



Top Quark Mass Measurement with a Matrix-Element Method in the Dilepton Channel

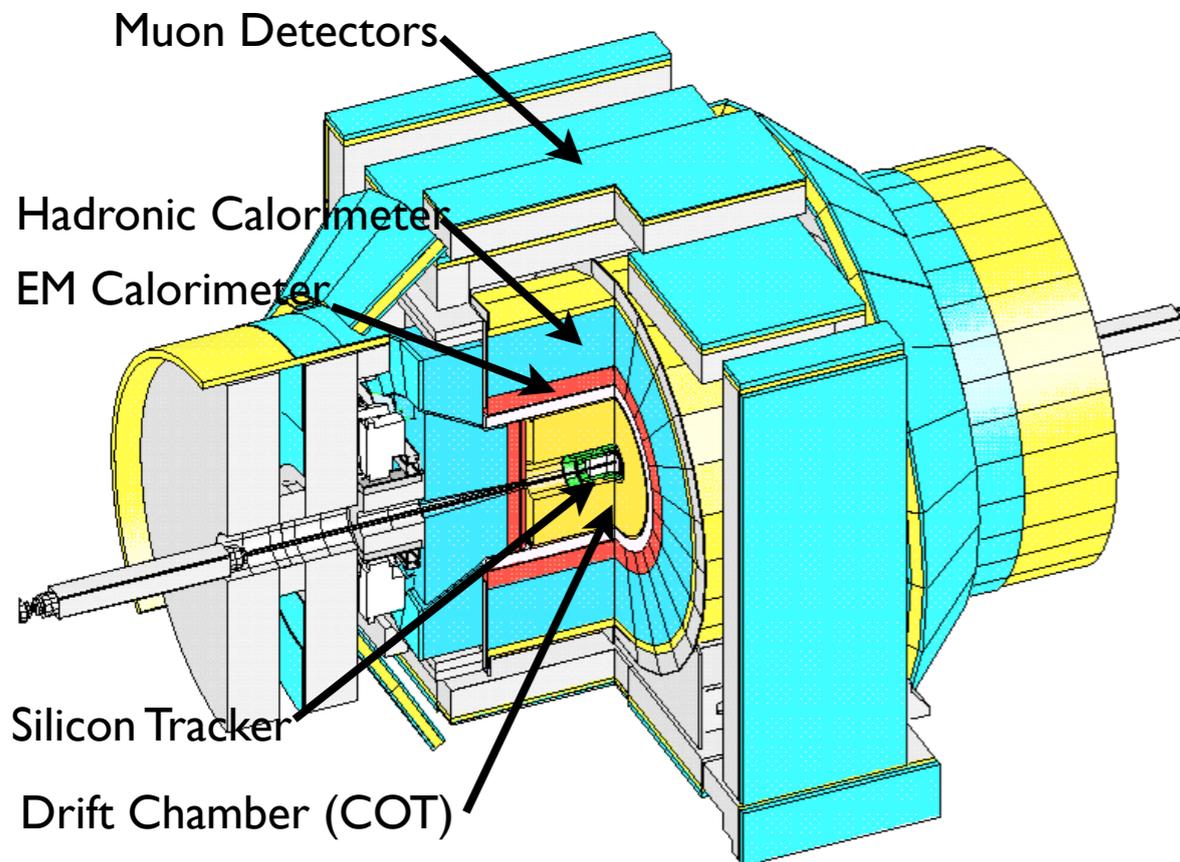
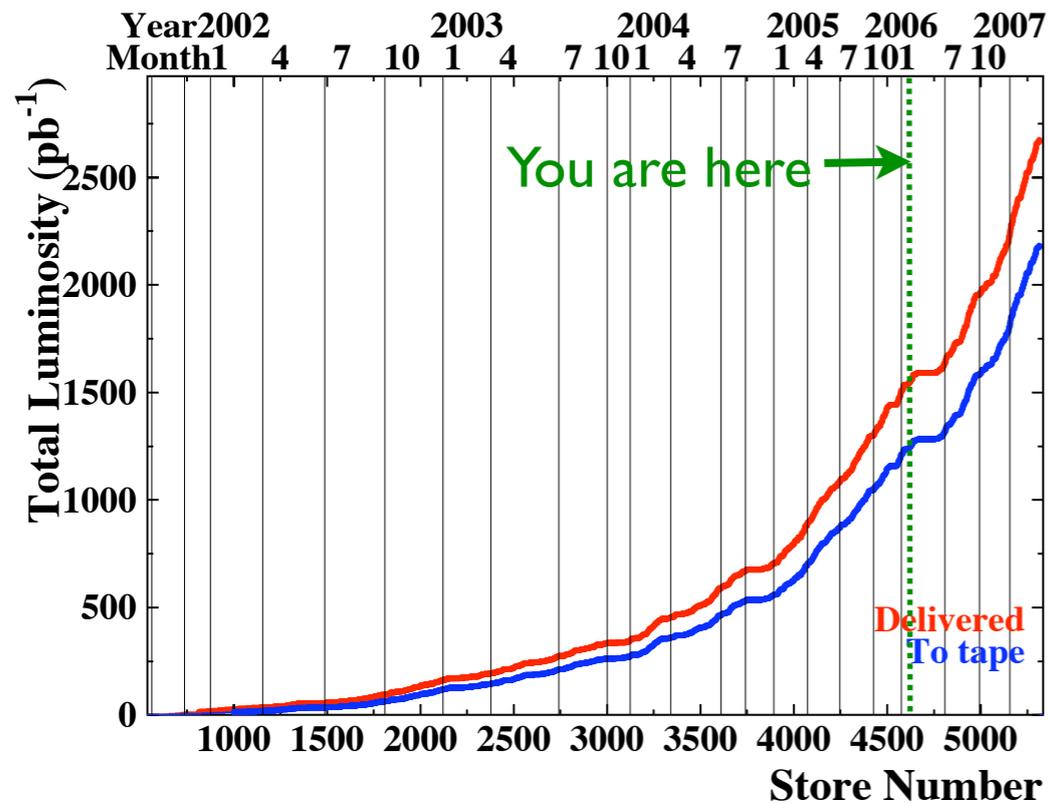
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On Behalf of the CDF Collaboration

