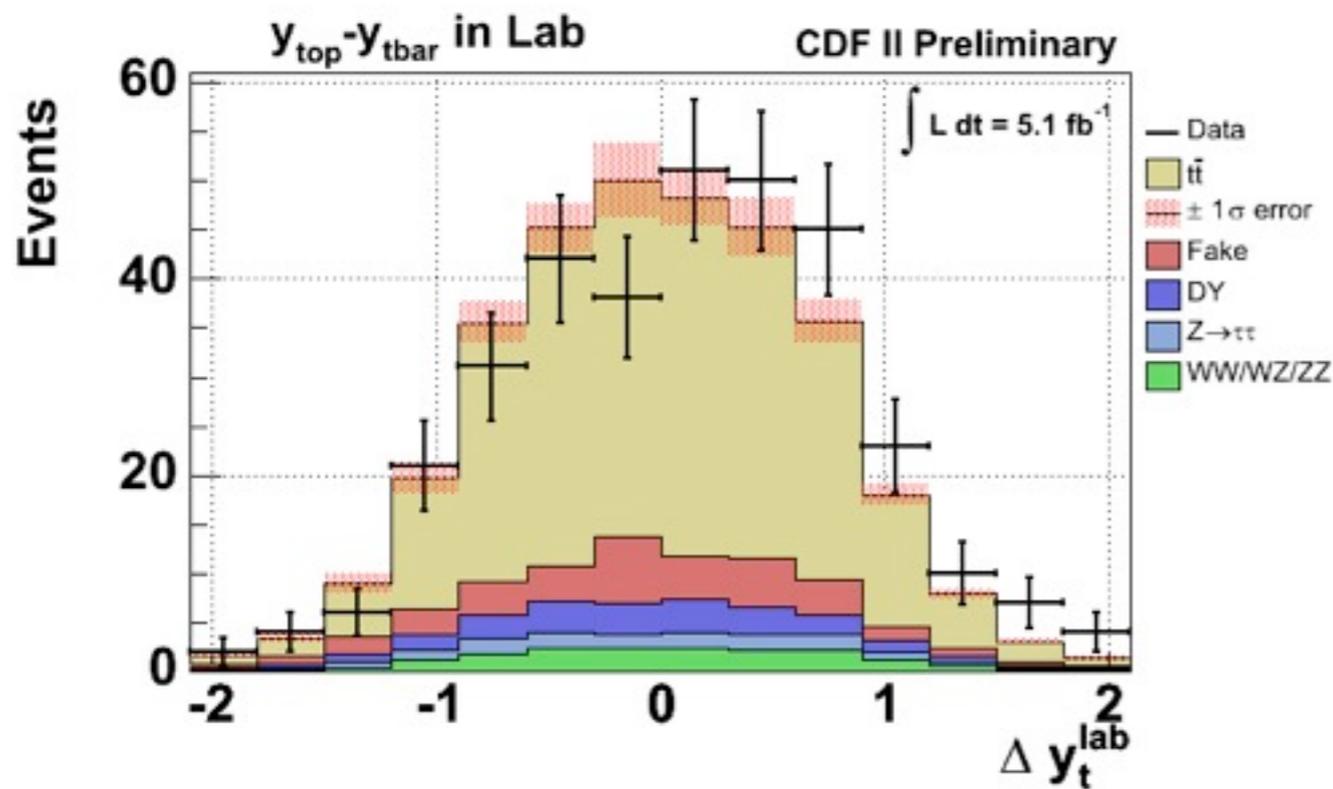


$$A_{FB} = 15 \pm 5_{\text{stat+syst}} \%$$

Lab Frame

	Inclusive	M < 450 GeV	M > 450 GeV
Data - tt Frame	$5.7 \pm 2.8 \%$	$-1 \pm 3 \%$	$21 \pm 5 \%$
SM Prediction	$2 \pm 0.4 \%$	$1 \pm 0.6 \%$	$3 \pm 0.7 \%$
Data - pp Frame	$7.3 \pm 2.8 \%$	$5.9 \pm 3.4 \%$	$10.3 \pm 4.9 \%$
SM Prediction	$2 \pm 0.4 \%$	$-1 \pm 0.5 \%$	$2 \pm 0.7 \%$

Dileptons vs L+Jets



$$A_{\text{FB}} = 42 \pm 15_{\text{stat}} \pm 5_{\text{syst}} \%$$

5.1 fb^{-1}

$$A_{\text{FB}} = 16 \pm 7_{\text{stat}} \pm 2_{\text{syst}} \%$$

5.3 fb^{-1}

$M_{t\bar{t}}$ Dependence

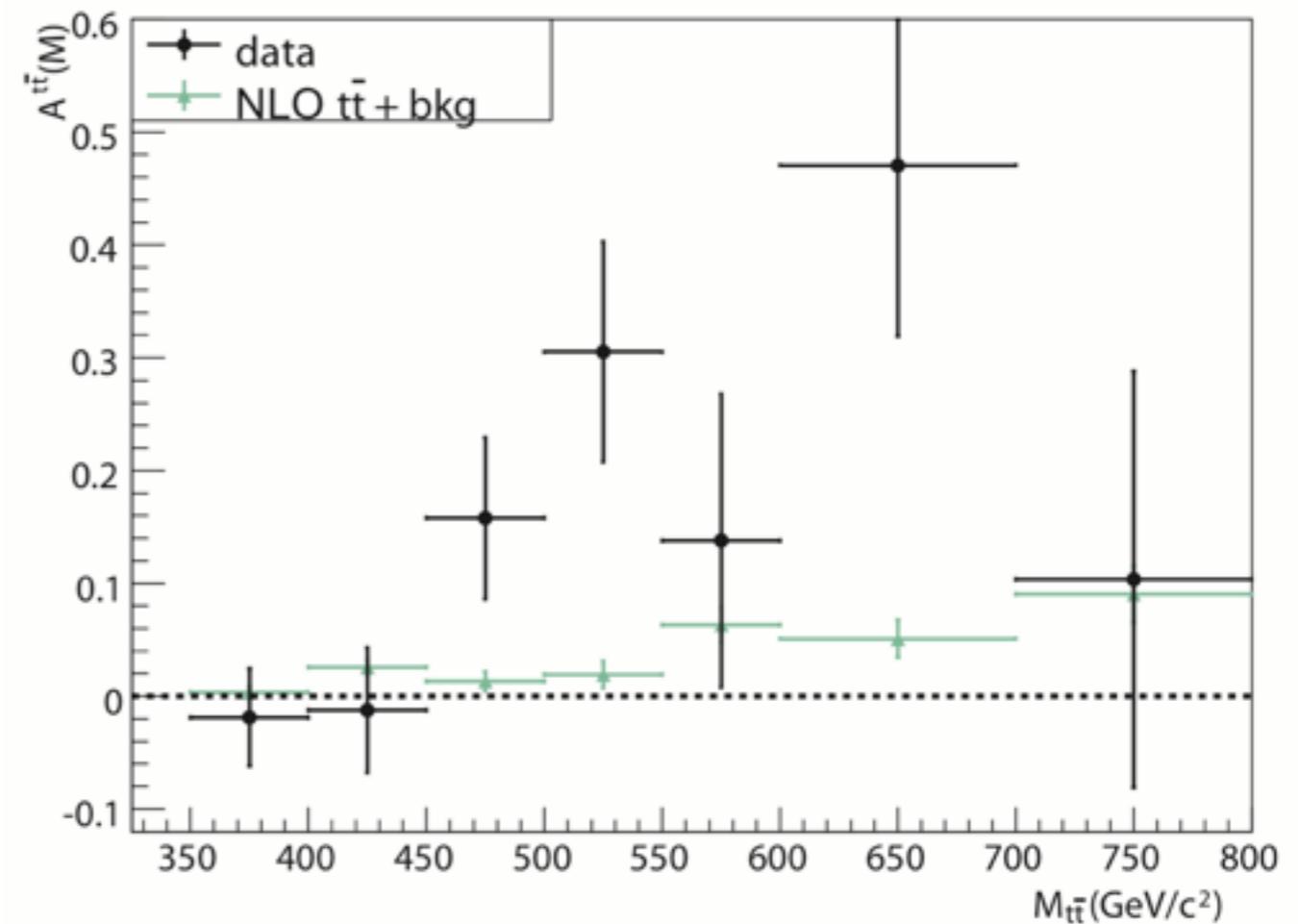
- What is the optimal high/low bin-edge (based on MC) ?

bin-edge (GeV/ c^2)	OctetA		OctetB	
	$A^{t\bar{t}}$	significance	$A^{t\bar{t}}$	significance
345	0.082 ± 0.028	2.90	0.168 ± 0.028	5.99
400	0.128 ± 0.036	3.55	0.235 ± 0.035	6.74
→ 450	0.183 ± 0.047	3.91	0.310 ± 0.044	7.08
500	0.215 ± 0.060	3.60	0.369 ± 0.054	6.81
550	0.246 ± 0.076	3.25	0.425 ± 0.066	6.43
600	0.290 ± 0.097	2.97	0.460 ± 0.081	5.70

Models provided by Tim Tait

$M_{t\bar{t}}$ Dependence

- **Interesting effect**
- **Want to correct this now to compare directly to SM - unfolding**
- **450 GeV choice though lies on a weird spot**
- **We're stuck with what we chose, but this demonstrates the limits of 4-bin unfolding**



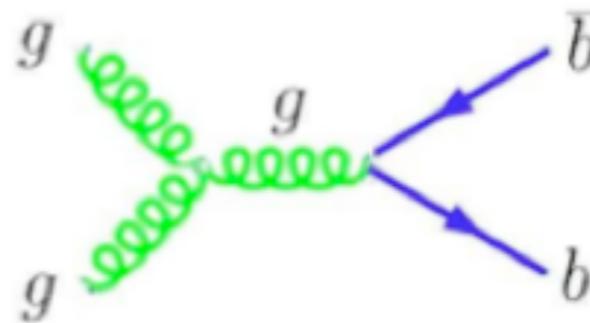
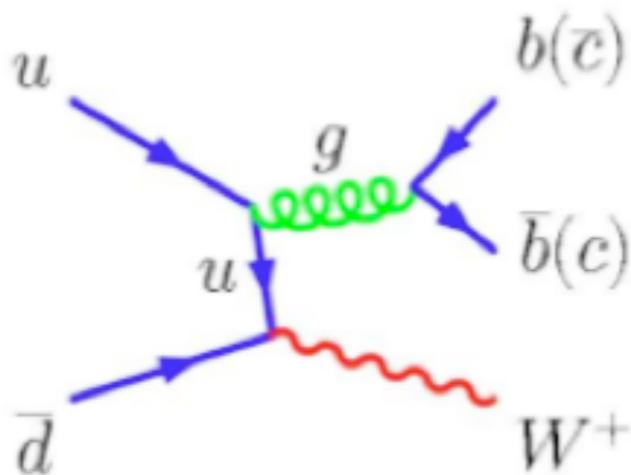