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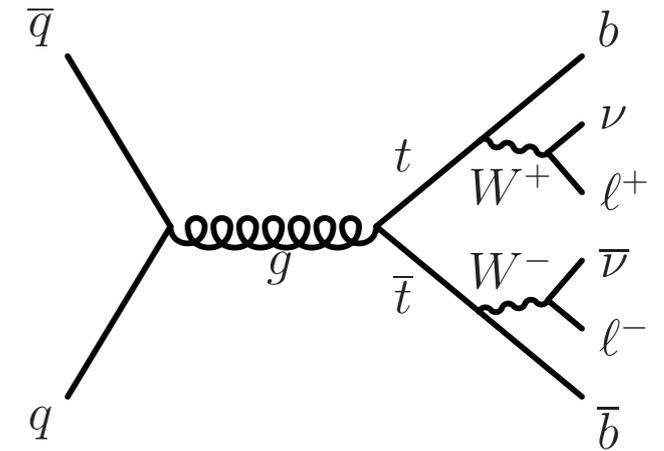
Tevatron and CDF detector



- Tevatron
 - Peak luminosity $>2.8 \times 10^{32} \text{ cm}^{-2}\text{s}^{-1}$
 - 2.5 fb^{-1} delivered to experiments
- CDF Detector - General purpose detector
 - Precision tracking (Silicon + COT)
 - EM and Hadronic calorimeters
 - Muon detectors (extended for Run II)
 - $>2.0 \text{ fb}^{-1}$ recorded at CDF
 - Measurement shown uses 1 fb^{-1} (up to March 2006)

Top quark decay: the dilepton channel

- Top quarks are primarily pair produced at Tevatron
 - Decay channel is defined by W decay modes
- Both W s decay leptonically in **~5%** of all decays
 - 2 leptons (e or μ), 2 jets (from b -quarks), large missing \cancel{E}_T from ν s



Advantages

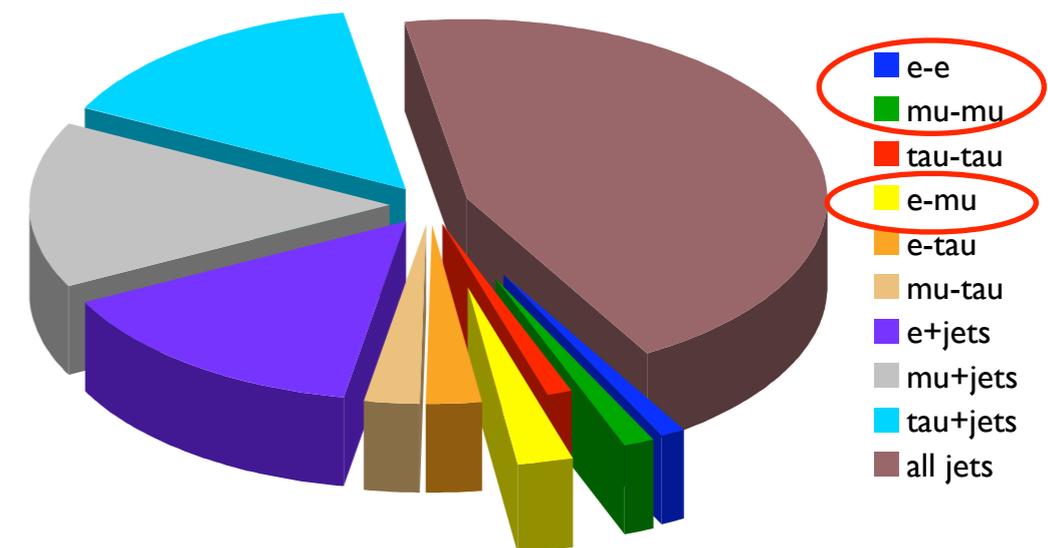
- Clean: little background without need for b -tagging
- Least jets of any channel (less reliant on JES, less ambiguity in jets)

Disadvantages

- Low statistics
- 2 ν s escape undetected— underconstrained system

Backgrounds

- Drell-Yan + jets (DY)
- Diboson + jets
- Mis-ID leptons (“fakes”)



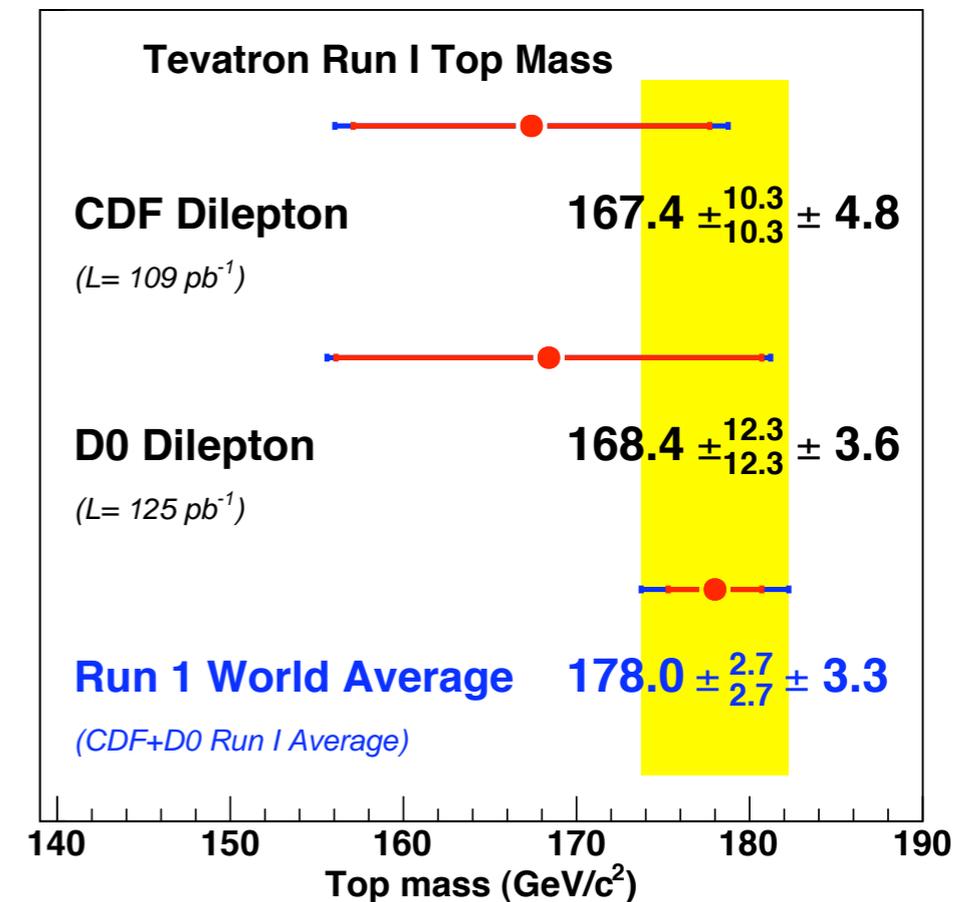
Measuring M_{top} in the dilepton channel

Important measurement

- Contributes to overall knowledge of top mass
- Verify that we are measuring SM top
- If results across channels inconsistent, new physics might be in sample

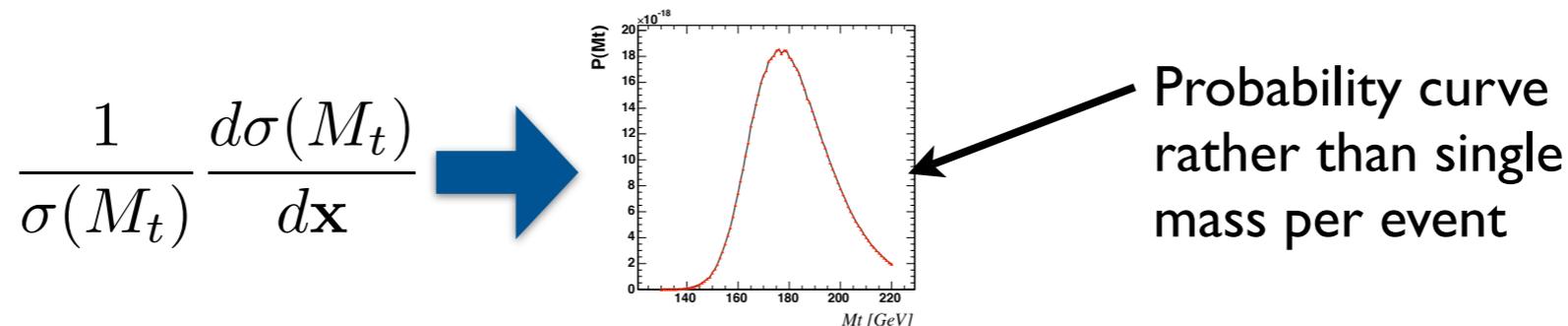
Difficult channel to work in

- Low statistics
- Two neutrinos escape undetected
- Only one missing transverse energy measurement
 - Kinematically under-constrained
- Forced to make assumptions and integrate
- No hadronic W to make *in situ* JES measurement



The matrix element method

- Use differential cross-section to calculate probability of event coming from M_{top}



- Formulate differential cross-section using **LO matrix element** and **transfer functions**

$$\frac{d\sigma(M_t)}{d\mathbf{x}} = \int d\Phi |\mathcal{M}_{t\bar{t}}(p_i; M_t)|^2 \prod W(p_i, \mathbf{x}) f_{PDF}(q_1) f_{PDF}(q_2)$$

- Transfer functions link measured quantities \mathbf{x} to parton-level ones, p_i
 - Jet energy-parton energy
 - $t\bar{t} p_T$ - measured recoil
- Perform integrals over unknown quantities (8)
- Simplifying assumptions made for tractability
 - e.g. lepton momenta and jet angles perfectly measured
- Use similar differential cross-sections for background processes
 - Final probability becomes weighted sum of signal and background probabilities

Integrals still take
2-3 hours per event!

$$P(\mathbf{x}|M_t) = P_s(\mathbf{x}|M_t)p_s + P_{bg_1}(\mathbf{x})p_{bg_1} + P_{bg_2}(\mathbf{x})p_{bg_2} + \dots$$

Dataset used

- 1 fb⁻¹ of data collected up to March 2006 at CDF
- Basic selection: 2 high- p_T (>20 GeV/c) leptons, 2 high- E_T (>15 GeV) jets, large \cancel{E}_T (>25 GeV)
- Additional cuts to help reduce background
 - Elevate \cancel{E}_T requirement when m_{ll} is close to Z mass
 - Require scalar sum of energies in event, $H_T > 200$ GeV

Source	N_{evs}
$t\bar{t}$ ($M_t=175$ GeV/c ² , $\sigma=6.7$ pb)	50.2
$Z \rightarrow ee/\mu\mu$	10.9
Fakes	8.7
WW/WZ	5.1
$Z \rightarrow \tau\tau$	2.2
Total	77.1
<i>Observed</i> (1.0 fb ⁻¹)	78

Uncertainties

Statistical Uncertainty

- Expected for $M_{\text{top}}=175 \text{ GeV}/c^2$, $\sigma = 5.0 \text{ GeV}/c^2$
- Expected for $M_{\text{top}}=165 \text{ GeV}/c^2$, $\sigma = 4.2 \text{ GeV}/c^2$