Reconstruction and Corrections

Backgrounds

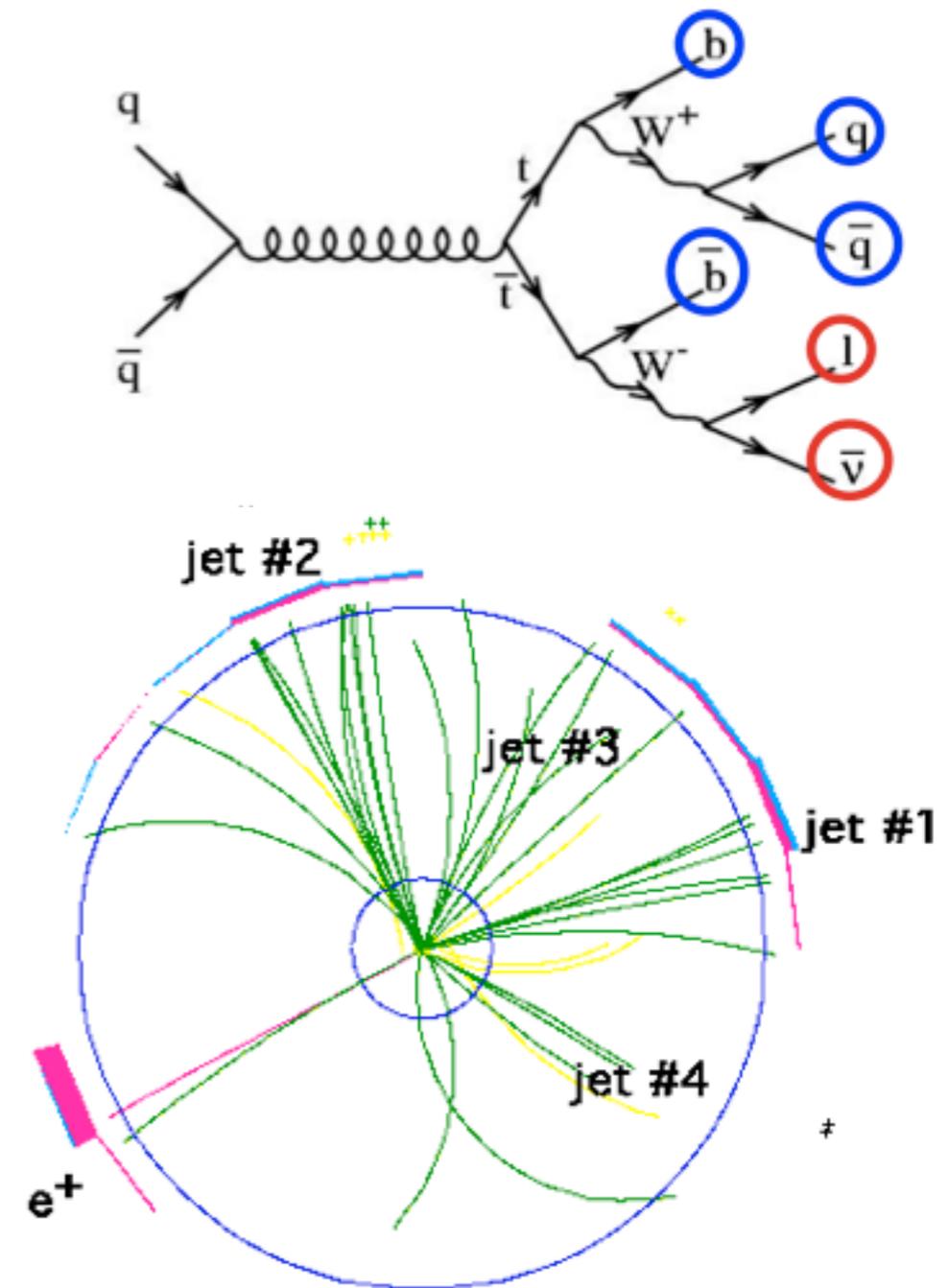
- **Select 1260 Events**
- **Predict ~ 1287**
- **~ 20% background**

Process	Prediction
W+Jets	181
QCD	67
Other	35
$t\bar{t}$	1004
Data	1260

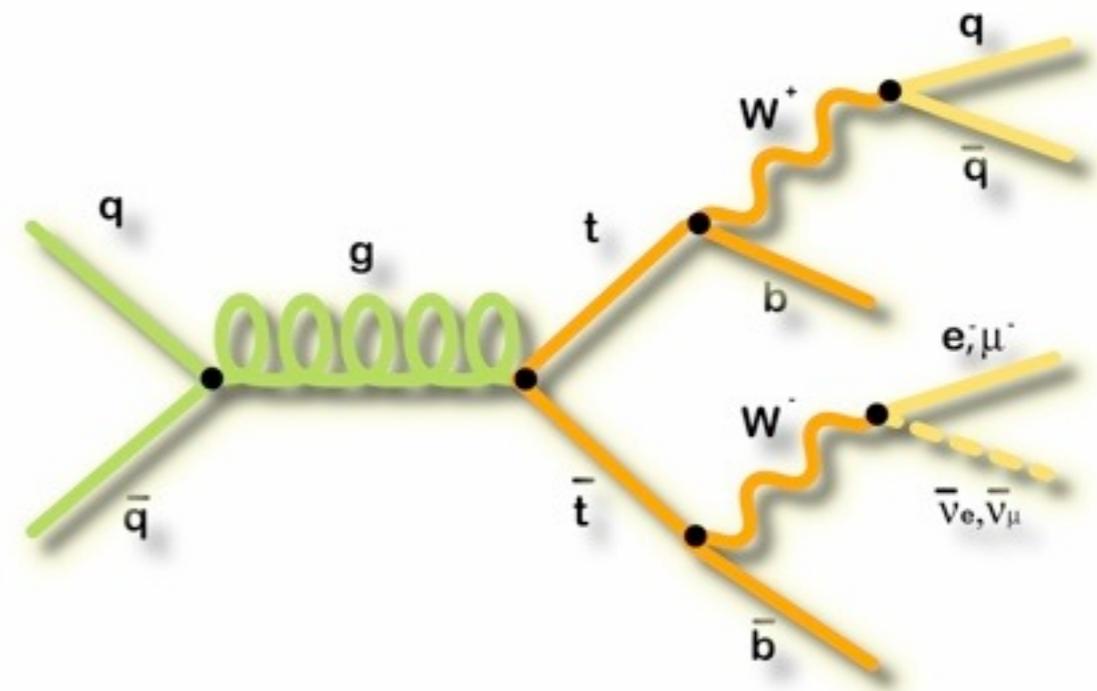
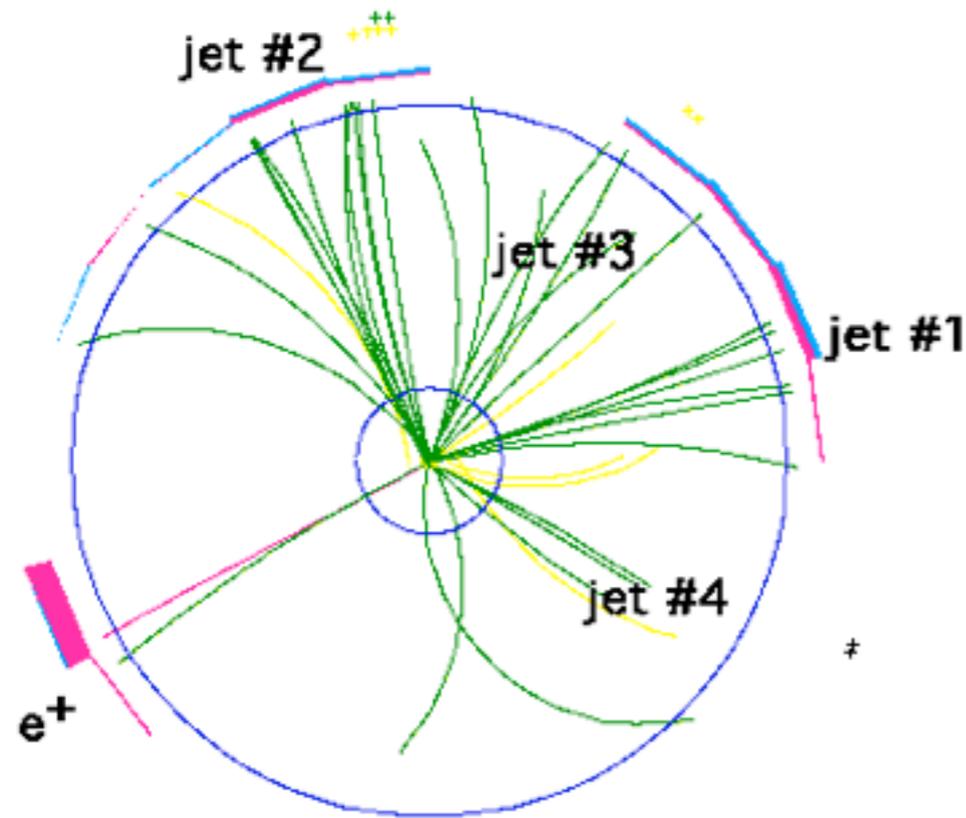


Event Reconstruction

- **Reconstruct the top direction from the observables in the detector**
- **Biggest problem is to match the jets in the detector to the “true” decay products of t and \bar{t} ?**
- **4 Jets to match to 4 quarks leads to 24 combinations**
- **Use the event topology to build an algorithm!**

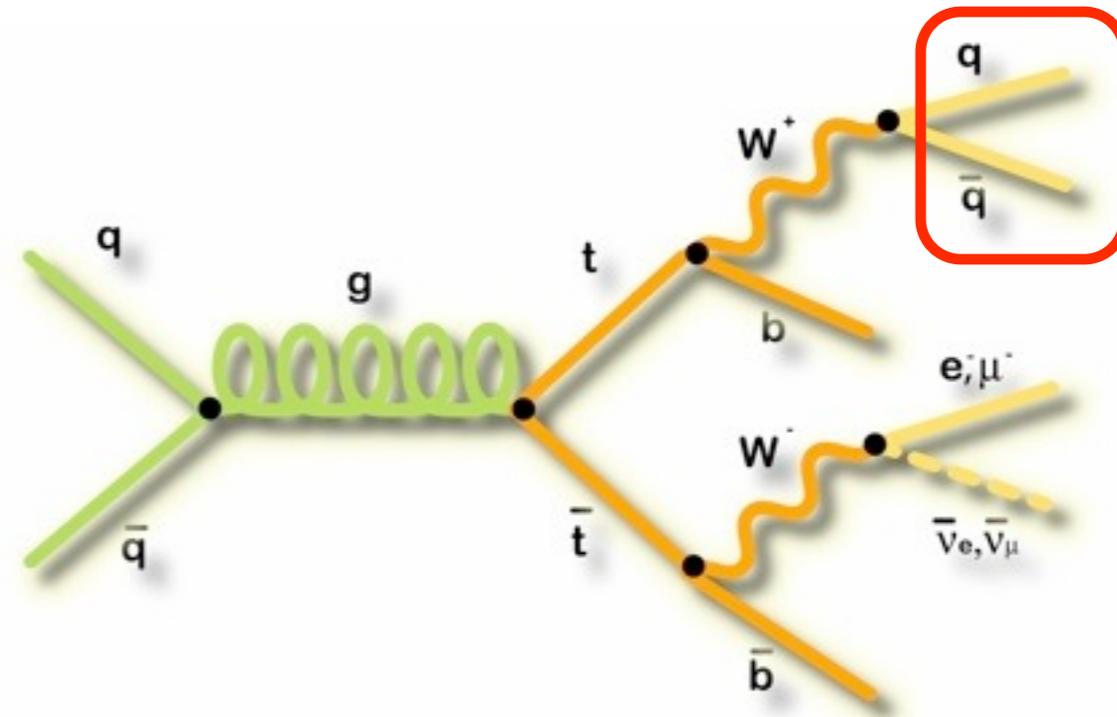
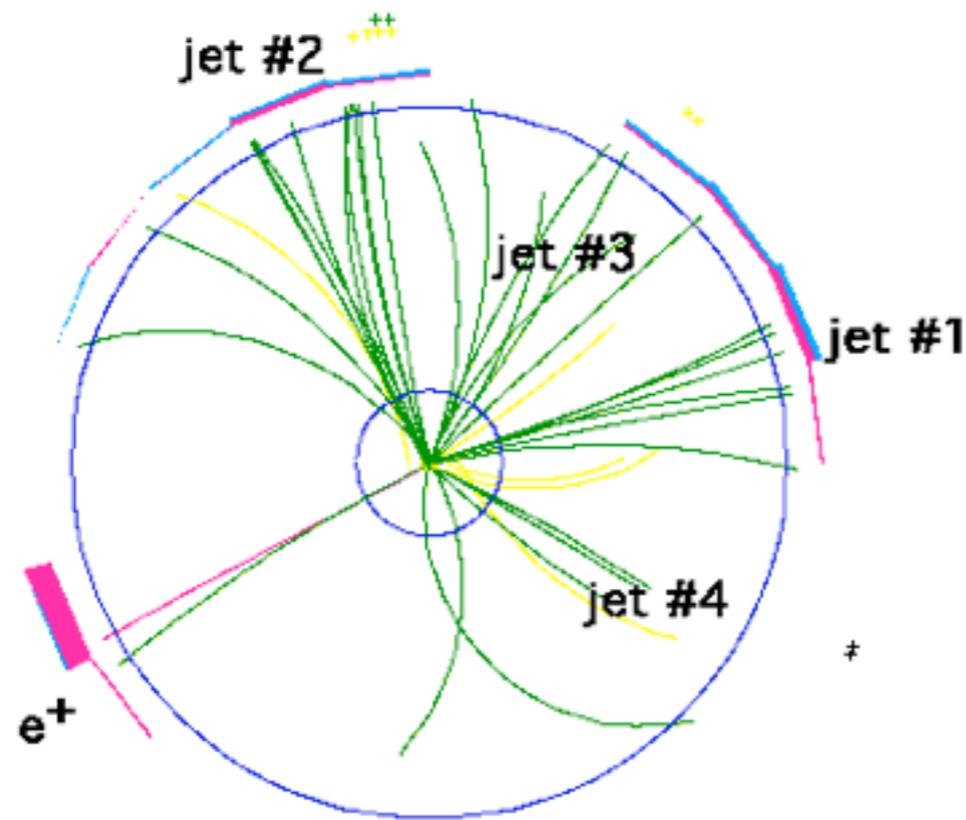