Systematic Uncertainty

Source	ΔM_{top} (GeV/ c^2)
Jet Energy Scale	3.5
Generator	0.9
Method	0.6
Sample Composition	0.7
Background Statistics	0.7
Background Modeling	0.2
FSR	0.3
ISR	0.3
PDFs	0.8
<i>Total</i>	3.9

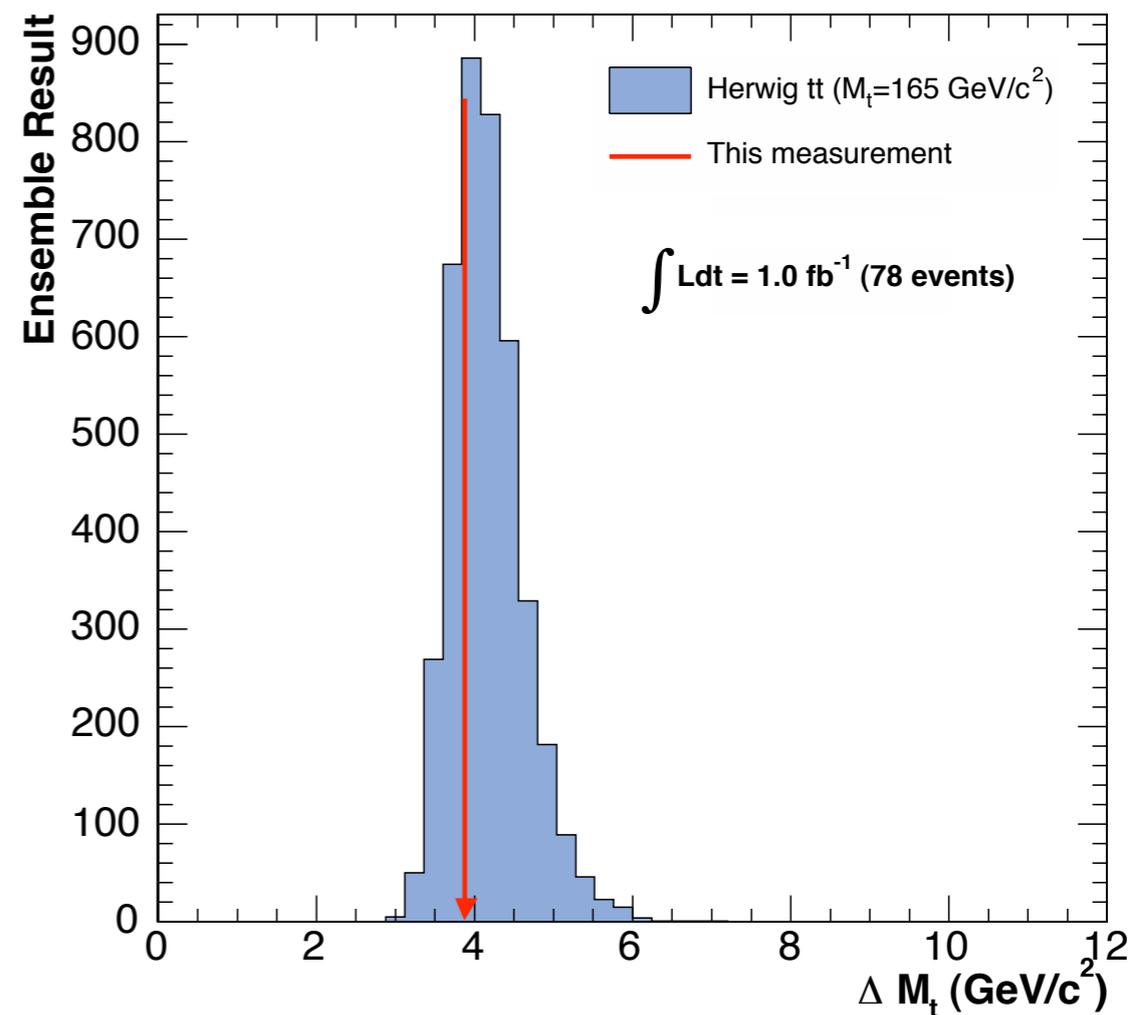
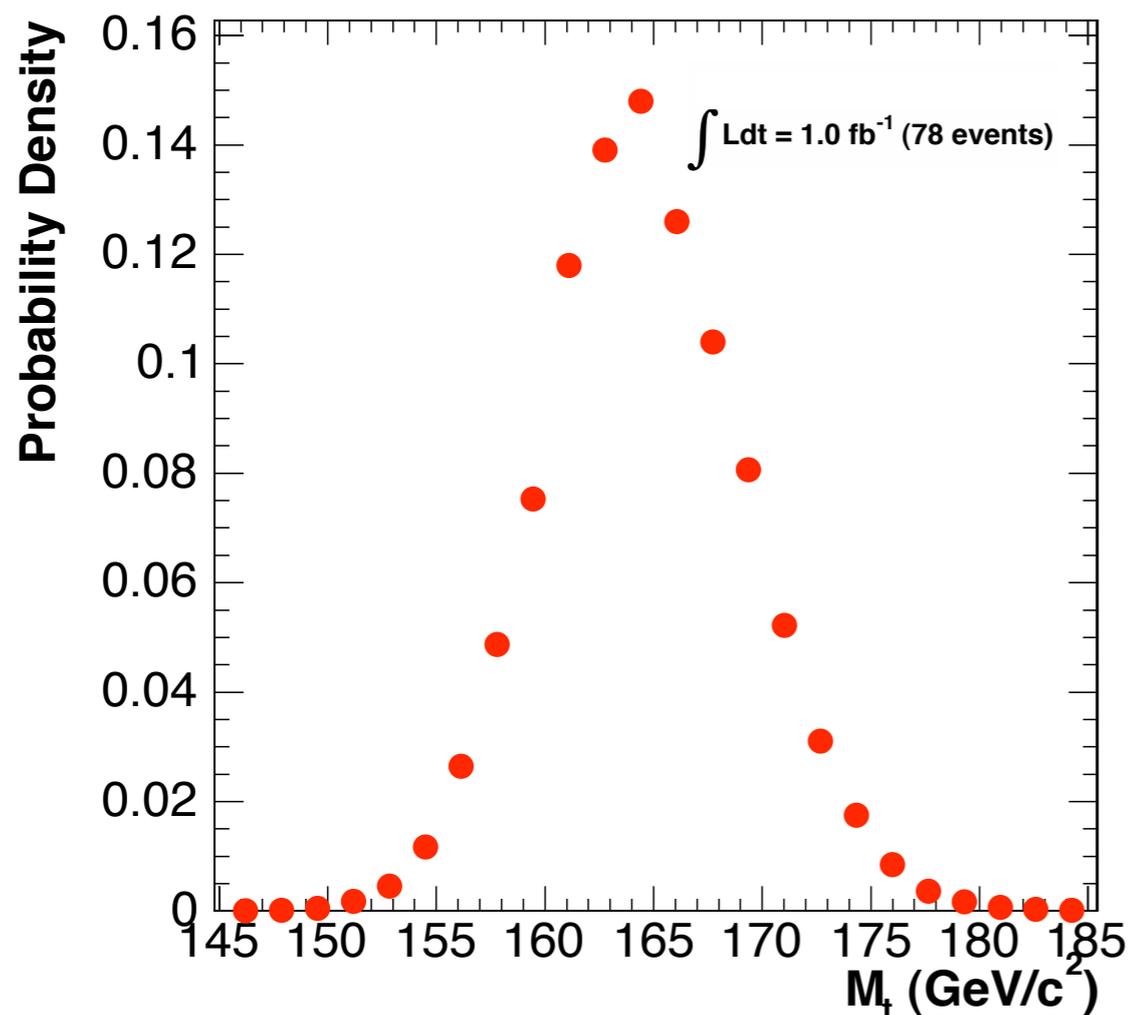
Working on using $Z \rightarrow bb$ to improve

Driven by small sample of (data-based) “fake” lepton events

Improves with better methods and/or more data

Improves with more CPU

Result

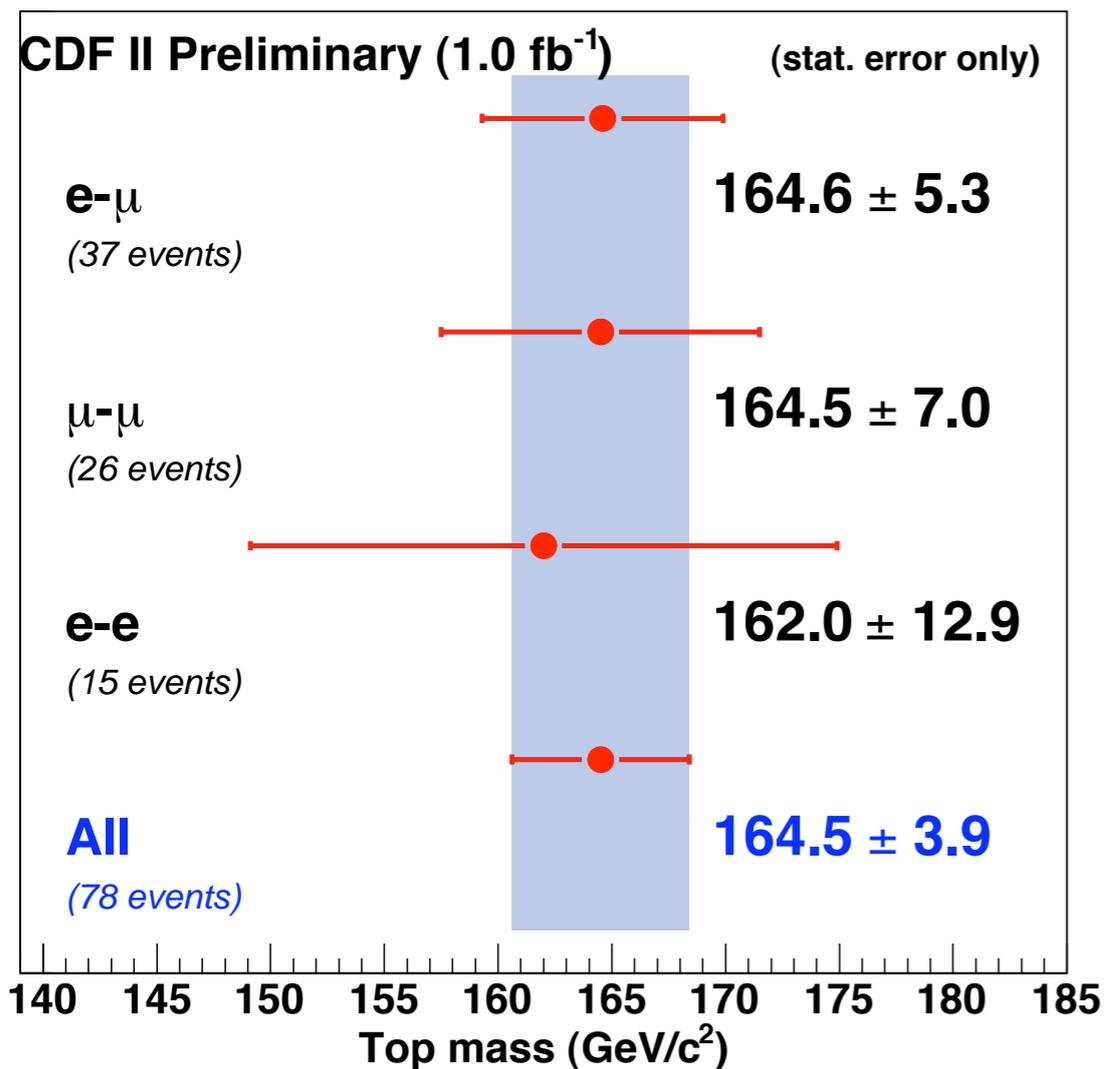


$$M_{\text{top}} = 164.5 \pm 3.9(\text{stat.}) \pm 3.9(\text{syst.}) \text{ GeV}/c^2$$