Event Reconstruction



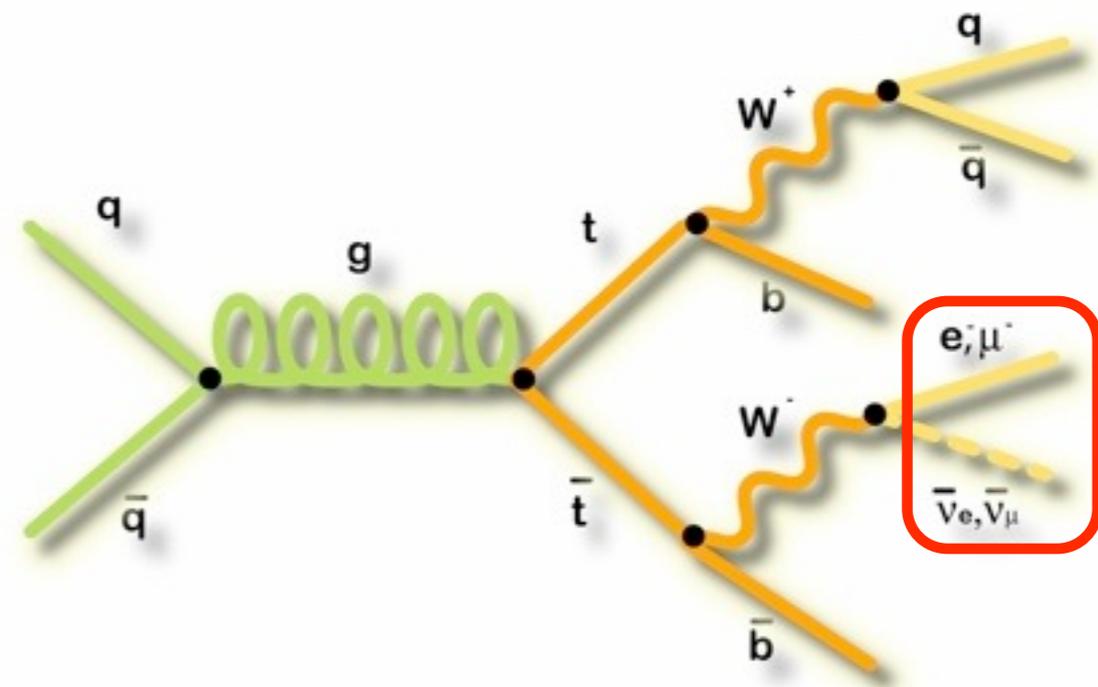
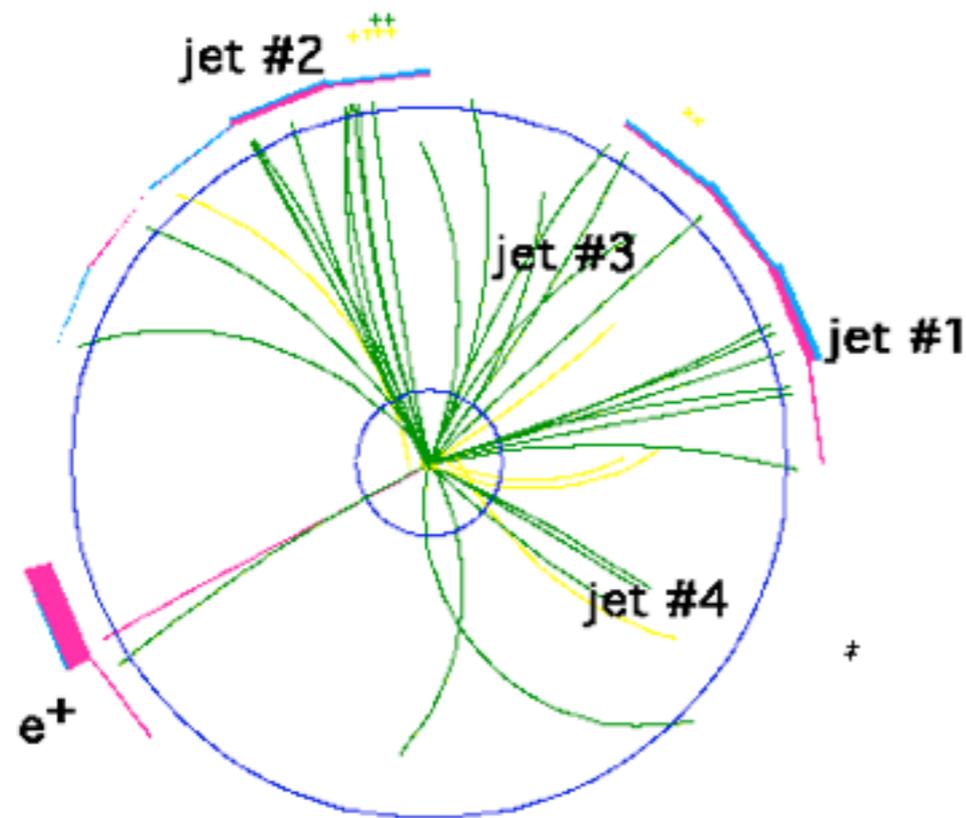
$$\chi^2 = \sum_{i=l,jets} \frac{(p_t^{i,meas} - p_t^{i,fit})^2}{\sigma_i^2} + \sum_{j=x,y} \frac{(p_j^{UE,meas} - p_j^{UE,fit})^2}{\sigma_j^2} + \frac{(M_{jj} - M_W)^2}{\Gamma_W^2} + \frac{(M_{lv} - M_W)^2}{\Gamma_W^2} + \frac{(M_{bjj} - M_{fit})^2}{\Gamma_t^2} + \frac{(M_{blv} - M_{fit})^2}{\Gamma_t^2}$$

Event Reconstruction



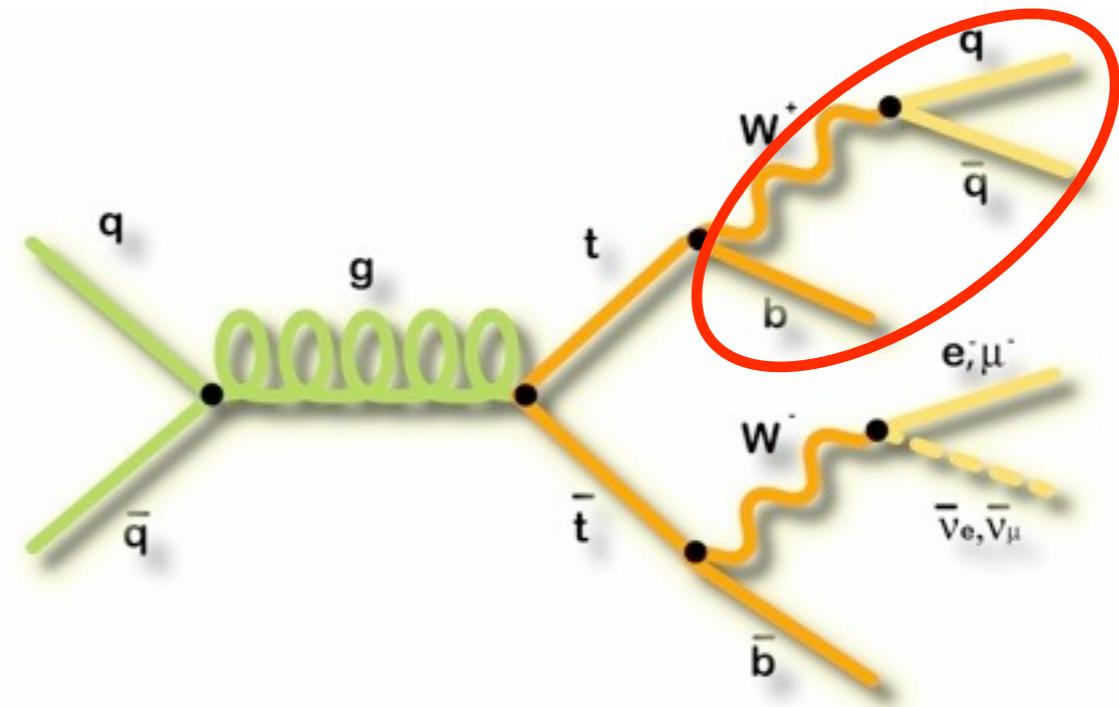
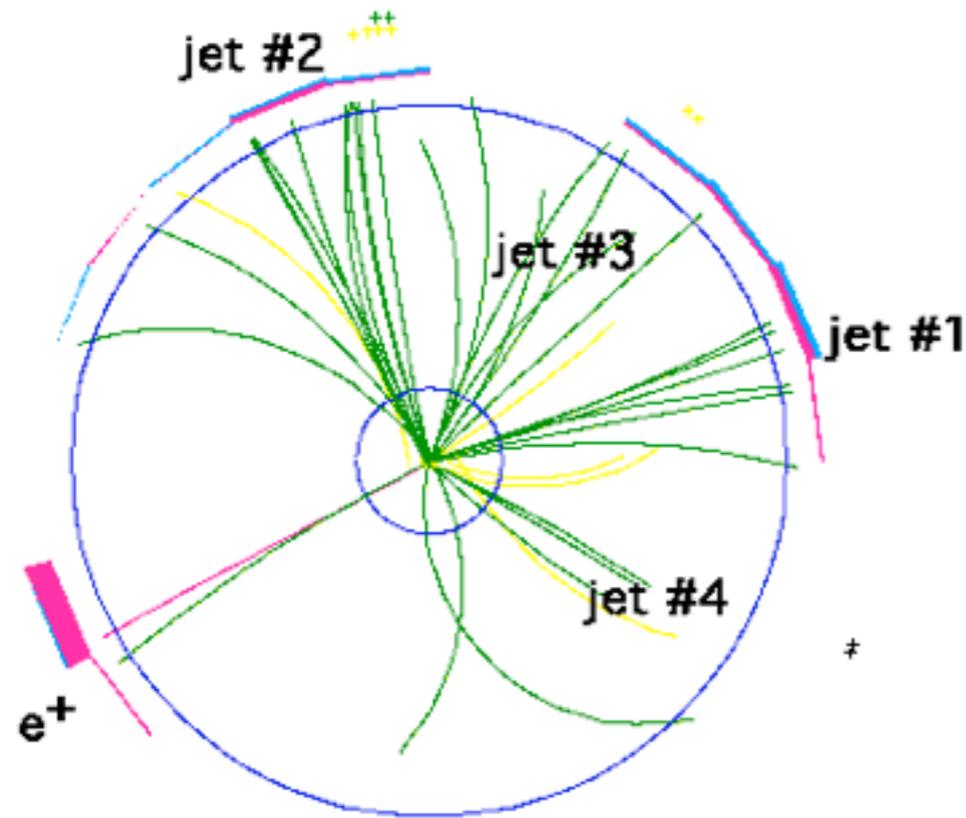
$$\chi^2 = \sum_{i=l,jets} \frac{(p_t^{i,meas} - p_t^{i,fit})^2}{\sigma_i^2} + \sum_{j=x,y} \frac{(p_j^{UE,meas} - p_j^{UE,fit})^2}{\sigma_j^2} + \frac{(M_{jj} - M_W)^2}{\Gamma_W^2} + \frac{(M_{lv} - M_W)^2}{\Gamma_W^2} + \frac{(M_{bjj} - M_{fit})^2}{\Gamma_t^2} + \frac{(M_{blv} - M_{fit})^2}{\Gamma_t^2}$$