- **Single most precise** dilepton top mass measurement to-date
 - With no improvements to method, projected stat. error with 4 fb^{-1} is $2.5 \text{ GeV}/c^2$
- Published in PRD **75**, 031105(R)
 - Previously (340 pb^{-1}) PRL **96**, 152002, PRD **74** 032009 (with more detail)

Cross-Checks

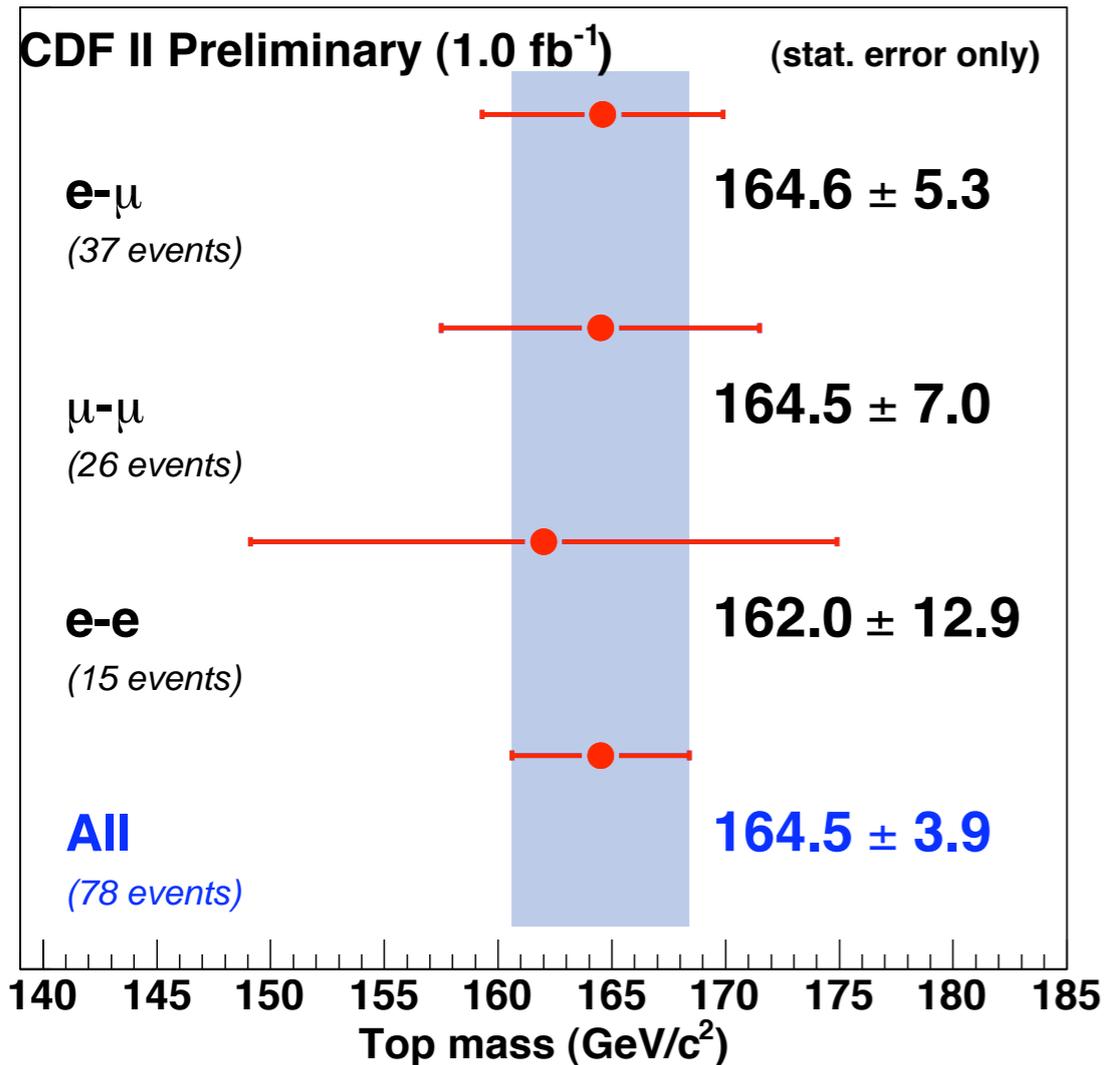
Lepton Flavor



- Measure mass separately for ee , $e\mu$ and $\mu\mu$ events
- Results consistent