Event Reconstruction



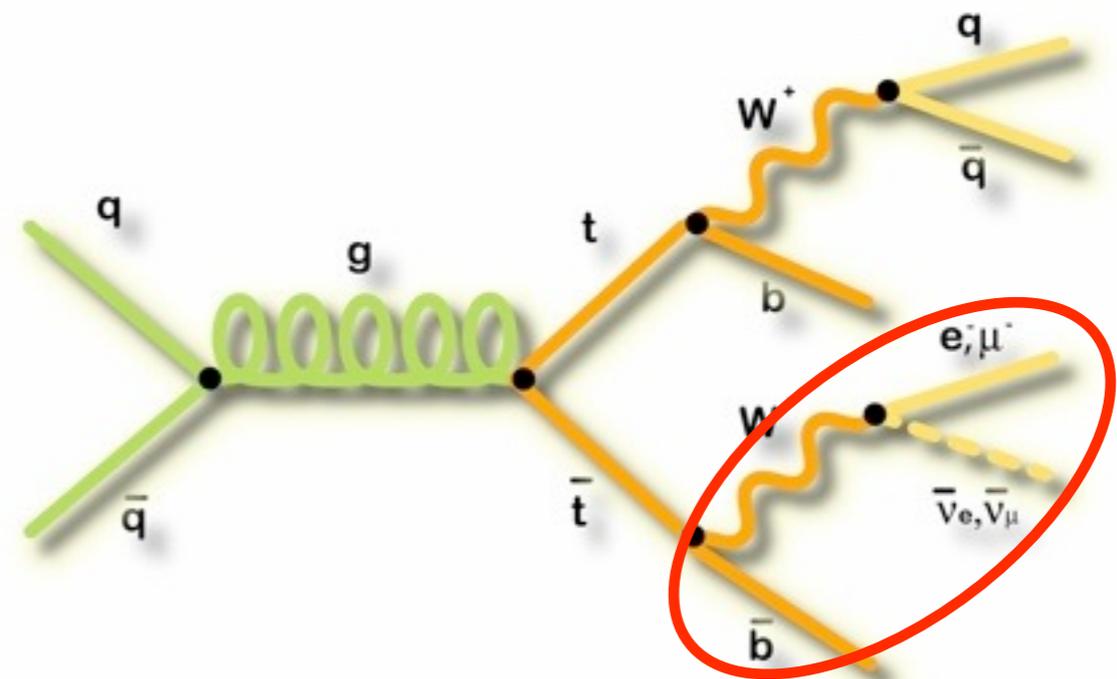
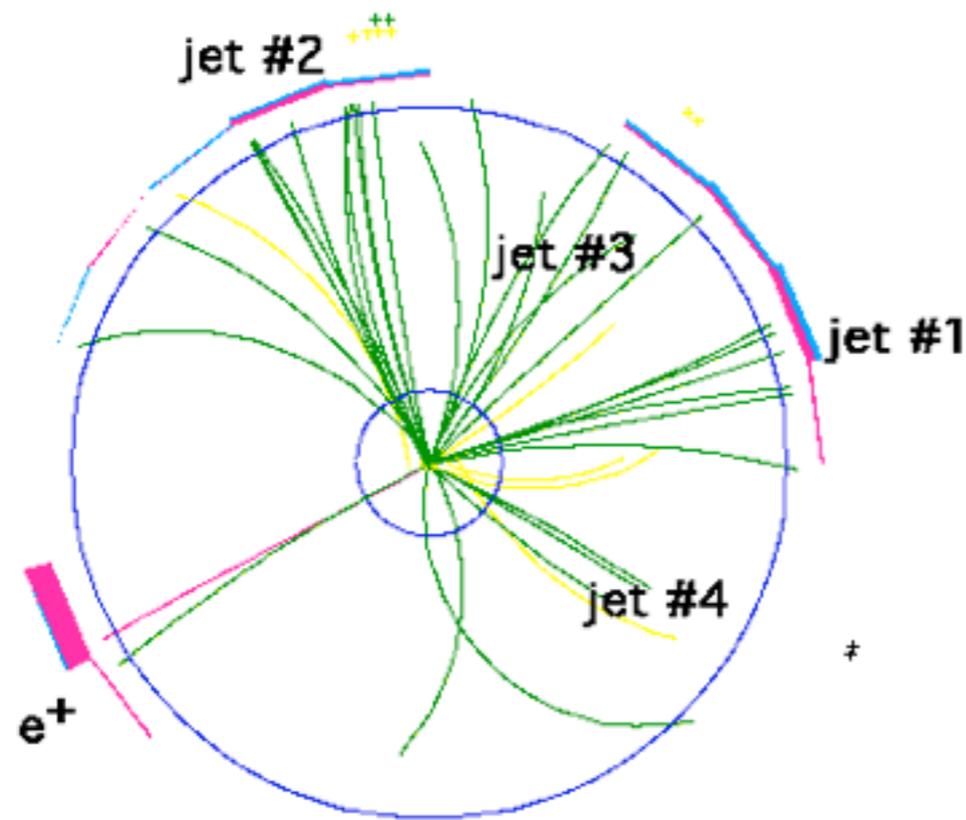
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Event Reconstruction



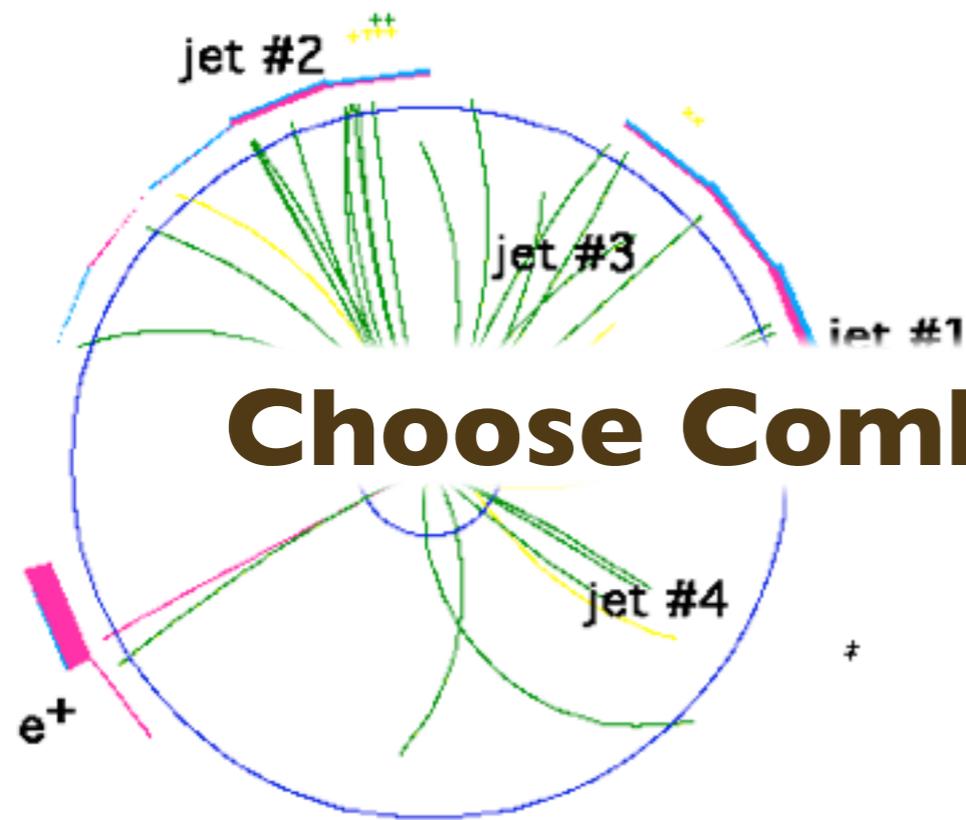
$$\chi^2 = \sum_{i=l,jets} \frac{(p_t^{i,meas} - p_t^{i,fit})^2}{\sigma_i^2} + \sum_{j=x,y} \frac{(p_j^{UE,meas} - p_j^{UE,fit})^2}{\sigma_j^2} + \frac{(M_{jj} - M_W)^2}{\Gamma_W^2} + \frac{(M_{lv} - M_W)^2}{\Gamma_W^2} + \frac{(M_{bjj} - M_{fit})^2}{\Gamma_t^2} + \frac{(M_{blv} - M_{fit})^2}{\Gamma_t^2}$$

Event Reconstruction



$$\chi^2 = \sum_{i=l,jets} \frac{(p_t^{i,meas} - p_t^{i,fit})^2}{\sigma_i^2} + \sum_{j=x,y} \frac{(p_j^{UE,meas} - p_j^{UE,fit})^2}{\sigma_j^2} + \frac{(M_{jj} - M_W)^2}{\Gamma_W^2} + \frac{(M_{lv} - M_W)^2}{\Gamma_W^2} + \frac{(M_{bjj} - M_{fit})^2}{\Gamma_t^2} + \frac{(M_{blv} - M_{fit})^2}{\Gamma_t^2}$$