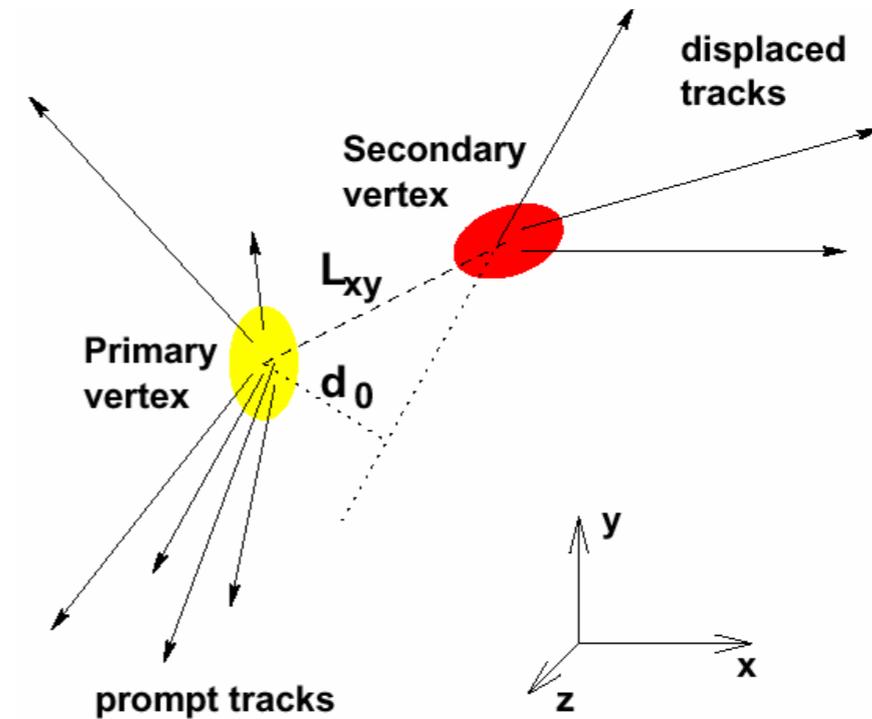
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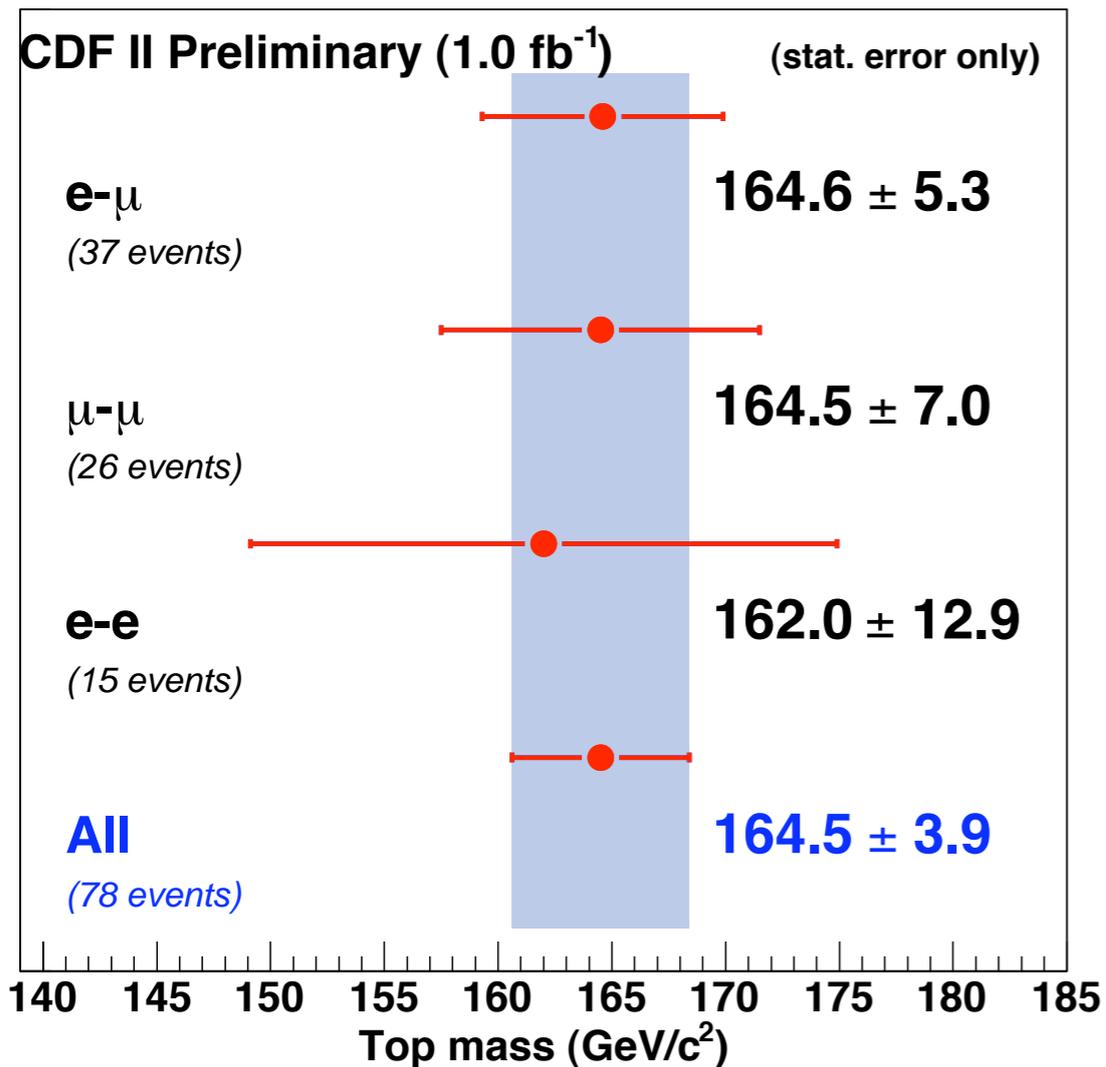
B-tagging



- Use secondary vertex tagging
 - Increases $S:B$ to $\sim 15:1$
 - Retains $\sim 60\%$ of signal events
- See if measurement consistent with full sample