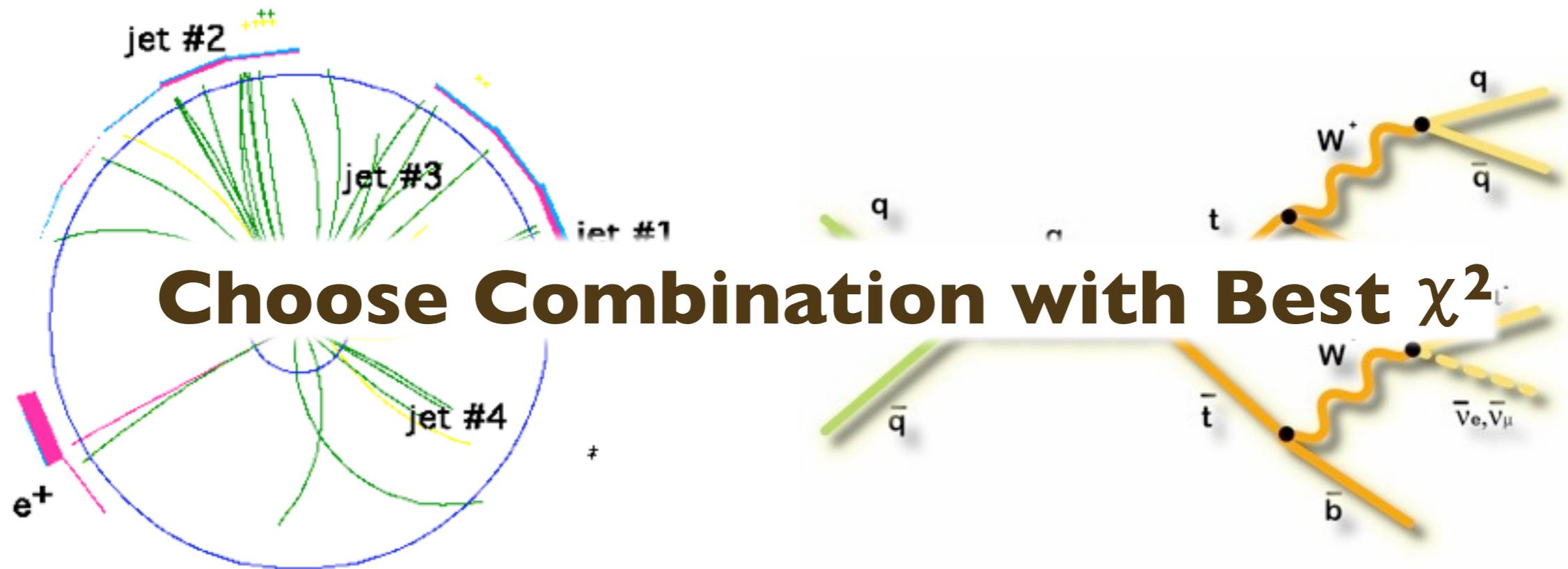
Event Reconstruction



Choose Combination with Best χ^2

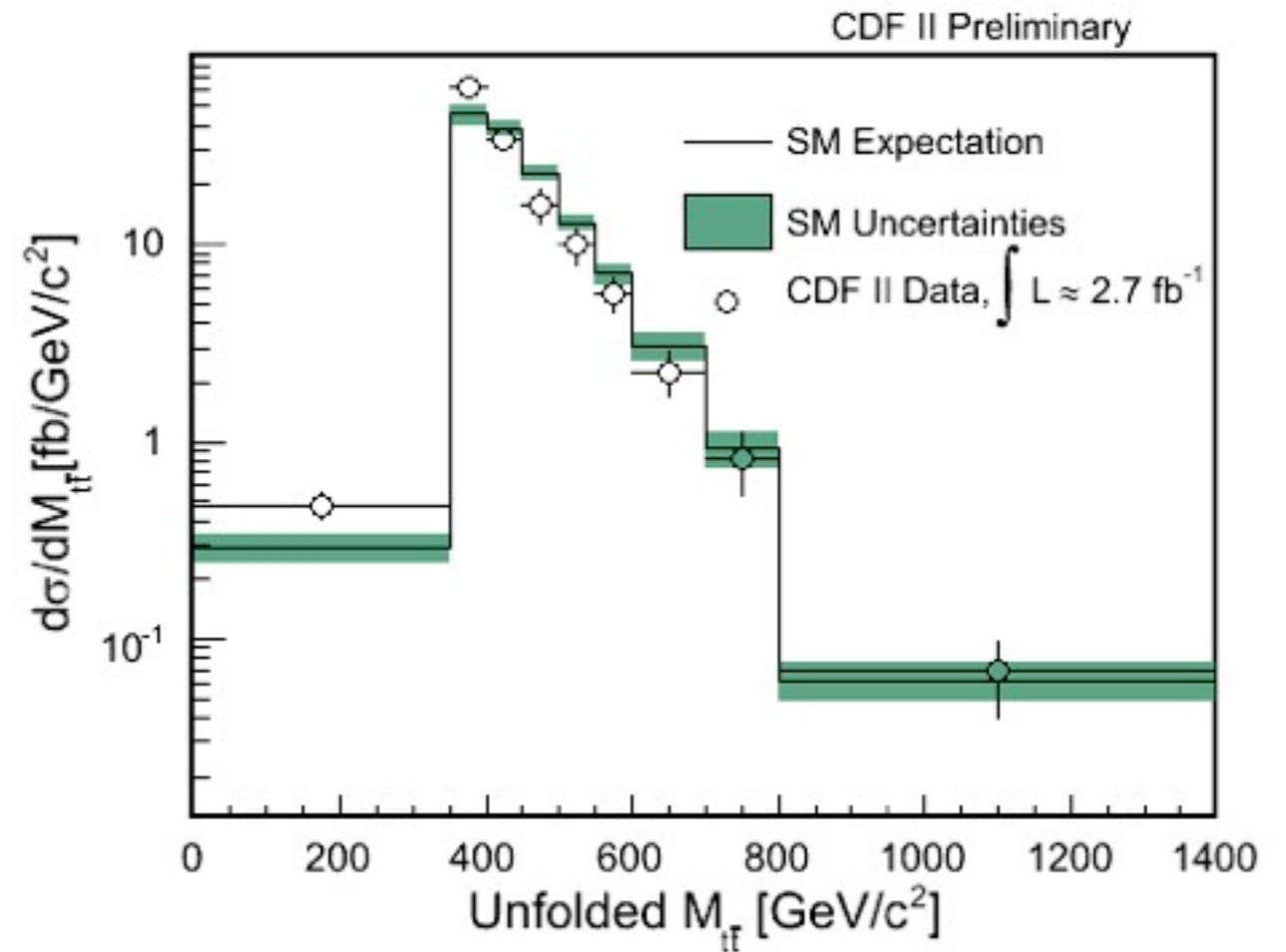
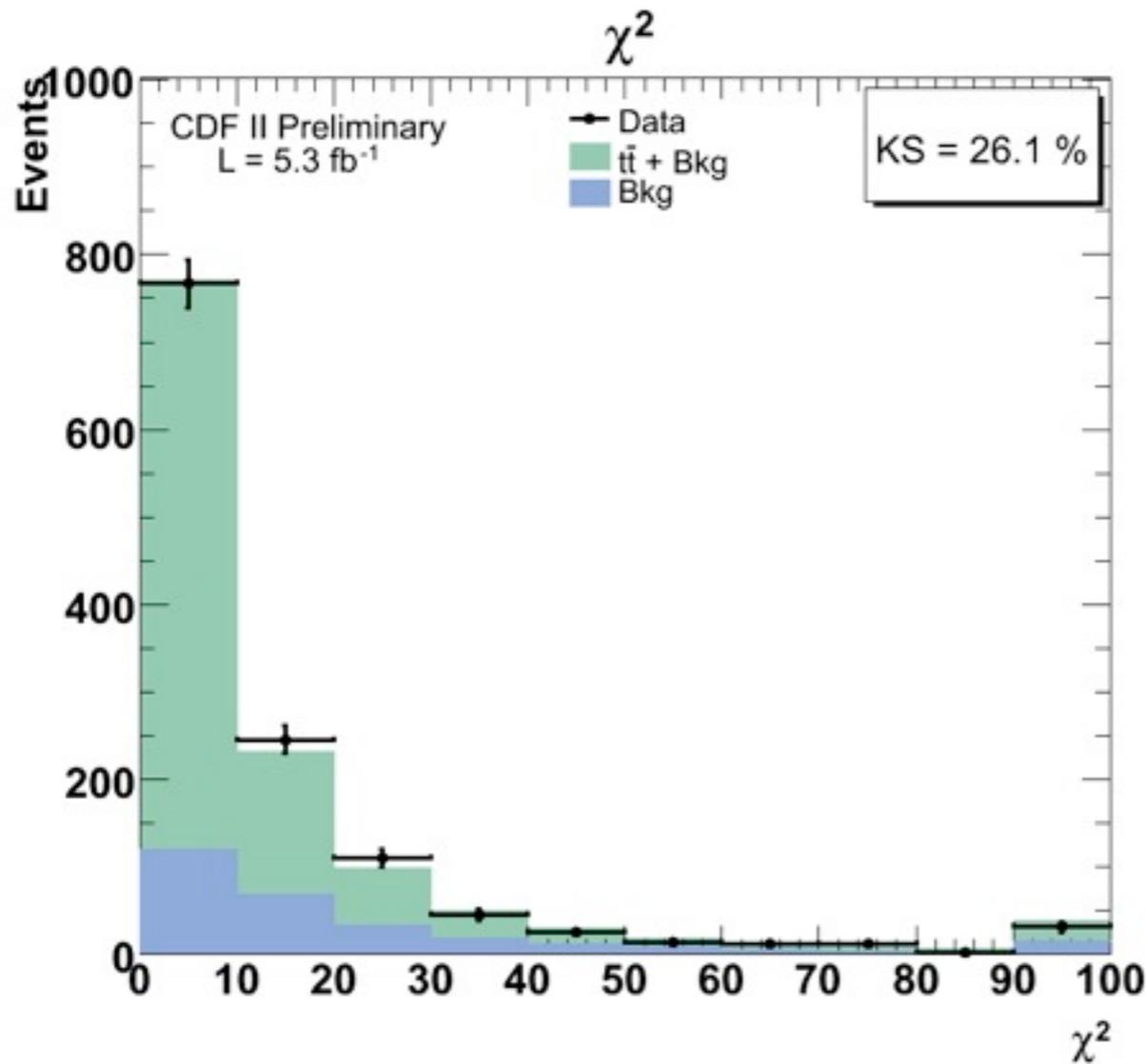
$$\chi^2 = \sum_{i=l,jets} \frac{(p_t^{i,meas} - p_t^{i,fit})^2}{\sigma_i^2} + \sum_{j=x,y} \frac{(p_j^{UE,meas} - p_j^{UE,fit})^2}{\sigma_j^2} + \frac{(M_{jj} - M_W)^2}{\Gamma_W^2} + \frac{(M_{lv} - M_W)^2}{\Gamma_W^2} + \frac{(M_{bjj} - M_{fit})^2}{\Gamma_t^2} + \frac{(M_{blv} - M_{fit})^2}{\Gamma_t^2}$$

Event Reconstruction



All particle energies and angles are available after reconstruction

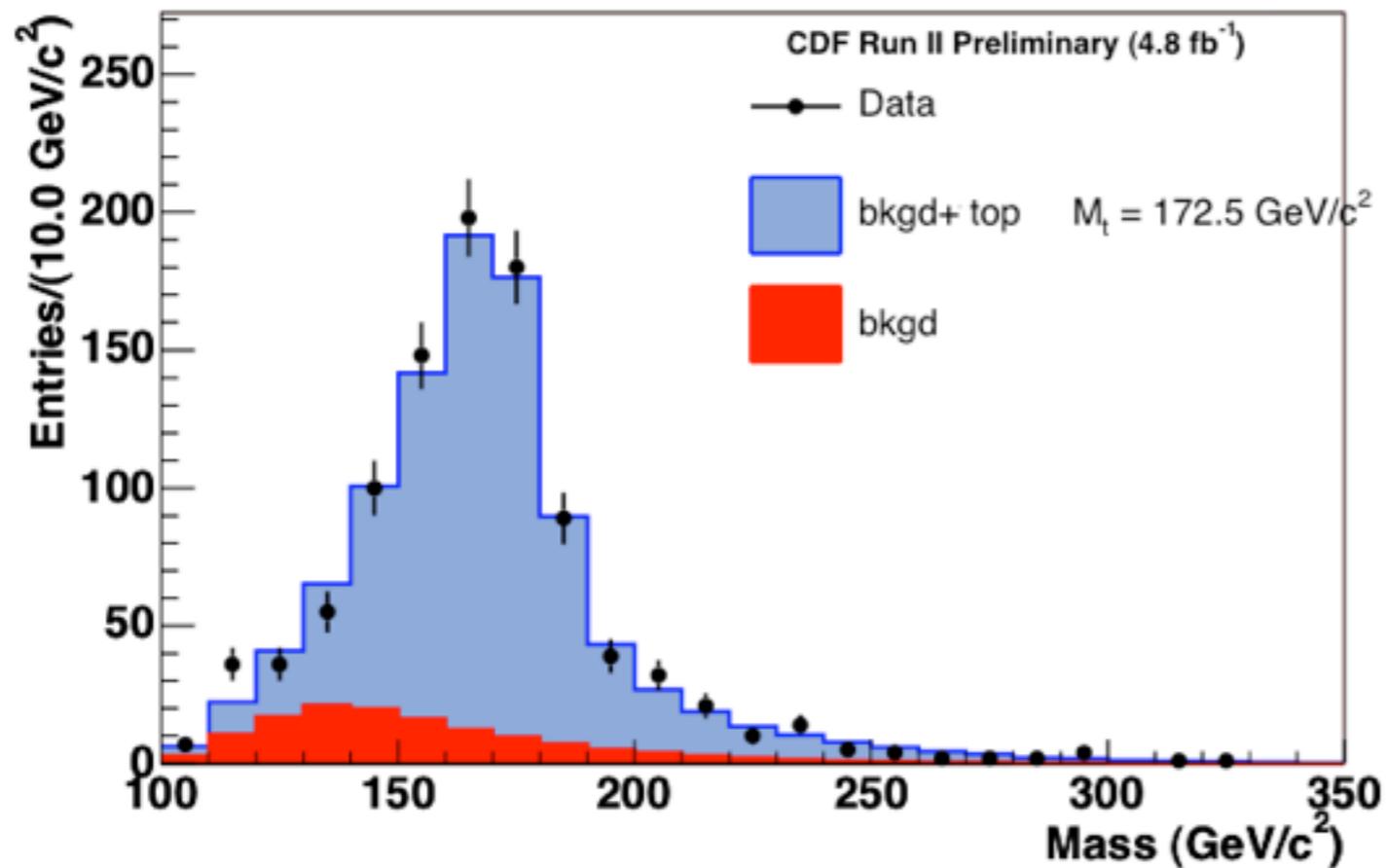
Event Reconstruction



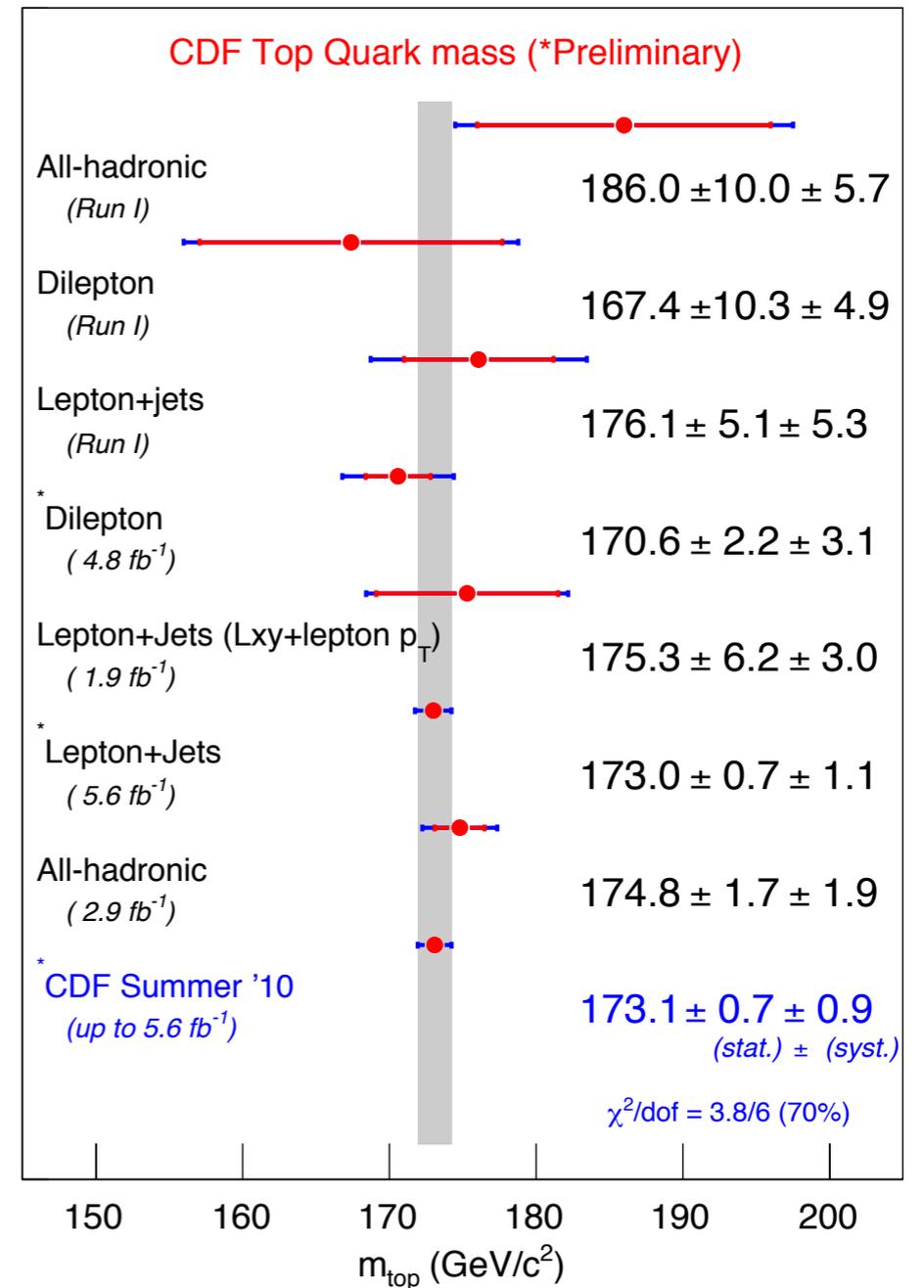
<http://www-cdf.fnal.gov/physics/new/top/2010/tprop/Afb/validation.html>

Reconstructed Mass

Used in CDF Top Mass Measurement

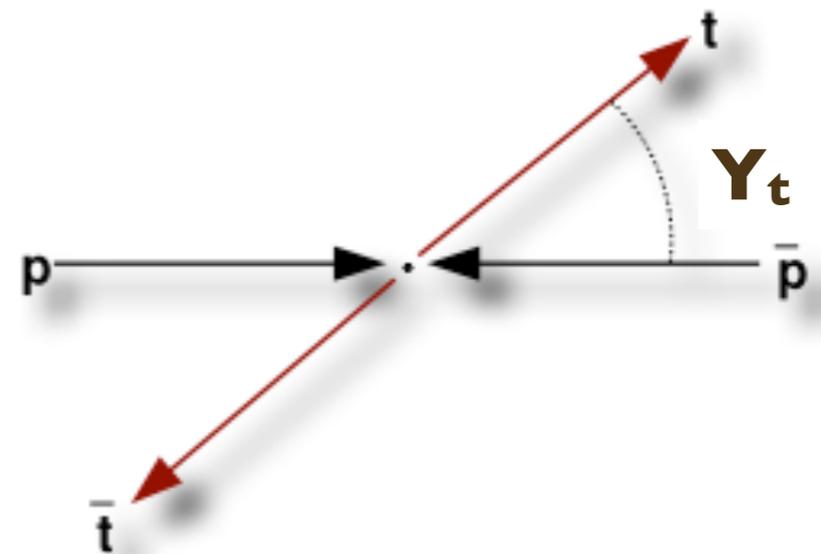


$$M_T = 172.0 \pm 1.5 \text{ GeV}$$



Top Angle

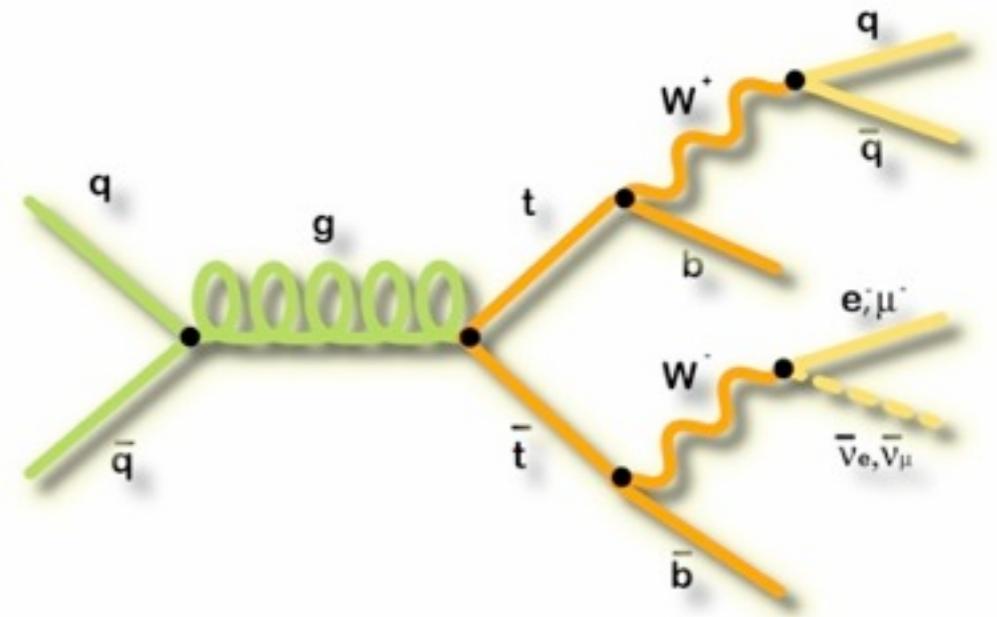
- Use the top rapidity (Y_t) to measure the asymmetry
- Unfortunately, we do not reconstruct top or antitop, rather $t \rightarrow l\nu b$ and $t \rightarrow jjb$
- Rapidity difference (ΔY) of t and \bar{t} is proportional to Y_t in $t\bar{t}$ rest frame
- Measure A_{FB} using ΔY



$$\Delta Y = q_{lep} \cdot (Y_{lep} - Y_{had})$$

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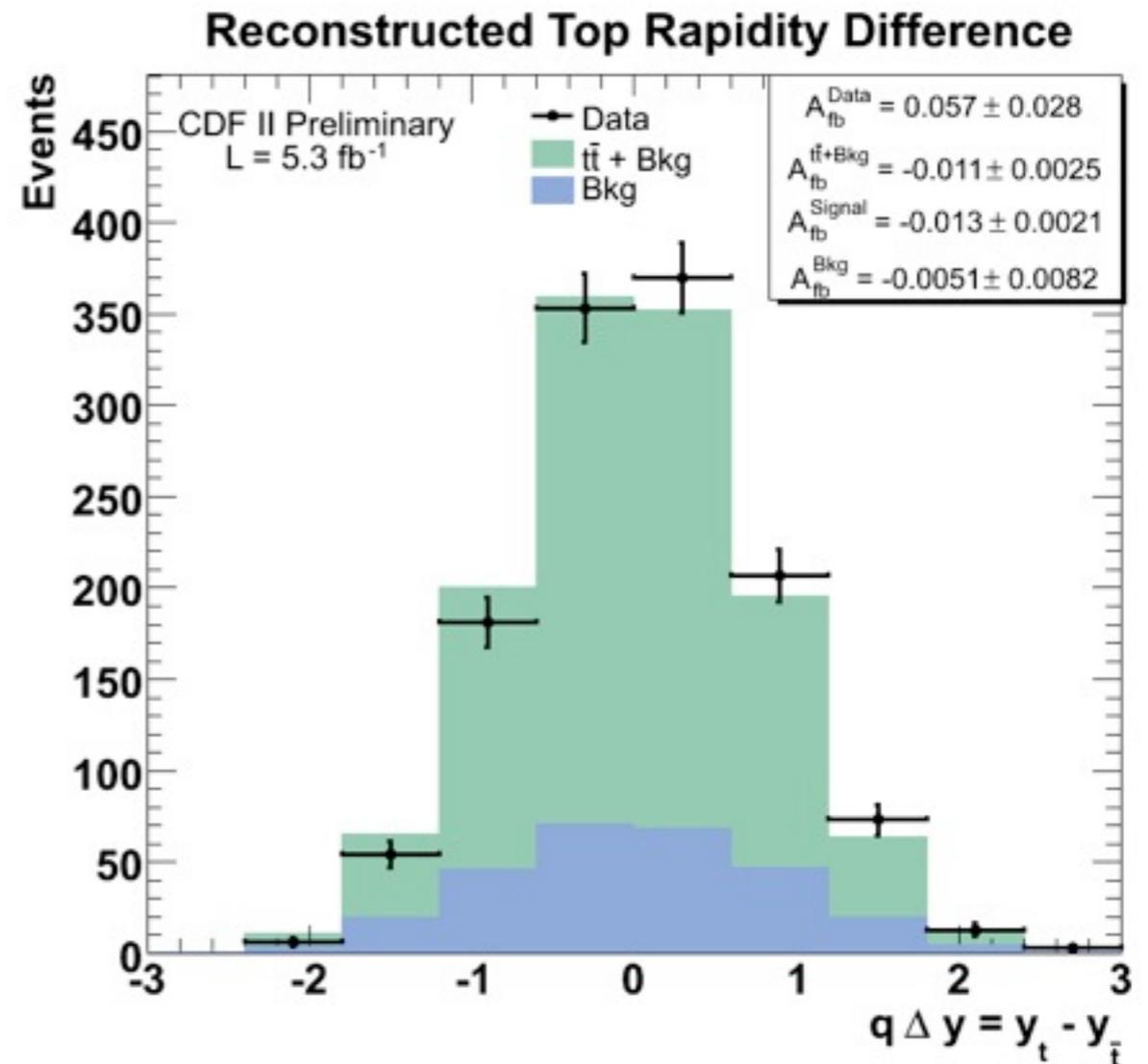
$$\Delta Y = q_{lep} \cdot (Y_{lep} - Y_{had})$$

Top Angle

Uncorrected

$$A_{\text{FB}} = 5.7 \pm 2.8 \%$$

- The shape in data can be biased and diluted by backgrounds, acceptance, and poor reconstruction
- Each effect has to be corrected to compare our measurement to theory