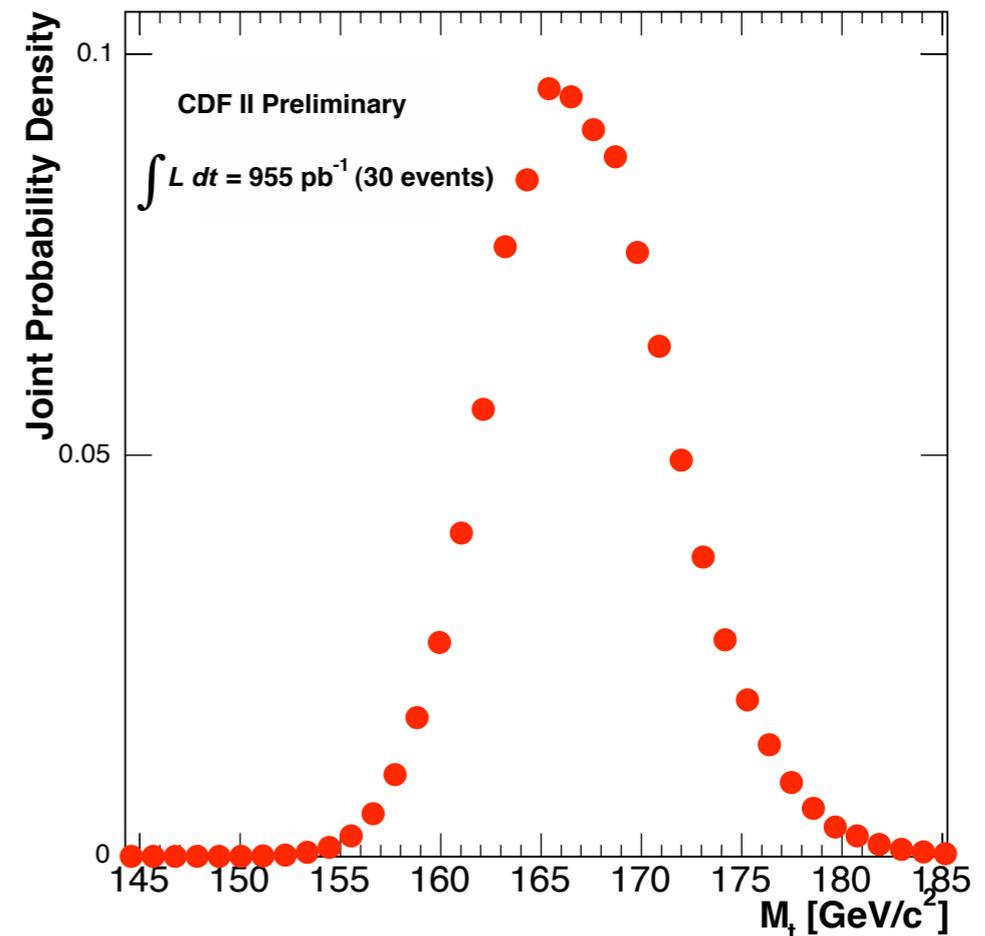
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Lepton Flavor



- Measure mass separately for ee, eμ and μμ events
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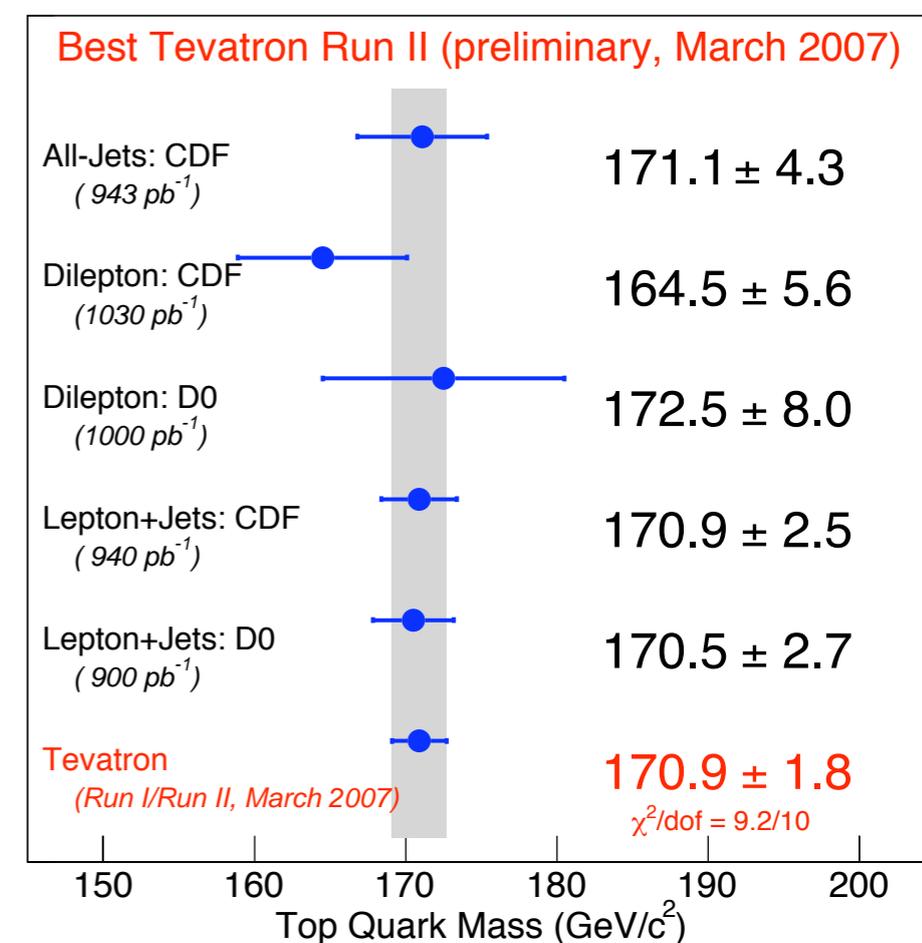


- Use secondary vertex tagging
 - Increases S:B to ~15:1
 - Retains ~60% of signal events
- See if measurement consistent with full sample

$$M_{\text{top}} = 167.3 \pm 4.6(\text{stat.}) \pm 3.8(\text{syst.}) \text{ GeV}/c^2$$

Impact and outlook

- Measurement is included in world average
 - Carries ~5% weight
- Starts to get limited by systematic uncertainty
 - Cannot use *in situ* measurement of JES
 - Can use $Z \rightarrow b\bar{b}$ to measure *b*-jet specific JES
 - Studying genetically evolving neural net selection
 - Studying further optimization of integration



Conclusion

- Application of Matrix Element technique to the dilepton channel
- Most precise single measurement of M_{top} in the dilepton channel

$$M_{\text{top}} = 164.5 \pm 3.9(\text{stat.}) \pm 3.9(\text{syst.}) \text{ GeV}/c^2$$

- Included in current world average
- With no improvements to method, projected stat. error with 4 fb^{-1} is $\sim 2 \text{ GeV}/c^2$
 - Improvements to method in progress