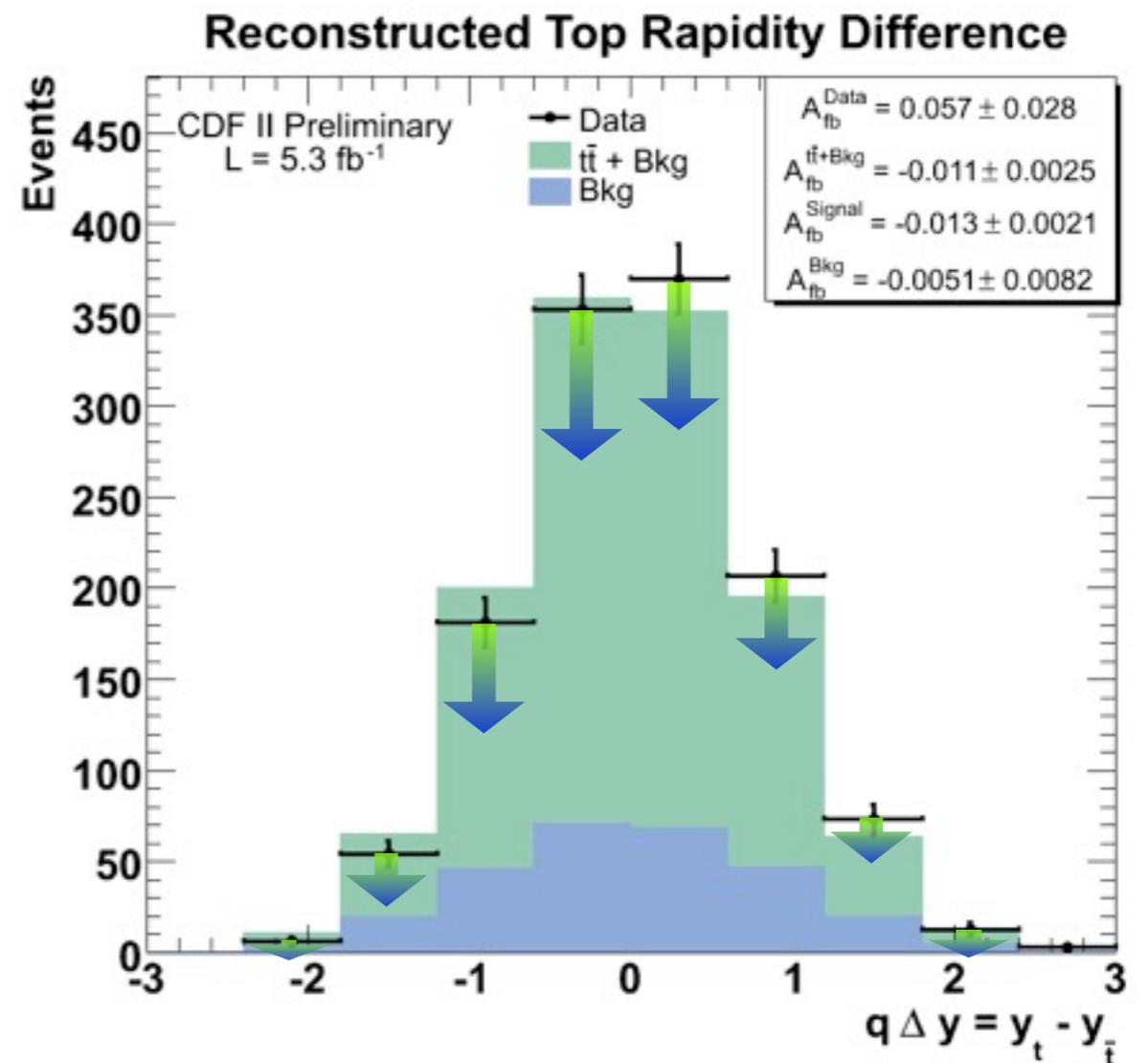


Backgrounds

- Subtract predicted background shape from data
- Resulting distribution is the $t\bar{t}$ production angle after selection and reconstruction

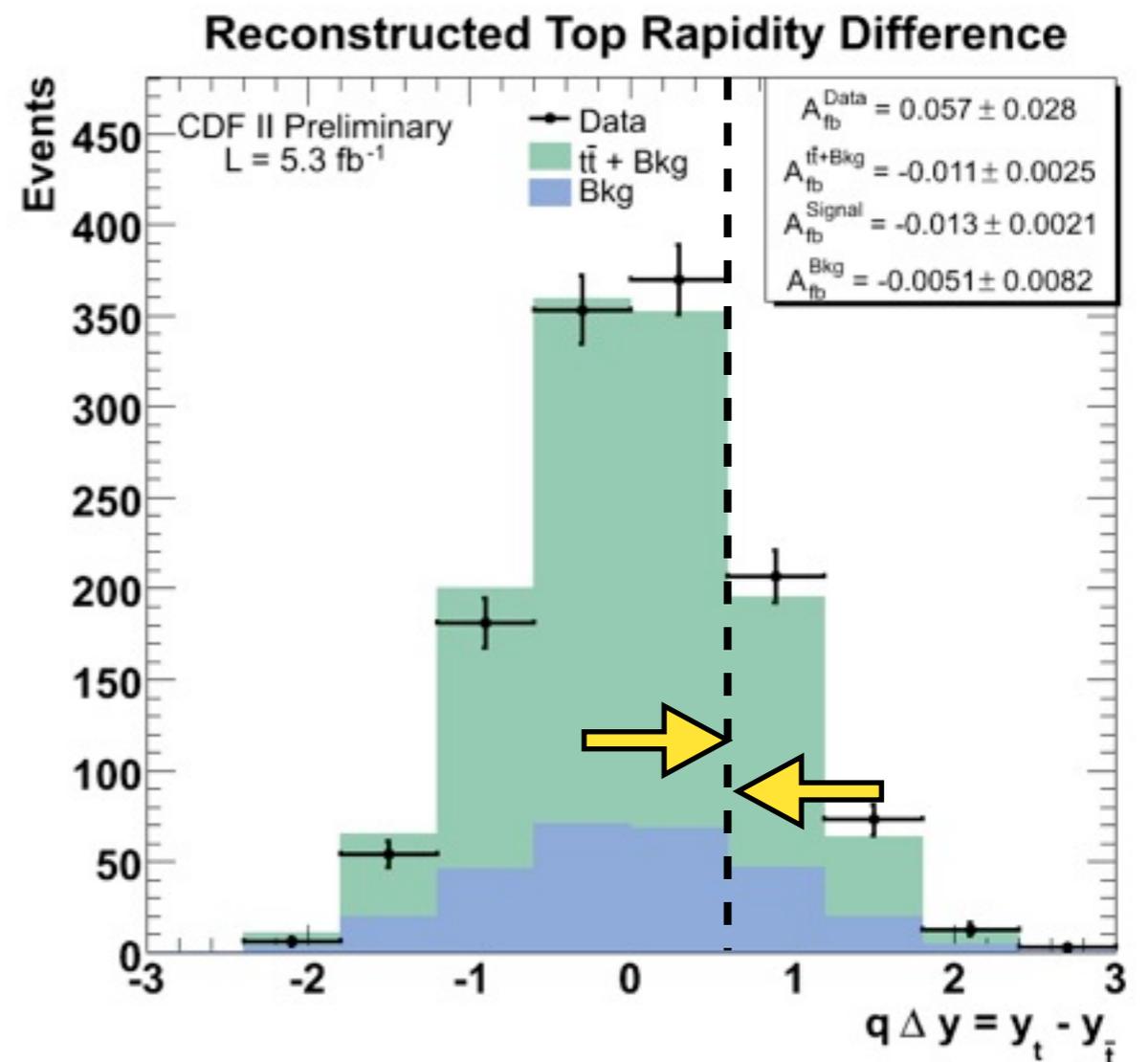
Bkg Corrected

$$A_{FB} = 7.5 \pm 3.7 \%$$



Correcting Reconstruction

- **Mis-reconstruction of the top production angle will dilute or skew the true asymmetry**
- **Can correct for this by simulating smearing in Monte Carlo and applying to data**

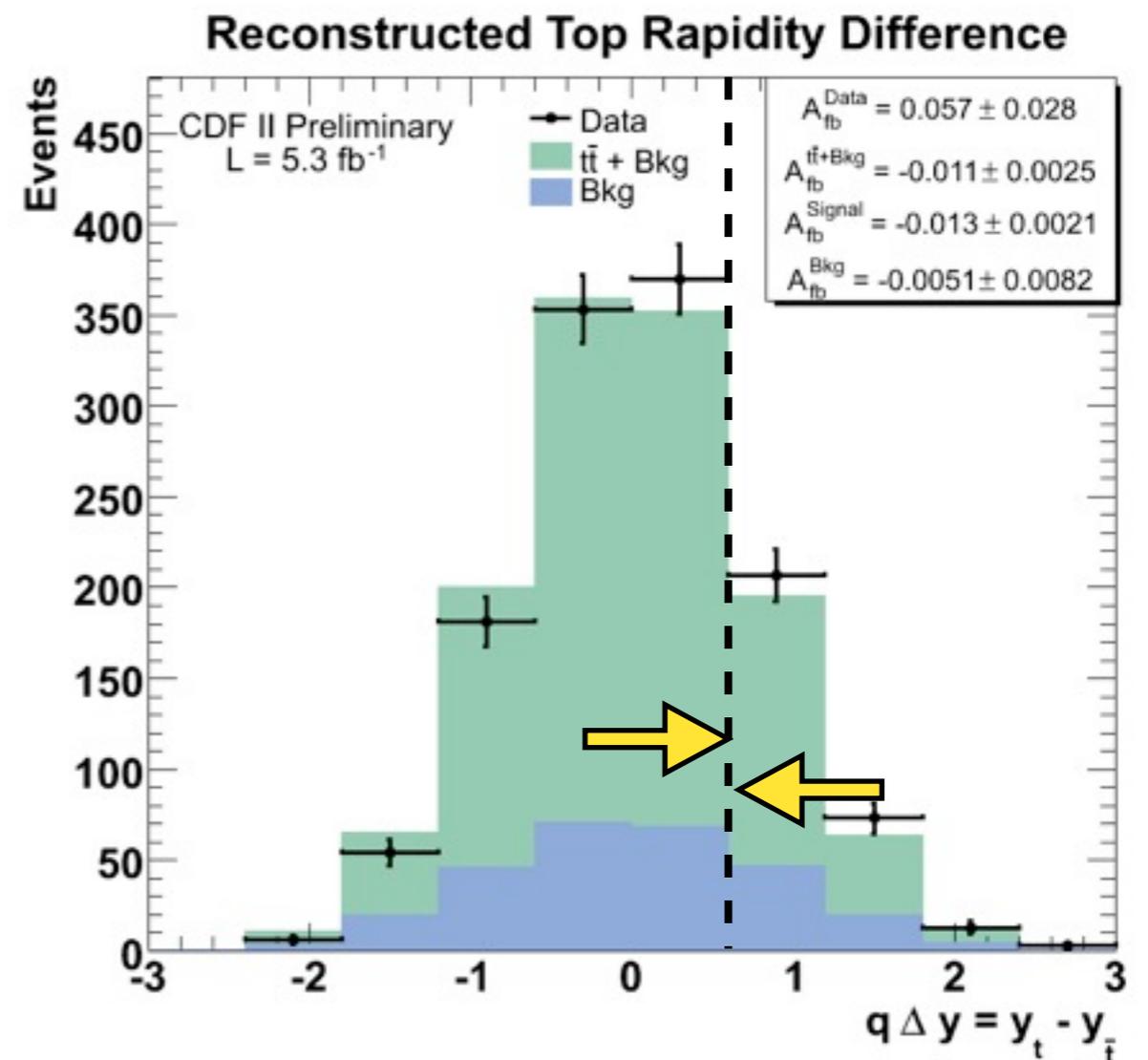


Correcting Reconstruction

- Derive smearing matrix (S) from MC

$$[Recon] = \begin{bmatrix} s_{0,0} & s_{0,1} & \dots & s_{0,nbins} \\ s_{1,0} & s_{1,1} & \dots & \dots \\ \dots & \dots & \dots & \dots \\ s_{nbins,0} & \dots & \dots & s_{nbins,nbins} \end{bmatrix} [True]$$

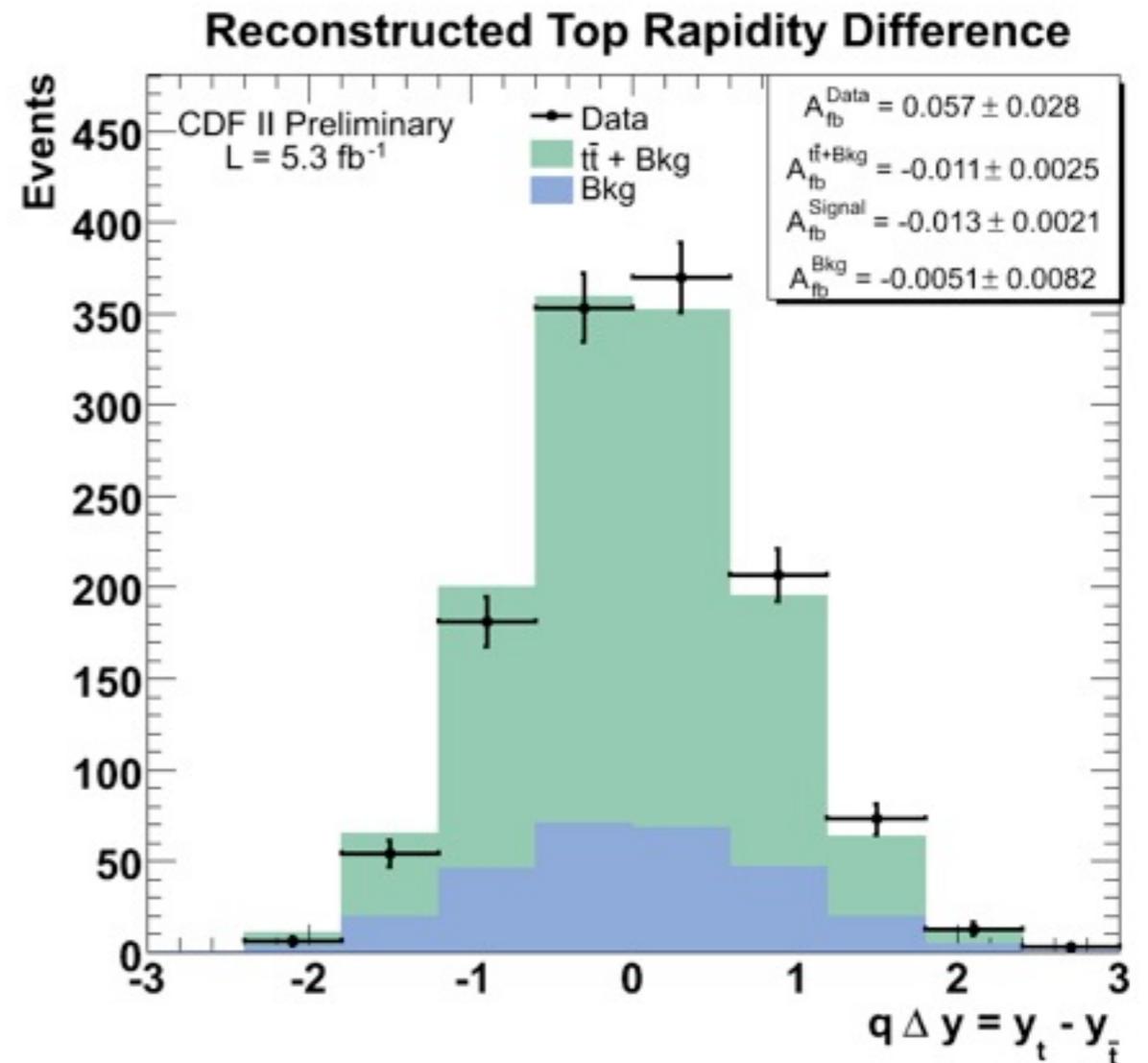
- The matrix is inverted to correct for smearing



Correcting Acceptance

- Similarly, detector acceptance is represented as a matrix (A)

$$[Selected] = \begin{bmatrix} \epsilon_0 & 0 & 0 & 0 \\ 0 & \epsilon_1 & 0 & 0 \\ 0 & 0 & \dots & 0 \\ 0 & 0 & 0 & \epsilon_{nbins} \end{bmatrix} [True]$$



Putting it All Together

- **Cascade correction matrices and apply to the background corrected data**
- **Result can then be directly compared to the Standard Model**

$$\text{Corrected} = \mathbf{A}^{-1} \cdot \mathbf{S}^{-1} \cdot (\text{Data} - \text{Bkg})$$

Bin-to-Bin Oscillations

- **Simple Example of a smearing matrix**

$$\begin{bmatrix} d_1 \\ d_2 \end{bmatrix} = \frac{1}{2} \cdot \begin{bmatrix} 1 + \epsilon & 1 - \epsilon \\ 1 - \epsilon & 1 + \epsilon \end{bmatrix} \cdot \begin{bmatrix} t_1 \\ t_2 \end{bmatrix}$$

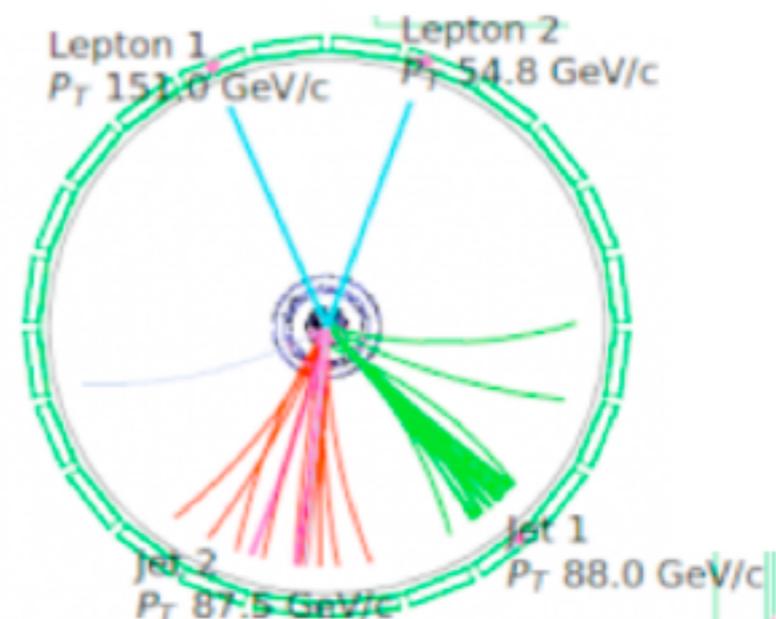
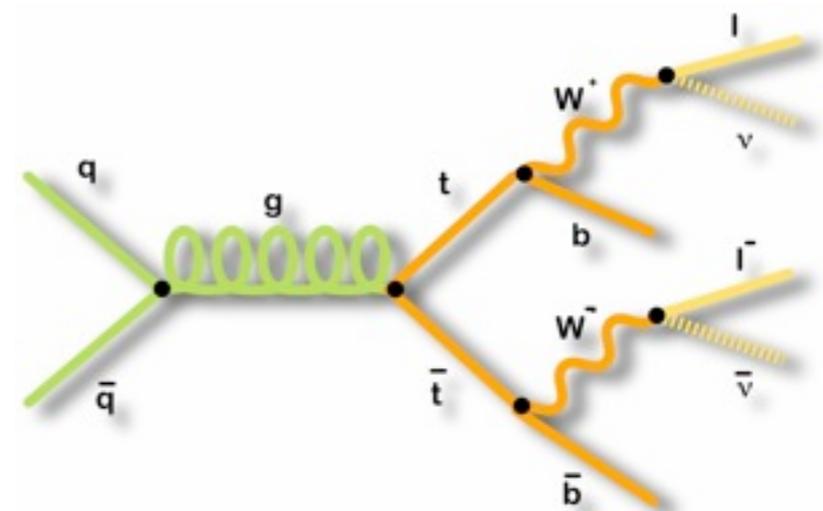
- **Inverted to solved for truth, you get**

$$\begin{bmatrix} t_1 \\ t_2 \end{bmatrix} = \frac{d_1 + d_2}{2} \cdot \begin{bmatrix} 1 \\ 1 \end{bmatrix} + \frac{d_1 - d_2}{2\epsilon} \cdot \begin{bmatrix} 1 \\ -1 \end{bmatrix}$$

- **If $d_1 - d_2$ are not statistically distinct, then bad smearing can dominate the solution! Need a way to dampen these terms...**

A_{FB} in Dileptons

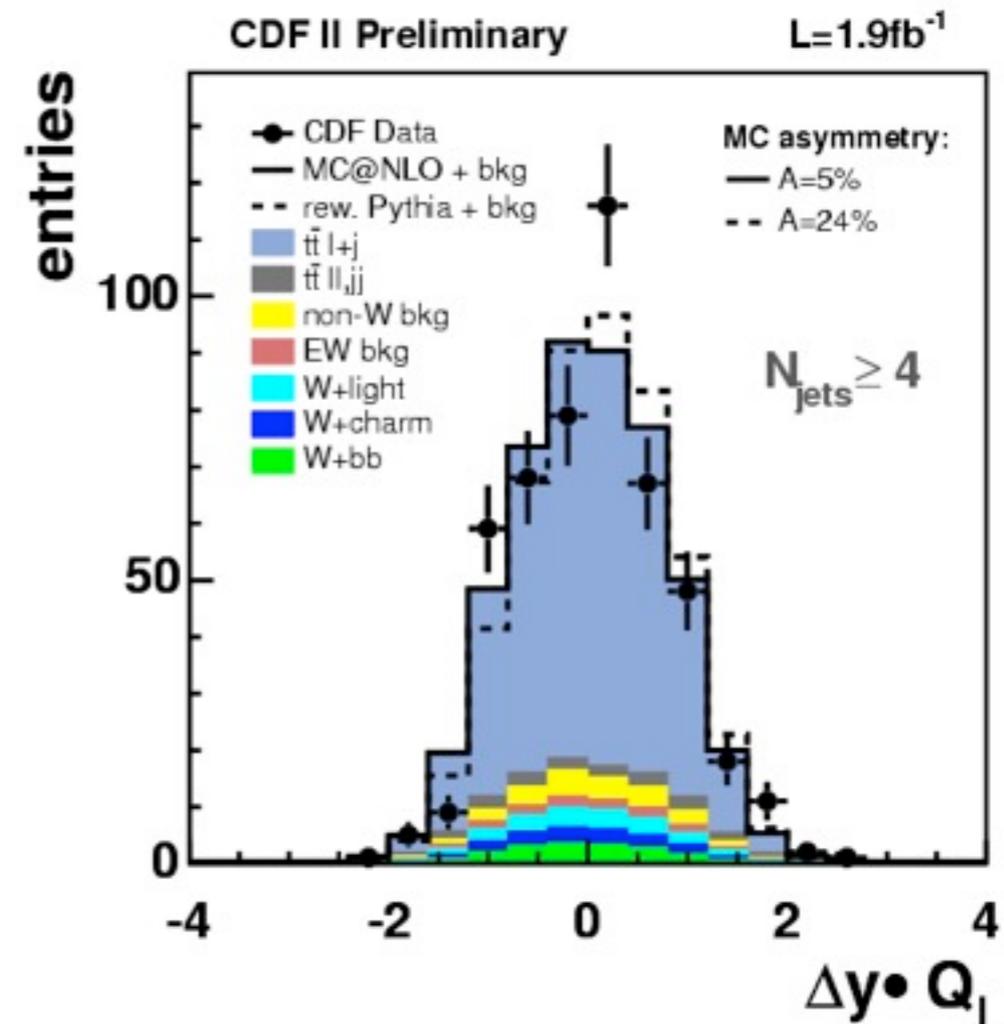
- Leptons well measured, but missing two neutrino momenta and match jets to b quarks
- Energy, momentum constraints lead to 4 possible solutions
- Best solution chosen from likelihood based on PDF's for P_z^{tt} , P_T^{tt} , and M_{tt}
- Top and anti-top direction both fully reconstructed



Other Signs?

- **Alternative measurement at CDF (Karlsruhe)**
- **Measured in $t\bar{t}$ rest frame**
- **Performed with 1.9 fb^{-1}**

$$A_{\text{FB}} = 24 \pm 14_{\text{stat+sys}} \%$$



$$A_{\text{FB}}^{\text{SM}} = 7 \pm 2 \%$$